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A stochastic concept for the optimization of manufacturing tolerances in computer aided process plan simulation

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In order to integrate tolerance synthesis for manufacturing dimensions in CAPP systems, an automated process plan simulation module has previously been developed. This module permits the verification of the manufacturing pre-projects and the optimization of the manufacturing dimensions. The module used an optimization procedure which was realized through an equal distribution of the excess tolerance which is that of the design functional requirement. However in reality, this distribution should take into account the stochastic aspects of the dispersions and the complexity or cost of the manufacturing dimensions. In the present work, in order to overcome these drawbacks, a statistical and cost based tolerance synthesis model has been developed. It is shown that this model performs an objective and global distribution of the residual (excess) tolerances of the design functional dimensions on all the manufacturing dimensions of the process plan. The dispersions method is used in the modelling process to determine the variables of the objective function and to automatically extract the manufacturing tolerance chains. These chains are then used to construct the functional constraints of the optimization model. The whole process has been programmed as an automated tolerancing tool for manufacture and validated for several examples.

Keywords: Manufacturing tolerances; Process plan simulation; Optimization; Statistical model; Dispersions; CAPP

1. Introduction

Industrial products are nowadays appreciated by their quality, their price, their delivery periods and also their availability on the market and all that, in a competing environment. The market pressure and competition are imposing very short development and industrialization cycle times for products. This has led companies to direct their efforts towards an increase in the effectiveness of their design-manufacture process in order to optimize the production cycle of their products. In that order, the use

of computer aided design and manufacture (CAD/CAM) systems has brought much in terms of computer power for production time saving and product quality enhancement. Most of these systems have been independently developed mainly in design (CAD) and process planning in manufacture (CAM). Although the automation of mechanical manufacture has reached a very advanced degree, the activity of manufacturing preparation has known limited computer assistance due to the complexity of the formulation of its various tasks. Among the tasks which lend themselves with difficulty to a complete automation, one

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finds the process plan simulation which approves or disapproves a process plan draft or pre-project as shown in figure 1. Despite the automation of several activities of manufacture in computer aided process planning (CAPP) systems, very few of them have addressed the aspect of process plan simulation and only some solutions were presented in the literature (Fainguelernt et al. 1986, Weill 1988, Halevi and Weill 1995). In a previous work (Hamou et al. 2004), a module for automating the process plan simulation based on the dispersions method also known as the DI method was proposed. This module allows on the one hand the verification of the feasibility of the process plan draft or pre-project through tolerance transfer from design to manufacture. On the other hand, it allows the calculation of the optimized manufacturing dimensions using the process dispersions. The optimization of the manufacturing tolerances applied in this automated procedure was performed through an equal distribution of the excess tolerance of the design dimension condition on the individual components of the manufacturing tolerance chain. However in reality, this distribution should take into account the stochastic aspects of the dispersions as well as the complexity and the cost of the dimensions to be processed where the greatest tolerance should be assigned to the most difficult dimension to process. In this context, for a more objective distribution of the design excess tolerance, a statistical tolerance synthesis model for the manufacturing dimensions is developed and presented in this paper. The dispersions method is used to automatically identify the variables of the objective function and to automatically extract all the manufacturing dimension chains to build the constraints for the tolerance optimization model.

2. Process plan simulation using the DI method

The simulation of the process plan (PP) pre-project is a very significant stage in the manufacturing process of an

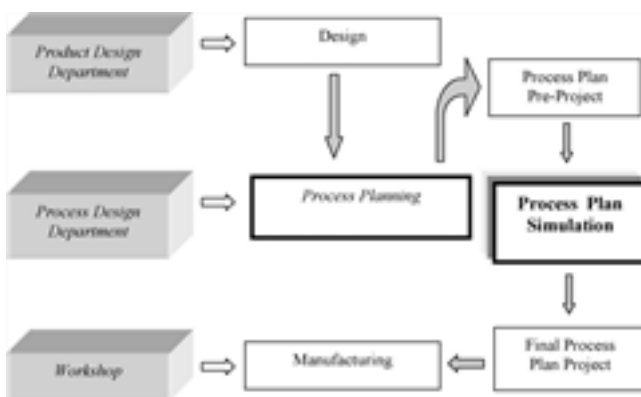


Figure 1. Position of the PP simulation in design and manufacture.

industrial product. It permits the feasibility of the process plan to be checked for all the functional design dimensions (CBE) and process chip dimensions (CBM) and to calculate the optimized manufacturing dimensions. In the literature, there are two popular methods used to simulate the process plan pre-project, the vectorial method and the DI method (Marty and Linares 1994). The latter is more efficiently programmable than the manual vectorial method. In a previous work (Hamou et al. 2004), we have proposed a process plan simulation based on the DI method constructed in the form of three procedures in a given chronological order. Based on the minimal transfer method (Duret 1981), a first procedure performs the verification of the process plan drafts represented in a dispersions matrix format. Then, a second procedure performs an equal optimization of the dispersions. Finally, a third procedure computes the optimized manufacturing dimensions. In the present work, the verification procedure is reformulated so that it can automatically identify all the manufacturing dimensions which have an effect on the design (CBE) including the process minimal chip (CBM) dimensions. In the same way, it allows the determination of the manufacturing tolerance chains from the dispersions matrix obtained by the minimal transfer method (Hamou et al. 2004). To illustrate these stages of identification and calculation, we take the application example of the process plan pre-project of figure 2. This figure shows the design dimension and process dimension specifications, the

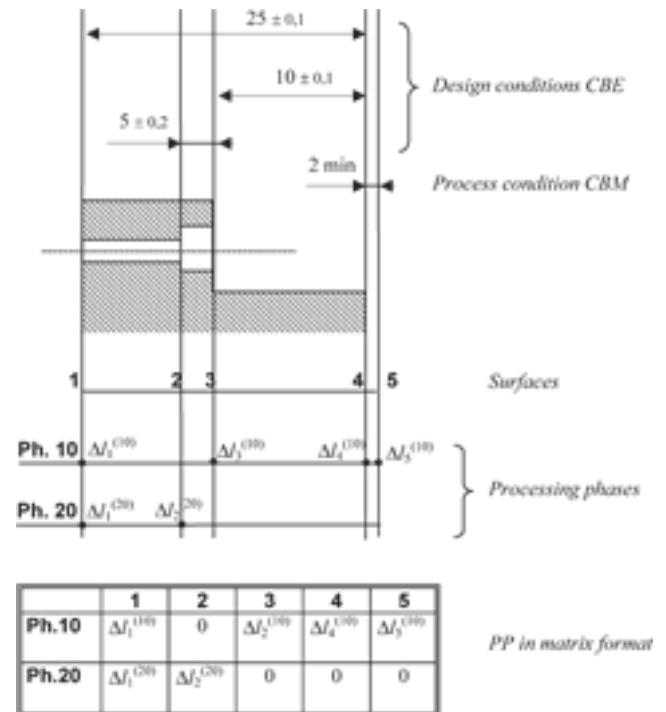


Figure 2. Application example of a PP pre-project.

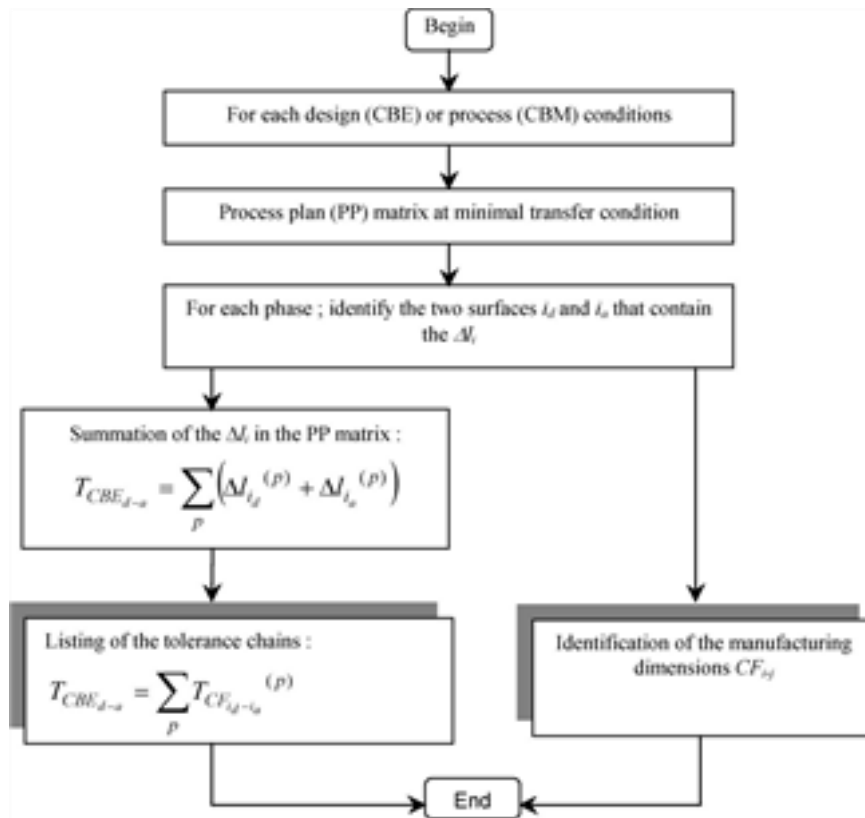


Figure 3. Automated extractions of dimension and tolerance chains.

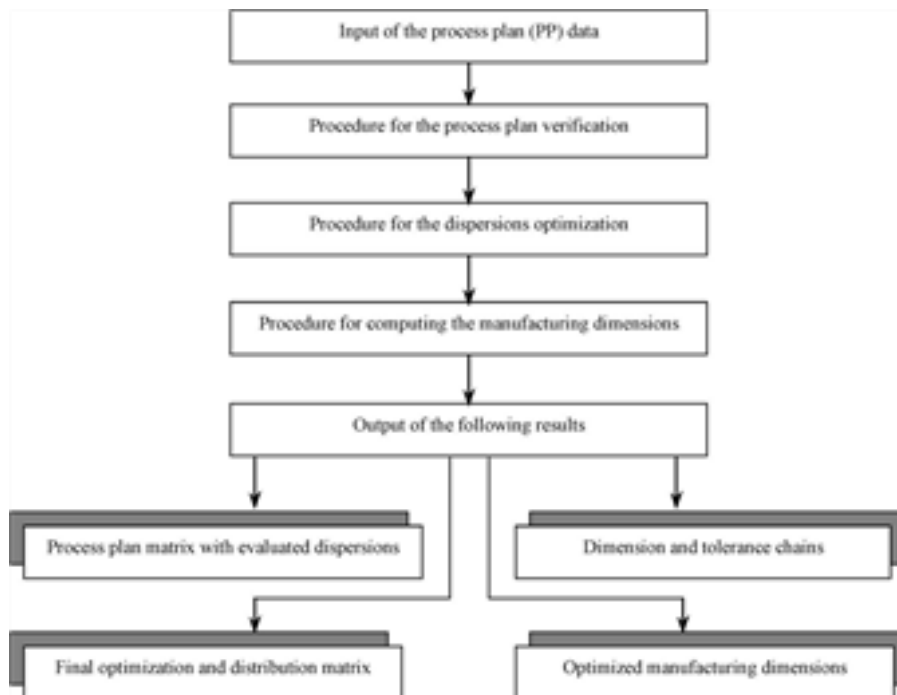


Figure 4. General flowchart of the simulation.

the drawbacks of equal distribution of excess design tolerance, the chains are used to build a mathematical model for the optimization and statistical synthesis of manufacturing tolerances.

3. Statistical tolerance synthesis model

In the previous simulation module (Hamou et al. 2004), the optimization of the manufacturing tolerances was performed through an equal distribution of the excess design tolerance among the manufacturing dimensions (CF) of the chain. However in reality, this distribution should take into account parameters such as the stochastic aspects of the machining dispersions as well as the complexity and the cost of the dimensions to be processed. To satisfy this objective, the arithmetic model for the tolerance chain given by equation (5) is reformulated into a statistical model which will assign the biggest tolerance to the most difficult dimension to machine.

3.1. Arithmetic model

Once the process plan pre-project has been checked for all the functional conditions T_{CC} of the design dimensions (CBE) or the process dimensions (CBM) using equation (6), the process plan becomes a project of manufacture. It is then possible to optimize the dispersions affecting the manufacturing dimensions by increasing the values of the dispersions until equation (7) is satisfied for all the manufacturing tolerance chains.

$$T_{CC} \leq \sum_i D_i \quad \delta 6b$$

$$T_{CC} \leq \sqrt{\sum_i D_i^2} \quad \delta 7b$$

Since the manufacturing tolerances are the resultant of the dispersions affecting the delimiting surfaces of each manufacturing dimension (CF), the arithmetic model is given from equation (7) and equation (5) as follows:

$$T_{CC_j} \leq \sqrt{\sum_{i \in I} T_{CF_i}^2} \quad \delta 8b$$

Where T_{CC_j} denotes in general the tolerance T_{CBE} of the functional design dimension (CBE) or tolerance T_{CBM} of the functional process dimension (CBM) and n_j denotes the number of tolerance components in the manufacturing tolerance chain j .

3.2. Statistical model

Assuming that all the components making up the manufacturing dimension chain (functional design dimension and manufacturing dimensions) are independent and

normally distributed, the statistical model given by equation (9) can be used. This equation which is obtained by applying the statistical parameter variance to the manufacturing dimension chain, gives the relation between the standard deviation s_{CC_j} of the functional dimensions j and the standard deviation s_{CF_i} of the manufacturing dimensions i within the chain.

$$s_{CC_j}^2 \leq \sum_i s_{CF_i}^2 \quad \delta 9b$$

Introducing the coefficient K representing the probability of having a dimension within the tolerance interval T , we can write:

$$T_{CC_j} \leq K s_{CC_j}; \quad T_{CF_i} \leq K s_{CF_i} \quad \delta 10b$$

Replacing s_{CC_j} and s_{CF_i} from equations (10) into equation (9) gives the following general statistical model for the manufacturing tolerance chain:

$$\frac{T_{CC_j}^2}{K^2} \leq \sum_{i \in I} \frac{T_{CF_i}^2}{K^2} \quad \delta 11b$$

In manufacturing practice K is equal to 6 (Tinel and Dardy, 1991) which will give from equation (11) the following root sum squares (RSS) statistical model:

$$T_{CC_j}^2 \leq \sum_{i \in I} T_{CF_i}^2 \quad \delta 12b$$

3.3. Manufacturing cost based tolerance synthesis model

The manufacturing tolerance allocation problem is a matter of manufacturing cost as well as of function and process capability. In fact, the compiled cost-tolerance data in the literature (Peat 1968) such as the one given in figure 5 reflects clearly the existing relationship between cost and manufacturing tolerance. Based on the cost tolerance data presented in this figure, an approach which adequately describes the relationship between tolerance and associated cost is used (Cheikh 1998). It is evident from this figure that the cost-tolerance curve is strongly concave when drawn as a function of the square of the tolerance. As outlined in figure 6, the cost curve for each manufacturing dimension is approximated by a set of small linear segments. The objective function which is the sum of concave functions leads to the formulation of a linear programming problem as can be seen later.

Based on the model of figure 6, let V_{ik} be the slope of the linear segment k in the cost-tolerance curve $C_i \delta T_{CF_{ik}}^2$ when $T_{CF_{ik}}^2 \in [T_{CF_{ik}y1}^2; T_{CF_{ik}y2}^2]$ for the manufacturing dimension i ; where $k \in \{1, 2, \dots, l_i\}$ (l_i : number of segments k for dimension i). $T_{CF_i}^2$ is replaced by the unit tolerance variables X_{ik} defined as $X_{ik} \in [0; T_{CF_{ik}y1}^2]$ and if $X_{ik} > 0$ then $X_{is} \leq \max_{i \in I} \delta X_{is} \leq T_{is}^2 \delta T_{is}^2$ for every s such as $s \leq k$.

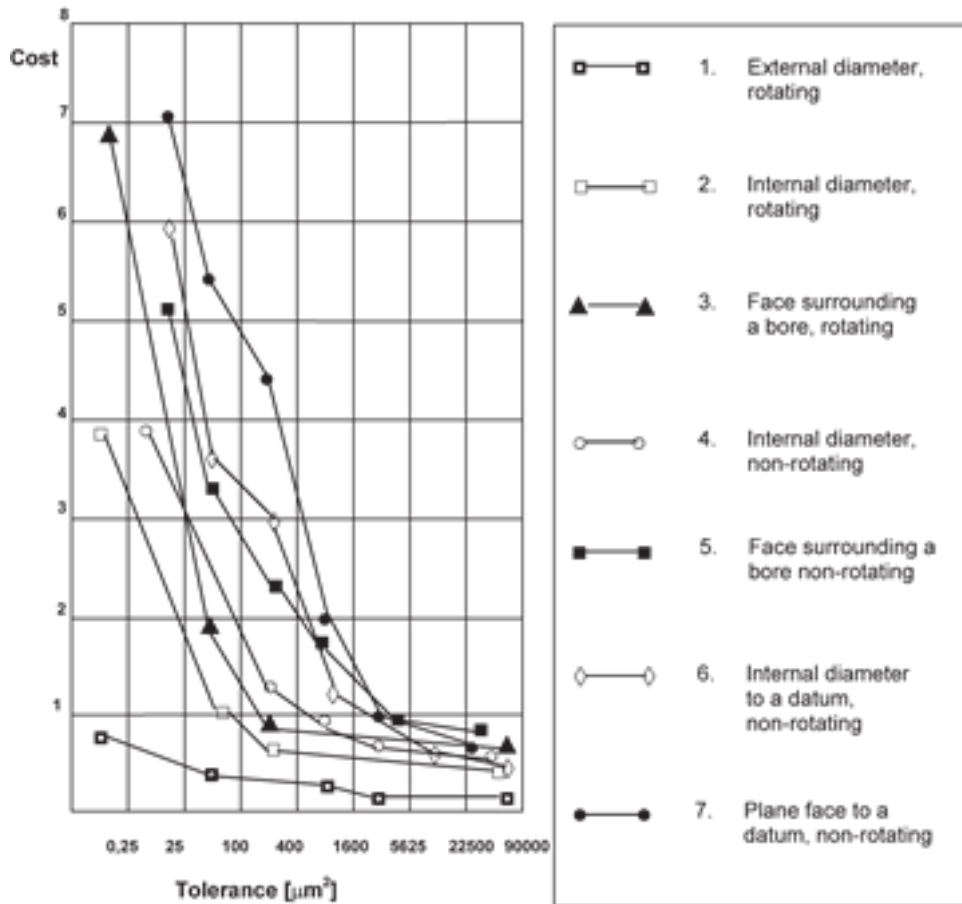


Figure 5. Cost-tolerance database.

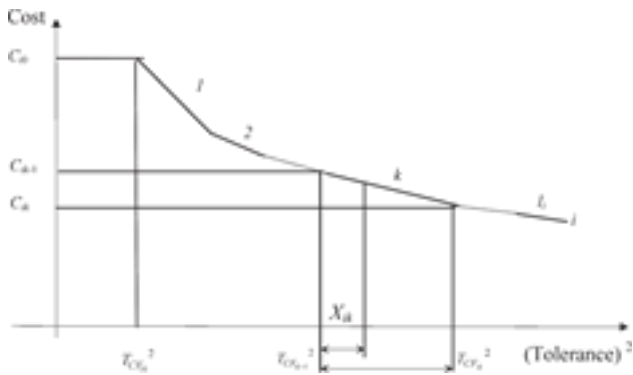


Figure 6. Cost-tolerance model.

The tolerance and corresponding cost for the manufacturing dimension CF_i are given by the following relations:

$$T_{CF_i}^2 = T_{CF_{i0}}^2 \prod_{k=1}^i X_{ik}; \quad \delta i \quad \delta 13b$$

$$C_i = C_{i0} \prod_{k=1}^i V_{ik} X_{ik}; \quad \delta i \quad \delta 14b$$

where the V_{ik} slopes are computed as follows:

$$V_{ik} = \frac{C_{ik} \dot{y}_{C_{ik}y_1}}{T_{CF_{ik}}^2 \dot{y}_{T_{CF_{ik}y_1}}}; \quad \delta i; k \quad \delta 15b$$

The application of equations (13) and (14) to all the manufacturing dimensions affecting a functional dimension condition i.e. a manufacturing dimension chain, gives the following tolerance synthesis model for a dimension chain j :

minimize

$$C_{CC_j} = \prod_{i=1}^j \delta C_i \dot{y}_{C_{i0}p} \prod_{i=1}^j \prod_{k=1}^i V_{ik} X_{ik} \\ \prod_{i=1}^j \prod_{k=1}^i \frac{C_{ik} \dot{y}_{C_{ik}y_1}}{T_{CF_{ik}}^2 \dot{y}_{T_{CF_{ik}y_1}}} X_{ik}$$

subject to

$$\prod_{i=1}^j X_{ik} T_{CC_j}^2 \dot{y}_{T_{CF_{i0}}} = \prod_{i=1}^j T_{CF_{i0}}^2 \\ 0 < X_{ik} < T_{CF_{ik}} \dot{y}_{T_{CF_{ik}y_1}}^2; \quad \delta i; k$$

This optimization model represents a linear programming problem which is solved for the unit tolerance variables X_{ik} using the simplex technique (Murty 1983). The model can be separately applied to all the manufacturing tolerance chains j within the process plan pre-project in order to distribute the functional design tolerance T_{CC_j} among the manufacturing tolerances T_{CF_i} which are computed from the optimized variables X_{ik} using equation (13). However a number of these manufacturing tolerances are common to several tolerance chains that the process plan simulation module must take into account during the tolerance synthesis. Dong and Soom (1994) proposed a solution applied to the design dimension chains where several dimensions are common to several dimension chains within a mechanical assembly. This solution is perfectly adaptable to the case of the manufacturing dimension chains. If there are w dimension chains within the process plan, each dimension chain j can have n_j manufacturing dimensions where m_j dimensions are common to the other chains. This will result in the following tolerance chains:

$$\begin{matrix} 2 \\ \text{tolerance chains}_4 \\ \begin{matrix} T_{CF_{11}} & T_{CF_{12}} & T_{CF_{1n}} & \dots & m_1 \\ T_{CF_{21}} & T_{CF_{22}} & & & m_2 \\ & & & & \dots \\ T_{CF_{w1}} & T_{CF_{w2}} & T_{CF_{wnw}} & & m_w \end{matrix} \end{matrix}$$

In the process plan there will be m manufacturing dimensions common to two or more manufacturing chains; m is given then by:

$$m \approx m_1 \setminus m_2 \setminus \dots \setminus m_w \quad (16)$$

Taking into account the fact of common manufacturing dimensions to several dimension chains and in order to perform the optimization procedure to the whole process plan, the final tolerance synthesis model to be integrated in the process plan simulation is reformulated as follows:

minimize

$$C_{PP} \approx \sum_{j=1}^{n_j} \sum_{i=1}^{m_j} \sum_{k=1}^{m_j} \frac{C_{jik} \cdot \dot{y}_{jik} \cdot C_{jik} \cdot \dot{y}_{jik}}{T_{CF_{jik}}^2 \cdot \dot{y}_{jik} \cdot T_{CF_{jik}}^2} X_{jik}$$

subject to

$$\sum_{i=1}^{n_j} \sum_{k=1}^{m_j} X_{jik} \leq \sum_{i=1}^{n_j} \sum_{k=1}^{m_j} T_{CF_{jik}}^2 \cdot \dot{y}_{jik} \cdot T_{CF_{jik}}^2 \quad (8j); i, k$$

$$\sum_{t=1}^{n_{tk}} \sum_{k=1}^{m_{tk}} X_{tk} \leq \sum_{t=1}^{n_{tk}} \sum_{k=1}^{m_{tk}} T_{CF_{tk}}^2 \cdot \dot{y}_{tk} \cdot T_{CF_{tk}}^2 \quad (8t); k$$

This tolerance synthesis model is built as a linear programming based optimization model (Murty 1983). The optimization process computes the unit tolerance variables X_{jik} and X_{tk} . The computed unit variables X_{jik} are then used to determine $T_{CF_{ji}}$ the individual tolerances for the manufacturing dimensions i in each dimension chain j in the process plan from equation (13) using the following relation:

$$T_{CF_{ji}}^2 \approx T_{CF_{j0}}^2 \cdot \sum_{k=1}^{m_j} X_{jik}; \quad (8j); i \quad (17)$$

On the other hand, the computed unit variables X_{tk} are used to determine T_{CF_t} the tolerances of the manufacturing dimensions common to two or more dimension chains in the process plan from equation (13) using the following relation:

$$T_{CF_t}^2 \approx T_{CF_{t0}}^2 \cdot \sum_{k=1}^{m_{tk}} X_{tk}; \quad (8t) \quad (18)$$

4. Test and model integration in the process plan simulation

The developed statistical tolerance synthesis model has been programmed into the tolerance optimization procedure of the process plan simulation module as illustrated in figure 7. This figure clearly shows that on one side, the model functional constraints are given from the automatically extracted manufacturing dimension chains. On the other side the cost-tolerance objective function is constructed using the automatically identified manufacturing tolerances T_{CF_i} and the cost-tolerance data of figure 5.

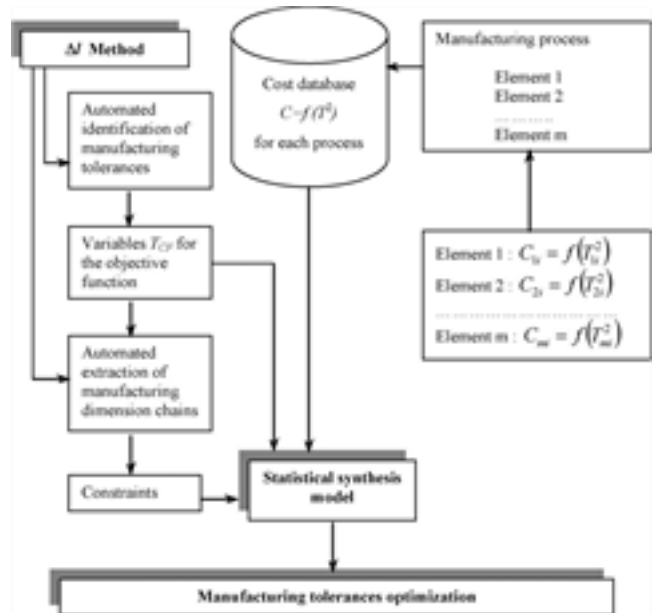


Figure 7. Flowchart of the optimization procedure.

The tasks of chain extraction and tolerance identification are performed using the dispersions (DI) method during the verification procedure of the simulation module as previously explained in figure 3. The statistical tolerance synthesis model has been tested on the sample example of figure 1. The screen of figure 8 gives the results for this example of the simulation module based on the DI method. The screens of figure 9 show the results of the simulation module based on the newly developed statistical tolerance synthesis model. Table 3 gives a comparison of the results given by both the previously developed optimization using the dispersions method and the newly developed synthesis model based on linear programming. These results show that the new optimization procedure performs a better

tolerance distribution in adequacy with the type of manufacturing dimensions since they are obtained using different manufacturing processes and different settings. Moreover these tolerances are increased taking into account the statistical aspects of tolerance stack up in the manufacturing dimension chains. The optimization procedure has been integrated in a computer aided process plan simulation module, has been run on several complicated examples and has given similar results to the sample example.

It is worthy to notice that opposite to the previous procedure where the tolerances were optimized and fixed by processing separately the manufacturing dimension chains depending on a computed weight order, the new procedure

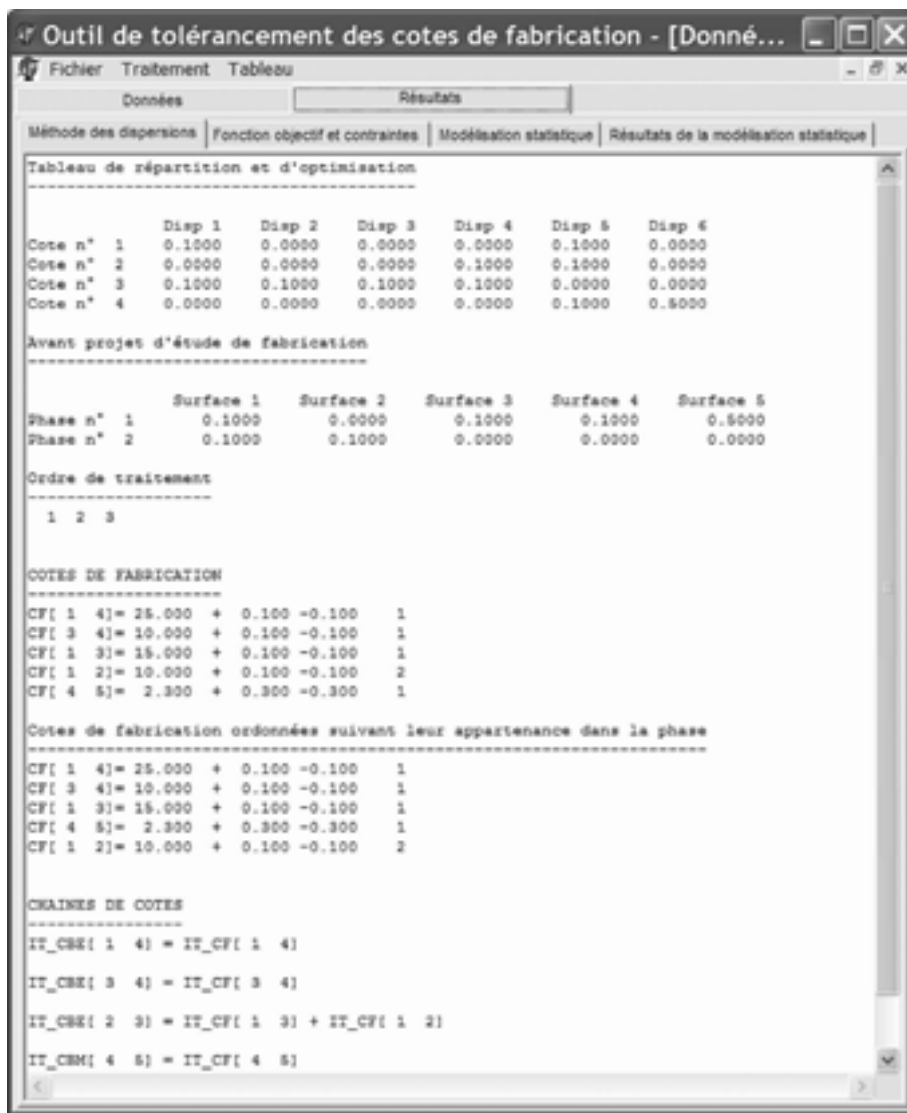


Figure 8. Tolerance optimization using the DI method for the sample example.

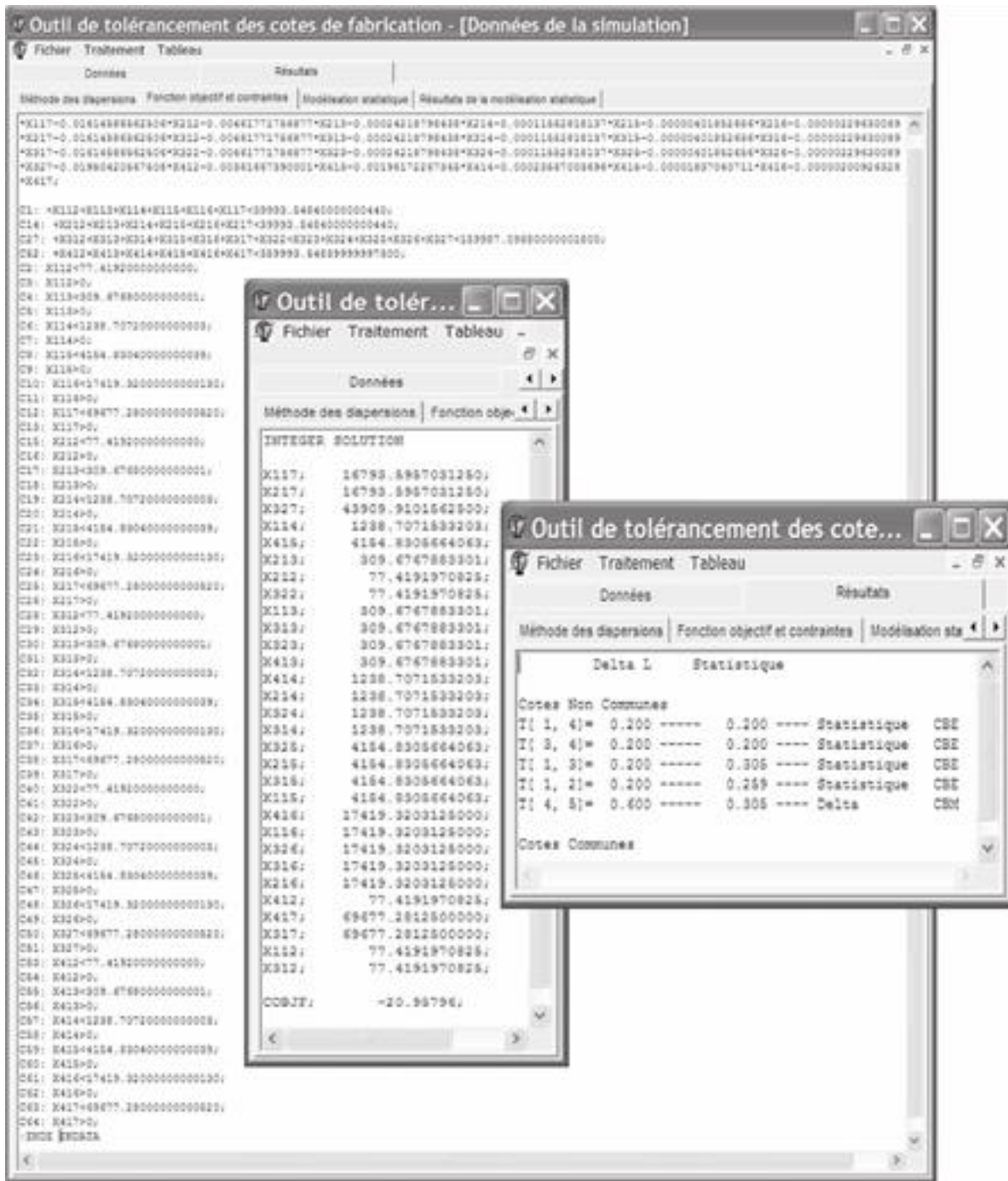


Figure 9. Statistical tolerance synthesis for the sample example.

performs a global optimization of the tolerances for the whole manufacturing process plan. This global optimization solves the whole process plan taking into account interrelated manufacturing chains with common manufacturing dimensions. This case is illustrated for the second sample process plan example of figure 10. The

screens of figure 11 give the simulation process plan data and the optimization results with the DI method. This figure shows from the extracted manufacturing chains that there are three common manufacturing dimensions CF_{2-3} , CF_{2-9} and CF_{2-10} in the process plan. The screens of figure 12 give the results of the simulation module based on the newly

Table 3. Manufacturing tolerances [mm] for the sample example.

Manufacturing tolerance	Distribution by the DI method	Statistical synthesis
$T_{CF_{3y_4}}$	0,200	0,200
$T_{CF_{1y_3}}$	0,200	0,305
$T_{CF_{1y_2}}$	0,200	0,259
$T_{CF_{1y_4}}$	0,200	0,200
$T_{CF_{4y_5}}$	0,200	0,305

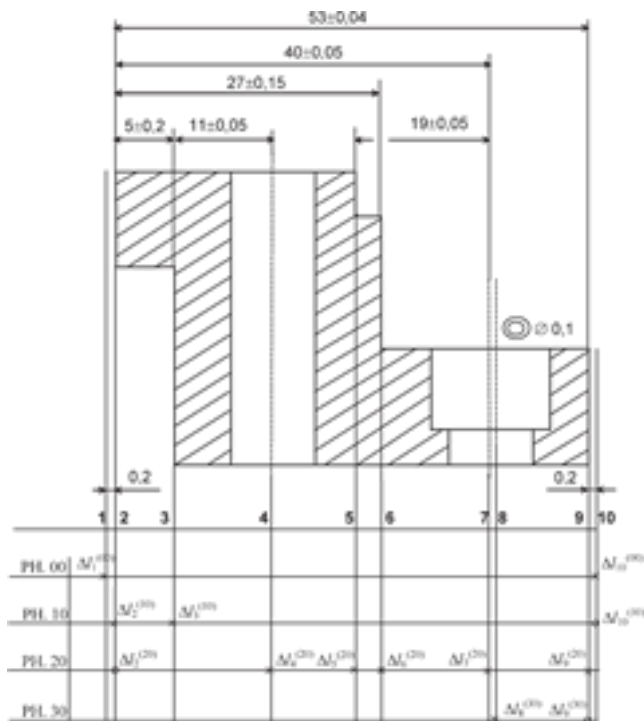


Figure 10. Sample example with interrelated manufacturing chains.

developed statistical tolerance synthesis model where the optimization is performed without fixing any of these common manufacturing tolerances.

5. Conclusions

This paper presents a new procedure for the optimization of manufacturing tolerances in computer aided process plan simulation. This procedure is based on a statistical tolerance synthesis model which globally distributes the functional design and process tolerances among all the manufacturing dimensions involved in the manufacturing dimension chains of the process plan. The model uses

the data extracted from the process plan matrices using the dispersions (DI) method. The optimization objective function of the model is constructed from the identified manufacturing dimensions and the constraints of the model are constructed from the extracted dimension chains. The cost-tolerance data is used to assign the largest tolerance to the most difficult manufacturing dimension to process and so on. The model integrates into its definition the statistical aspects of manufacture and assumes that all the manufacturing dimensions are normally distributed. This RSS model which is reliable to 99,73% requires a severe strategy of inspection of the manufactured parts. However, the model can on the one hand be adapted to take into account general non-normally distributed dimensions by keeping the statistical (standard deviation) parameters into its definition. On the other hand, the model can be reformulated as a worst case model in order to perform a global arithmetic distribution of the functional design tolerances among the components of all the manufacturing dimension chains of the process plan. Since the arithmetic distribution remains the surest way for a safe optimization and simulation, both the arithmetic and statistical tolerance synthesis are made available for use by the process engineers in the developed computer aided process plan simulation module.

Nomenclature

- s: standard deviation for a manufacturing dimension
- DI: dispersion of a machined surface or a positioning surface
- a: second limit surface of a dimension
- d: first limit surface of a dimension
- i: index for a surface; index for a manufacturing dimension
- j: dimension chain or tolerance chain
- k: linear segment in the tolerance-cost curve for a dimension
- l: number of segments in the tolerance-cost curve for a dimension
- m: number of common tolerance components in the process plan
- n: number of tolerance components in the tolerance chain
- p: manufacturing phase or operation
- s: linear segment in the tolerance-cost curve for $s \leq k$
- t: common manufacturing dimension
- w: number of manufacturing dimensions or tolerance chains
- C: cost factor of tolerance
- K: statistical parameter corresponding to the level of confidence
- T: tolerance

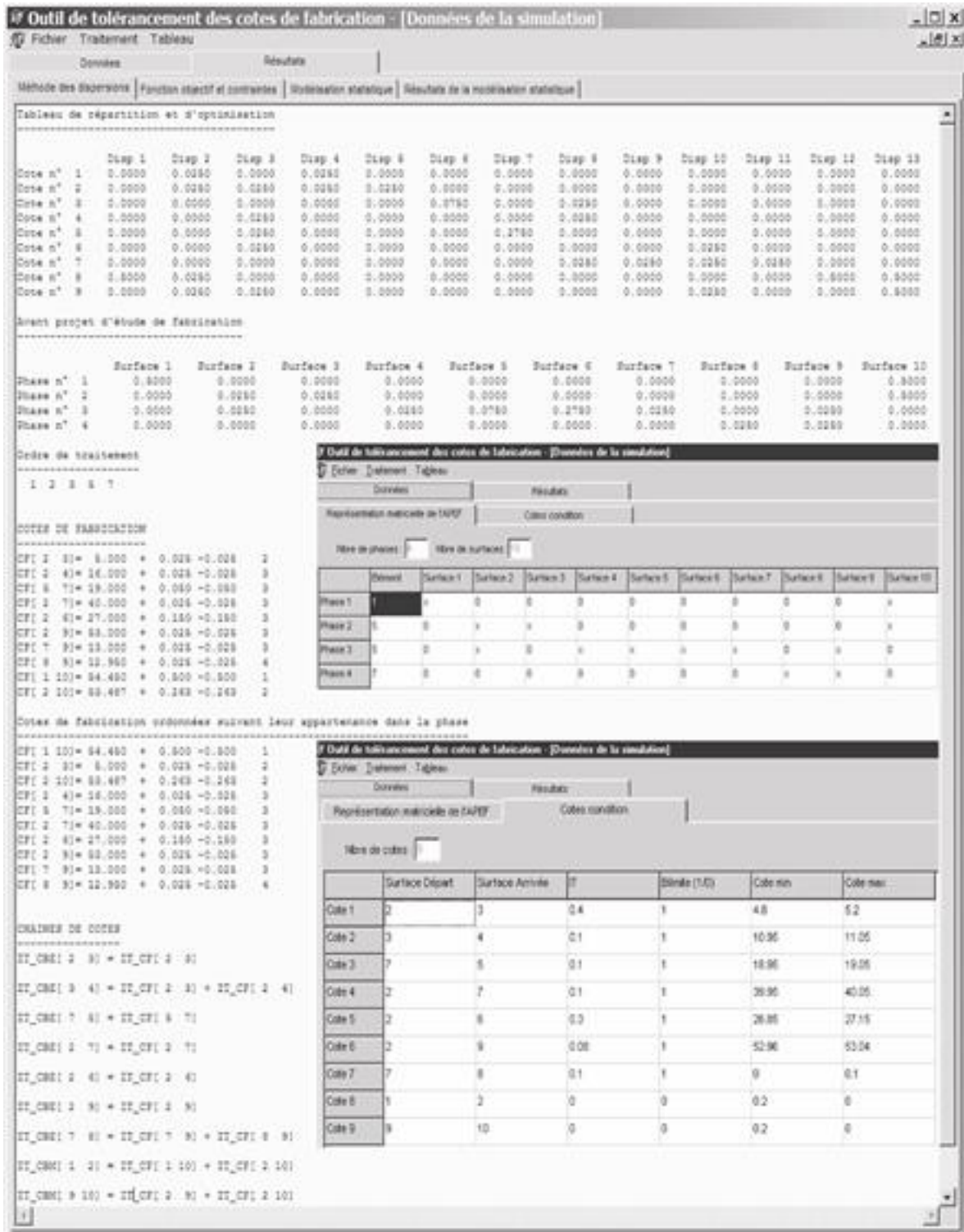


Figure 11. Simulation data and DI optimization results for the second example.

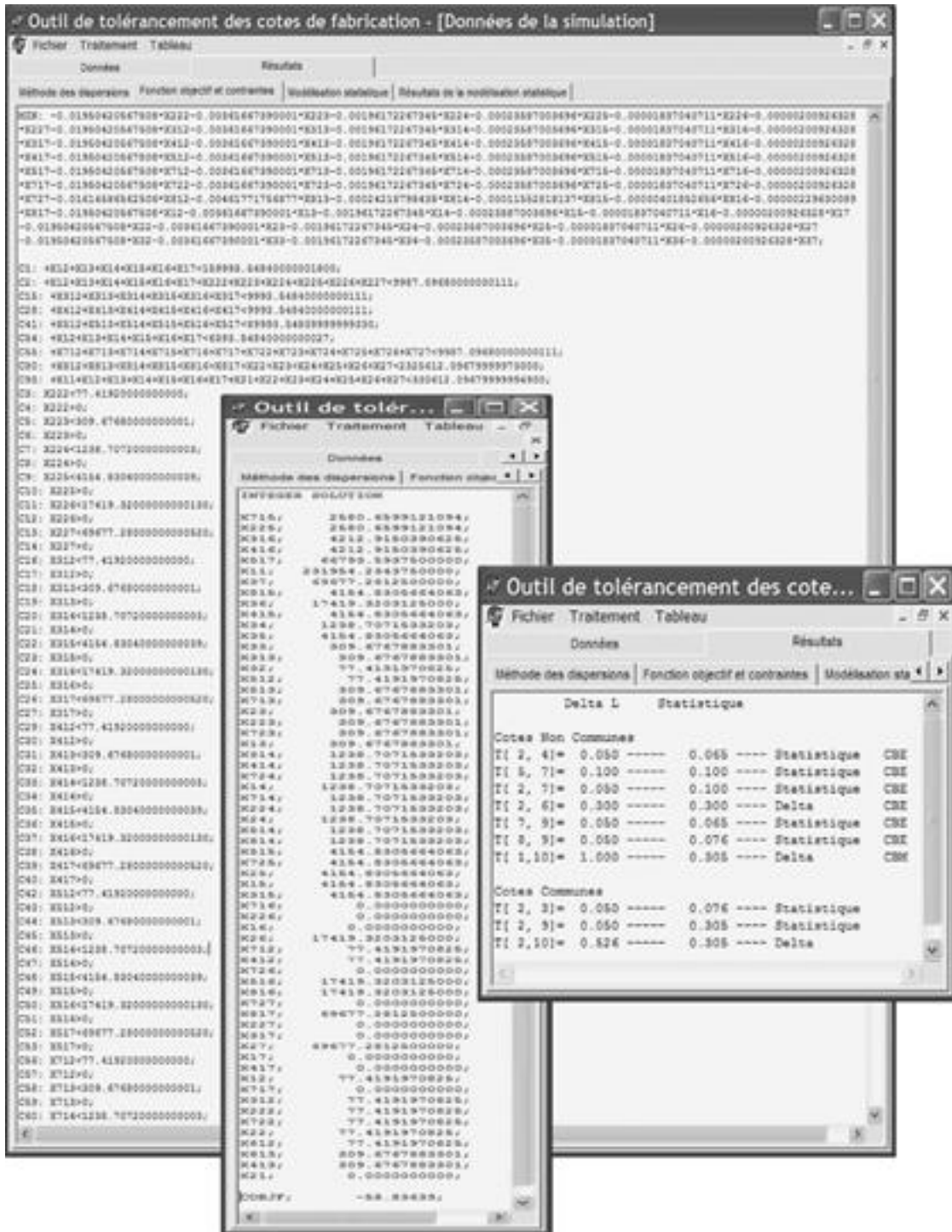


Figure 12. Simplex data and statistical synthesis results for the second example.

X: linear tolerance segment variable in the tolerance-cost curve
V: slope of linear tolerance segment in the tolerance-cost curve
CBE: functional design dimension
CBM: process minimal material removal or chip dimension
CC: design or process dimension condition
CF: manufacturing dimension
PP: process plan

References

- Cheikh, A., Combined statistical optimisation linear programming and mixed integer linear programming tolerance analysis and synthesis models. *Les Annales Maghrébines de l'Ingénieur*, 1998, 12 (Hors série), pp. 743–748.
- Dong, Z. and Soom, A., Automatic optimal tolerance design for related dimension chains, *Manufacturing Review*. American Society of Mechanical Engineers, 1994, 3/4, pp. 262–271.
- Duret, T., Simulation de gamme d'usinage. *Revue de l'Ingénieur et du Technicien de L'enseignement Technique*, 1981, 229, pp. 34–37.
- Fainguelernt, D., Weill, R. and Bourdet, P., Computer aided tolerancing and dimensioning in process planning. *Annals of the CIRP*, 1986, 35(1), pp. 311–315.
- Hamou, S., Cheikh, A., Linares, J.M. and Benamar, A., Machining dispersions based procedures for computer aided process plan simulation. *Int. J. Comput. Integ. Manuf.*, 2004, 17(2), pp. 141–150.
- Halevi, G. and Weill, R.D., *Principles of process planning a logical approach*, 1995 (Chapman and Hall: London).
- Marty, C. and Linares, J.M., *Industrialisation des produits mécaniques: conception et industrialisation*, 1994 (Hermès, Tome1: Paris).
- Murty, K.G., *Linear programming*, 1983 (John Willey & Son: New York).
- Peat, A.P., *Cost reduction charts for designers and process engineers*, 1968 (Machinery Pub Co.: London).
- Tinel, J. and Dardy, F., *Communiquer en conception mécanique*, 1991 (Coter-toléancer, Foucher: Paris).
- Weill, R., Integrating dimensioning and tolerancing in computer aided process planning. *Robotics and Computer Integrated manufacturing*, 1988, 4(1/2), pp. 41–48.