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# Aerial navigation and optic flow sensing: a biorobotic approach 

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#### Abstract

This chapter addresses some of the control problems involved in animal's visually guided 3D piloting. We formulated explicit control schemes which explain how insects may navigate without requiring any distance or speed measurements. The concept of the optic flow regulator, a feedback control system based on optic flow sensors, is presented. Based on a number of behavioral experiments conducted in our laboratory and elsewhere, we explain how $O F$ regulators suffice to account for various insect flight patterns observed over the ground and over still water, under calm and windy conditions, and in straight or tapered corridors. These control schemes were tested in simulation and implemented onboard two types of insect-like robots, a micro-helicopter and a micro-hovercraft, which behaved very much like insects when placed in similar environments. These robots were all equipped with electro-optic OF sensors inspired by the results of our previous microelectrode studies on the motion sensitive neurons present in the flies' eyes. The simple and parsimonious control schemes described here do without any conventional avionic devices such as radio-altimeters, laser rangefinders, variometers, radars, sonars or GPS receivers. While these control schemes are little demanding in terms of neural resources - consistent with their integration in the less-than-one-milligram insect's brain - they show great potential for simplifying the design of aerial and space vehicles, with interesting prospects in weight-reduction and low consumption.


## Introduction

Insects are no more that kind of dumb creatures they used to be. Some insects have well developed learning and memory capacities whose essential mechanisms do not differ drastically from those of vertebrates (Giurfa and Menzel, 1997, Giurfa, 2003). Flying insects have been in the business of sensory-motor integration for more than hundred millions years. These star pilots navigate swiftly through most unpredictable environments, often attaining a level of agility that greatly outperforms that of both vertebrate animals and present day aerial robots. Insects are capable of dynamic stabilization, 3D autonomous navigation, ground avoidance, collision avoidance with stationary and nonstationary obstacles, tracking, docking, decking on movable substrates, autonomous takeoff, hovering, landing, etc. They also behave in a predictive manner, making the appropriate anticipatory postural adjustements that will allow them to take off in the right direction when they notice an approaching threat (Card and Dickinson, 2008).
Insects' neural circuits are highly complex - commensurate with the sophisticated behavior they mediate - but unlike most (no less complex) vertebrate neural circuits, they can be investigated at the level of single, uniquely identifiable neurons, i.e., neurons that can be reliably identified in all the individuals of the species on the basis of their location in the ganglion, their exact shape and their consistent electrical responses. This great advantage of insect versus vertebrate neuroscience enables insect neuroscientists to accumulate knowledge during anything from a few days to several decades about a given individual neuron or a well defined neural circuit (Strausfeld, 1976, Hausen and Egelhaaf, 1989, Frye and Dickinson, 2001).

This chapter deals with the autopilot systems that may allow insects to fly safely without bumping into things. The chapter summarizes our recent attempts to formulate explicit control schemes explaining how insects may navigate without requiring any distance or speed measurements. The aim of these studies was not to produce a detailed neural circuit but rather to obtain a picture that abstracts some basic control laws. We attempted to determine the variables the insect needs to measure, the variables it needs to control, and the causal and dynamic relationships between the sensory and motor variables involved.
The last decades have provided evidence that flying insects guide themselves visually by processing the optic flow (OF) that is generated on their eyes as a consequence of their locomotion. In the animal's reference frame, the translational OF is the angular speed $\omega$ at which contrasting objects in the environment move past the animal as a consequence of locomotion (Kennedy, 1939; Gibson, 1950; Lee, 1980; Koenderink, 1986).
Our progress was achieved by performing simulation experiments and testing our control schemes onboard miniature aerial robots. Constructing a bio-inspired robot first requires exactly formulating the signal processing principles at work in the animal. It gives us, in return, a unique opportunity of checking the soundness and robustness of those principles by bringing them face to face with the real physical world (see also Webb, 2001).
Like the early terrestrial Robot-Fly (the "robot-mouche": Pichon et al., 1989; Franceschini et al., 1992), our aerial robots are based on the use of electronic OF sensors (Blanes, 1986, Franceschini et al., 1986) inspired by the housefly Elementary Motion Detectors (EMDs), which we previously studied in our laboratory (Rev.: Franceschini, 1985, 1992; Franceschini et al., 1989).
After recalling some aspects of the fly visual system and its motion sensitive neurons, we focus on the realisation of fly-inspired OF sensors. We then examine the problem of ground avoidance by flying creatures and introduce the principle of OF regulation. The microhelicopter demonstrator we built is then described, equipped with an electronic OF sensor and an $O F$ regulator. The extent to which the $O F$ regulator concept accounts for the actual
behavioral patterns observed in insects is discussed. The results of recent behavioral experiments on honeybees trained to enter a corridor led us to introduce the dual $O F$ regulator, an OF-based autopilot that is able to control both speed and clearance from the walls. This autopilot's performance was tested in simulation on a micro-hovercraft. We conclude by discussing the potential applications of these insect-derived principles to the navigation of aerial vehicles - in particular Micro Aerial Vehicles (MAVs) and Micro Space Vehicles (MSVs) which, like insects, are not supposed to carry the prohibitively large sensors and control systems present on conventional aircraft.


Figure 1: Head of the blowfly Calliphora erythrocephala with its panoramic compound eyes (left). The right part shows about $2 \%$ of the housefly retinal mosaic. A cluster of micrometer-sized photoreceptors is located in the focal plane of each facet lens : 6 outer receptors R1-6 surround a central cell R7 (prolonged by an R8, not seen here). These are the natural autofluorescence colors of the receptors observed in vivo under blue excitation (Franceschini et al., 1981a,b), after "optical neutralization of the cornea" (Franceschini, 2007).

## The fly visual system and its motion sensitive neurons

Each compound eye consists of an array of ommatidia, the frontend of which is a facet lens that focusses light on a small group of photoreceptor cells (Fig.1, right). The fly retina is among the most complex and best organized retinal mosaic in the animal kingdom. It has been described in great details, with its different spectral types of photoreceptor cells, polarization sensitive cells and sexually dimorphic cells. There exists a typical division of labour within the retina (Rev.: Franceschini, 1984, 1985; Hardie, 1985):

- The two central photoreceptor cells, R7-8, display various spectral sensitivities that are randomly scattered across the retinal mosaic, as attested by the characteristic R7 autofluorescence colors (Fig. 1). R7 and R8 are thought to participate in color vision.
- The outer 6 photoreceptor cells (R1-R6) all have the same, dual-peak spectral sensitivity (blue-green + UV). They participate, in particular, in motion detection (Rev.: Buchner, 1984, Heisenberg and Wolf, 1984; Riehle and Franceschini, 1984). In this visual pathway, signal-to-noise ratio is improved by the presence of an ultraviolet sensitizing
pigment that enhances their quantum catch (Kirschfeld et al., 1977), and by an exquisite optoneural projection called neural superposition (Braitenberg, 1967; Kirschfeld, 1967; Kirschfeld and Franceschini, 1968). The R1-R6 photoreceptors therefore make for a high sensitivity ("scotopic") system (Kirschfeld and Franceschini, 1968).
To estimate the OF, insects use motion sensitive neurons. Flies analyze the OF locally, pixel-by-pixel, via a neural circuit called an "Elementary Motion Detector" (EMD). Further down the neural pathways, more precisely in that part of the third optic ganglion called the lobula plate (LP), about 60 large-field collator neurons called "lobula plate tangential cells" (LPTCs) integrate the outputs of large numbers of EMDs (Rev.: Hausen and Egelhaaf, 1989; Egelhaaf and Borst, 1993; Hausen, 1993). The LPTC neurons analyze the OF field generated by the animal's locomotion (Rev.: Krapp et al., 1998; Borst and Haag, 2002, Taylor and Krapp, 2008). Some of them transmit electrical signals via the neck to thoracic interneurons directly or indirectly responsible for driving the wing-, leg-, or head-muscles. Other LPTCs (in particular, the H1 neuron, Fig.2b) send relevant signals to the contralateral eye. Taking advantage of the micro-optical techniques we had developed earlier (Rev.: Franceschini, 1975), we were able to activate a single EMD in the eye of the living housefly by stimulating single identified photoreceptor cells within a single ommatidium while recording the response of an identified motion sensitive neuron (H1) in the LP (Riehle and Franceschini, 1984, Franceschini, 1985, 1992 ; Franceschini et al., 1989).


Figure 2: (a-c) Principle of the experiment aimed at deciphering the principle of motion vision in flies, using optical stimulation of single photoreceptors. (d) Triple-beam incident light "microscope-telescope" that delivers a $1 \mu \mathrm{~m}$ light spot to two neighboring photoreceptor cells, R1 and R6, successively (see (a)). A microelectrode (c) records the unit response (nerve impulses) of the motion sensitive neuron H1 to this "apparent motion" (Franceschini et al., 1989).

We applied pinpoint stimulation to two neighboring photoreceptors (diameter $\cong 1 \mu \mathrm{~m}$ ) within the selected ommatidium (Fig.2a) by means of a high-precision instrument (a hybrid between a microscope and a telescope: figure 2d), where the main objective lens was a single ocular
facet (diameter $\cong 25 \mu \mathrm{~m}$, focal length $\cong 50 \mu \mathrm{~m}$ ). This laboratory-made optical instrument served to : (i) select the facet lens (Fig. 2a), (ii) select two out of the seven receptors visible in vivo in the back focal plane of the facet lenslet, and (iii) stimulate these two photoreceptors (R1 and R6) successively with $1 \mu \mathrm{~m}$-light spots. Sequential stimulation produced an "apparent motion" that would simulate a real motion within the small visual field of the selected ommatidium. The H1-neuron responded with a vigorous spike discharge only when the motion was mimicked in the preferred direction (see Fig.2c, top trace). The null response observed for the reverse sequence (Fig.2c, bottom trace) attests to the remarkable sequence-discriminating ability of an EMD, which is indeed directionally selective (Franceschini, 1992).
From many experiments of this kind, in which various sequences of light steps and/or pulses were applied to selected receptor pairs, an EMD block diagram was obtained and the dynamics and nonlinearity of each block were characterized (Franceschini, 1985, 1992; Franceschini et al., 1989). While not unveiling the EMD cellular details - still elusive in both vertebrates and invertebrates - our analysis at least allowed the EMD principle to be understood functionally, paving the way for some transcription into another, man-made technology, such as electronics.

## Neuromimetic optic flow sensors

In the mid 1980's, we designed a neuromorphic optic flow sensor (Blanes, 1986, Franceschini et al., 1986), the signal processing scheme of which was inspired by what we had learned from the fly EMD. The OF is an angular speed $\omega$ [rad. $\left.{ }^{-1}\right]$ that corresponds to the inverse of the time $\Delta \mathrm{t}$ taken by a contrasting feature to travel between the visual axes of two adjacent photoreceptors, separated by an angle $\Delta \varphi$. Our OF sensor processes this delay $\Delta t$ so as to generate a response that grows monotonically with the inverse of $\Delta t$, and hence with the optic flow $\omega$ (Fig. 3a). Short delays $\Delta \mathrm{t}$ give higher voltage outputs and vice versa.
(a)


Figure 3: (a) Principle of the electro-optic flow sensor derived from our electrophysiological analyses of the housefly's EMD (Blanes, 1986, Franceschini et al., 1986). (b) purely analogue version (weight 5 grams) built in 1989 for Robot-Fly, whose compound eye housed a ring of 114 EMDs of this type (Pichon et al., 1989 ; Franceschini et al., 1992) (c) hybrid (analogue + digital) version (size : $7 \mathrm{~mm} \times 7 \mathrm{~mm}$, mass 0.2 grams) based on a microcontroller and built using Low Temperature Co-fired Ceramics technology (LTCC) (Pudas et al., 2007).

Our scheme is not a "correlator scheme" (cf Hassenstein and Reichardt, 1956, Reichardt, 1969) and corresponds to the class of "feature-matching schemes" (Ullman, 1981), where a given feature (here a change in intensity that may represent an edge) is extracted and tracked in time. The photodiode signal of each channel is first bandpass filtered (Fig.3a) - resembling the analog signal measured in the large monopolar neurons of the fly lamina (Zettler and Weiler, 1974; Laughlin, 1984). The next step consists of hysteresis thresholding and generation of a unit pulse. In the EMD version built in 1989 for robot Fly (Fig.3b), the unit pulse from one channel was sampling a long-lived decaying exponential function generated by the other channel (Blanes, 1986, Franceschini et al., 1986), via a nonlinear circuit called a minimum detector, to give an output $\omega_{\text {measured }}$ that grows as a monotonic function of the angular velocity $\omega=\Delta \varphi / \Delta t$ (Fig. 3). The thresholding operation makes the voltage output virtually independent of texture and contrast - unlike the Reichardt correlator - and the circuit responds as well to natural scenes (Portelli et al., 2008). A very similar EMD principle has been conceived, independently, a decade later by C. Koch's group at CALTECH, where it became known as the "facilitate and sample" velocity sensor (Kramer et al., 1995). Yet another variant of our original "time of travel" principle was proposed another decade later (Möckel and Liu, 2006).
Since the original analog design, we have built various versions of OF sensors based on this very principle. In the EMD currently used onboard our aerial robotic demonstrators, the signals are processed using a mixed (analog + digital) approach (Ruffier et al., 2003). Such OF sensors can be small and lightweight (the smallest one weighs only 0.2 grams: Fig.3c) and several of them were also recently integrated on a miniature FPGA (Aubépart et al. 2004, 2008; Aubépart and Franceschini, 2007).

## The problem of ground avoidance

To control an aircraft, it has been deemed essential to measure state variables such as groundheight, groundspeed, descent speed, etc. The sensors developed for this purpose usually emissive sensors such as radio-altimeters, laser rangefinders, Doppler radars, GPS receivers, forward-looking infrared sensors, etc. are far too cumbersome for insects or even birds to carry and to power. The OF sensors evolved by natural flyers over the last few hundred million years are at odds with these avionic sensors. They are based on vision, which is a nonemissive sensory system, and more precisely on OF sensors.
The ventral OF experienced in the vertical plane by flying creatures - including aircraft pilots - is the apparent angular velocity $\omega$ generated by a point directly below on the flight track (Gibson et al., 1955; Whiteside and Samuel, 1970). As shown in figure 4a, the ventral OF depends on both the groundspeed $\boldsymbol{V}_{\boldsymbol{x}}$ and the groundheight $\boldsymbol{h}$ and is equal to the ratio between these two variables:

$$
\begin{equation*}
\omega=V_{x} / h\left[\text { rad. } \mathrm{s}^{-1}\right] \tag{Eq.l}
\end{equation*}
$$



Figure 4: Definition (a) and measurement of the ventral optic flow $\omega$ experienced by an insect (or a robot) flying in translation in the vertical plane. (b) an EMD of the type shown in Fig.3, like the EMDs driving the honeybees' VT neurons (Ibbotson, 2001), is able to measure the ventral OF, i.e., the angular speed $\omega$ at which any contrasting feature moves under the flying agent (Franceschini et al., 2007).

We know that flies and bees are able to react to the translational $O F$ independently of the spatial texture and contrast (David, 1982; Kirchner and Srinivasan, 1989, Srinivasan et al., 1991, 1993; Baird et al., 2005). We also know that some of their visual neurons may be involved in this reaction because they respond monotonically to $\boldsymbol{w}$ with little dependence on texture and contrast (Ibbotson, 2001; Shoemaker et al., 2005; Straw et al., 2008). Neurons facing downwards can therefore act as ventral OF sensors, and thus assess the $\boldsymbol{V}_{\boldsymbol{x}} / \boldsymbol{h}$ ratio (Fig.4).
Based on laboratory experiments on mosquitoes and field experiments on locusts, Kennedy put forward an "optomotor theory" of insect flight, according to which flying insects maintain a "preferred retinal velocity" with respect to the ground below (Kennedy, 1939, 1951). In response to wind, for example, insects may adjust their groundspeed or groundheight to restore the apparent velocity of the ground features. Kennedy's hypothesis has been repeatedly confirmed during the last 30 years: both flies and bees were found to maintain a constant OF with respect to the ground while cruising or landing (David, 1978; Preiss, 1992; Srinivasan et al., 1996, 2000, Baird et al., 2006).
The problem is how insects may achieve this feat, since maintaining a given OF is a kind of chicken-and-egg problem, as illustrated by equation 1: an insect may hold its ventral OF, $\omega$ constant by adjusting either its groundspeed (if it knows its groundheight) or its groundheight (if it knows its groundspeed). Besides, the insect could maintain an OF of $1 \mathrm{rad} / \mathrm{s}$ (i.e., $57^{\circ} / \mathrm{s}$ ), for instance, by flying at a speed of $1 \mathrm{~m} / \mathrm{s}$ at a height of 1 meter or by flying at a speed of $2 \mathrm{~m} / \mathrm{s}$ at a height of 2 m : there is an infinitely large number of possible combinations of groundspeed and groundheight that will give rise to the same "preferred OF".
Drawing on the experience we had with OF-based visual navigation of a terrestrial robot (Pichon et al., 1989; Franceschini et al., 1992), we attempted early to develop an explicit flight control scheme for aerial navigation in the vertical plane. Our first tentative step on these lines was not particularly successful, because we were cornered in the general notion that prevailed in those days that insect navigation relies on gauging range (Kirchner and

Srinivasan, 1989; Srinivasan et al., 1991; Franceschini et al., 1992; Srinivasan, 1993). In the experimental simulations we performed in 1994, for example (Mura and Franceschini, 1994), we assumed that the insect (or the robot) would know its groundspeed $\boldsymbol{V}_{\boldsymbol{x}}$ (by whatever means), so that by measuring $\omega$ it would be able to gauge the distance $\boldsymbol{h}$ from the ground (Eq.1) and react accordingly to avoid it. Although this procedure is still used in robotics (see, e.g., Barber et al, 2005; Srinivasan, 2006; Garratt and Chahl, 2008), where groundspeed can be determined (e.g., via GPS), this makes the way insects operate all the more elusive.
In 1999, we established (in simulation) how a rotorcraft (or an insect) might be able follow a terrain (Fig. 5a) and land (Fig. 5b) on the sole basis of OF cues, without measuring its groundspeed and groundheight (Netter and Franceschini, 1999).


Figure 5: Optic flow based terrain following and landing of a miniature helicopter whose eye ( 20 pixels, 19 EMDs) covers a frontal FOV of $75^{\circ}$ in the vertical plane, centered at $40^{\circ}$ below the horizon (a) Simulation of nap-of-the-earth flight (initial conditions: height: 5 m , speed $2 \mathrm{~m} \cdot \mathrm{~s}^{-1}$; iteration step 1 s ). (b) Landing initiated by simply decreasing the rotorcraft horizontal speed at every iteration while retaining the same request to maintain a reference OF value (Netter and Franceschini, 1999). (c) actual flight path of the tethered FANIA rotorcraft, which repeatedly jumped over a $30^{\circ}$ rising terrain (Netter and Franceschini, 2002).

The landing manoeuver was achieved under permanent visual feedback from a 20-pixel forward looking eye (with 19 EMDs). The driving force causing the progressive loss in altitude was the decrease in the horizontal flight speed, which occurred when the rotorcraft (or the insect) decreased its speed to land - either volontarily or in the presence of a headwind. The landing trajectory obtained in this simulation (Fig.5b) already resembles the final approach of bees landing on a smooth surface (Srinivasan et al, 1996). The principle was first validated onboard FANIA, a miniature tethered helicopter having a single (variable pitch) rotor, an accelerometer and a forward looking eye with 20 pixels (and, therefore, 19 EMDs) arranged in the frontal meridian (Netter and Franceschini, 2002). This $0.8-\mathrm{kg}$ rotorcraft had three degrees of freedom (surge, heave and pitch). Mounted at the tip of a flight mill, the robot lifted itself by increasing its rotor collective pitch. Upon remotely inclining the servovane located in the propeller wake, the operator made the helicopter pitch forward by a few degrees so that it gained speed and, therefore, climbed to maintain a reference OF with respect to the terrain below. FANIA was able to jump over a rising terrain by increasing its collective pitch as a function of the fused signals from its 19 EMDs (Fig.5c).

## The optic flow regulation principle

In spite of this early success to explain how an insect could navigate on an OF basis, we considered that Kennedy's insightful "optomotor theory" was calling for a clear formalization that would bring to light:

- the flight variables really involved
- the sensors really required
- the dynamics of the various system components
- the causal and dynamic links existing between the sensory output(s) and the variable(s) to be controlled
- the point of application of the various disturbances that an insect will experience in flight and the variables it will have to control to compensate for these disturbances.

We came up with an autopilot called OCTAVE (OCTAVE stands for Optical altitude Control sysTem for Autonomous VEhicles) that is little demanding in terms of neural (or electronic) implementation and could be just as appropriate for insects as it would be for aircraft (Ruffier \& Franceschini, 2003). A ventral OF sensor was integrated into a feedback loop that would drive the robot's lift, and thus the groundheight, so as to compensate for any deviations of the OF sensor's output from a given set point (Ruffier and Franceschini, 2003, 2004a, b, 2005; Franceschini et al., 2007). As we will see, this simple autopilot (Fig.6a) enabled a microhelicopter to perform challenging tasks such as take-off, terrain following, reacting suitably to wind, and landing.


Figure 6: (A) The OCTAVE optic flow regulator (bottom feedback loop) controls the mean flight force vector and hence the lift, and hence the groundheight, so as to maintain the ventral optic flow $\omega$ constant and equal to the set-point $\omega_{\text {set. }}$. (B) Flies, like helicopters, pitch forward slightly to increase their forward thrust, and hence their airspeed. As long as they pitch forward by $\Theta<10^{\circ}$, the lift component $L$ does not incur any major loss (Franceschini et al., 2007).

The OCTAVE autopilot can be said to be an OF regulator. The word 'regulator' is used here as in control theory to denote a feedback control system designed to maintain an output signal constantly equal to a given set point. The Watt flyball governor from the $18^{\text {th }}$ century, for instance, was not only one of the first servomechanisms ever built: it was also the very first angular speed regulator. It served to maintain the rotational speed of a steam engine shaft at a given set point, whatever interferences occurred as the result of unpredictable load disturbances. The Watt regulator was based on a rotational speed sensor (meshed to the output
shaft), whereas the $O F$ regulator is based on a noncontact rotational speed sensor - an $O F$ sensor - that measures the ventral OF (again in rad/s).
Specifically, the OF signal $\omega_{\text {meas }}$ delivered by the OF sensor (see Fig.6a) is compared with the OF set point, $\omega_{\text {set }}$. The comparator produces an error signal: $\varepsilon=\omega_{\text {meas }}-\omega_{\text {set }}$ which drives a controller adjusting the lift $\boldsymbol{L}$, and thus the groundheight $\boldsymbol{h}$, so as to minimize $\boldsymbol{\varepsilon}$. All the operator does is to set the pitch angle $\boldsymbol{\Theta}$ and therefore the airspeed (see figure 6A): the $O F$ regulator does the rest, that is, it attempts to keep $\omega$ constant by adjusting the groundheight $\boldsymbol{h}$ proportionally to the current groundspeed $\boldsymbol{V}_{x}$. In the steady state $(\mathrm{t}=\infty), \omega_{\text {meas }} \cong \omega_{\text {set }}$, and the groundheight becomes proportional to the groundspeed.

$$
\begin{equation*}
h=K V_{x} \quad\left(\text { with } K=1 / \omega_{\mathrm{SET}}=\text { constant }\right) \tag{Eq.2}
\end{equation*}
$$

The controller includes proportional and derivative (PD) functions, which ensure closed-loop stability in the groundspeed range of $0-3 \mathrm{~m} \cdot \mathrm{~s}^{-1}$. Controlling $\boldsymbol{F}$ (via the rotor speed) actually affects not only $\mathbf{L}$ but also $\boldsymbol{T}$. This coupling is negligible, however, because $\boldsymbol{\Theta}$ is always $\leq$ $10^{\circ}$ for the highest speed attained $\left(3 \mathrm{~ms}^{-1}\right)$, so that the ensuing change in $\boldsymbol{L}$ is at least 6 -times $\left(\operatorname{cotan} 10^{\circ}\right)$ greater than the change in $\boldsymbol{T}$.

## A micro-helicopter equipped with an OF sensor and an OF regulator

We tested the idea that insects may be equipped with a similar OF regulator by comparing the behavior of insects with that of a "seeing helicopter" placed in similar situations. The robot we built (Fig.7a) is a micro-helicopter (MH) equipped with a simple, 2-pixel ventral eye driving an EMD acting as an OF sensor (Fig.7a). The 100-gram robot is tethered to an instrumented flight mill consisting of a light pantographic arm driven in terms of its elevation and azimuth by the MH's lift and forward thrust, respectively (Fig.7b).


Figure 7: (a) 100-gram Micro-helicopter (MH) equipped with a ventral OF sensor (Fig.3e) and the OF regulator shown in A. (b) The MH can be remotely pitched forward by a small angle $\Theta$ while keeping its roll attitude. It lifts itself and circles counterclockwise at speeds up to $3 \mathrm{~m} / \mathrm{s}$ and heights up to 3 m over a large arena (outside diameter: 4.5 m ), giving rise to the flight patterns given in Figs. 8-9 The flight mill is equipped with ground-truth azimuthal and elevation sensors with which the position and speed of the MH can be monitored accurately in real time (Ruffier and Franceschini, 2003).

Any increase in the rotor speed causes the MH to rise, and the slightest (operator mediated) forward ("nose-down") tilting by a few degrees produces a forward thrust component that causes the MH to gain forward speed. The flight mill is equipped with ground-truth azimuthal and elevation sensors that allow the position and speed of the MH to be monitored at high accuracy and in real time. Since the MH purpose was to demonstrate a basic principle, it was equipped with an elementary ventral eye composed of only two photoreceptors driving a single Elementary Motion Detector (EMD) built according to the principle shown in Fig.3a (Ruffier and Franceschini, 2003, Ruffier et al., 2003).

## Micro-helicopter's versus insects' behavioral patterns

OCTAVE's OF regulator scheme results in the behavioral patterns shown in Fig.8. Between arrowheads 1 and 2, the operator simply pitched the MH forward rampwise by an angle $\Delta \Theta=+10^{\circ}$. The ensuing increase in groundspeed $\boldsymbol{V}_{\boldsymbol{x}}$ (up to $3 \mathrm{~m} . \mathrm{s}^{-1}$, see Fig.8B) automatically made the MH take off, since the feedback loop consistently increased $\boldsymbol{h}$ proportionally to $\boldsymbol{V}_{\boldsymbol{x}}$ to comply with equation (3).


Figure 8: Flight variables monitored during a 70-meter flight of the micro-helicopter over a flat, randomly textured pattern (shown at the bottom of (A)), including take-off, level flight and landing at a constant descent angle. (a) Flight path consisting of about six laps on the circular test arena. (B) Groundspeed $\boldsymbol{V}_{\boldsymbol{x}}$. (C) Output $\omega_{\text {meas }}$ of the OF sensor. (D) Actual OF, $\omega$ (calculated as $\boldsymbol{V}_{x} / \boldsymbol{h}$ ) resulting from the behavioral reaction (Franceschini et al., 2007).

Once reaching a constant speed, the MH flew level at a groundheight of approximately 1 m the value imposed by the OF set point $\omega_{\text {set }}=3 \mathrm{rad} . \mathrm{s}^{-1}=172^{\circ} . \mathrm{s}^{-1}$ (Fig.8C). After covering 42m, the MH was pitched backwards rampwise by an opposite angle $\Delta \Theta=-10^{\circ}$ (between arrowheads 3 and 4), and the ensuing deceleration (see Fig.8B) effectively produced an automatic descent and landing - a safe landing maneuver since it is performed "under visual control". The actual OF (Fig.8D) is seen to have been held relatively - but not perfectly constant throughout the journey, even during the takeoff and landing maneuvers where the groundspeed can be seen to vary considerably (Fig.8B).
Figure 9 shows that the various robot's flight patterns are extremely robust and reproducible, including those over a rising terrain and in the presence of wind.


Figure 9: Performance and reproducibility of the micro-helicopter's flight path in the longitudinal plane. (a) automatic take-off obtained by gradually pitching the rotorcraft forward (nose-down) by $10^{\circ}$ from the vertical. (b) automatic terrain following over the rising terrain shown in Fig.6d. (c) automatic approach and landing upon gradually raising the rotor axis vertically (nose-up). (d) a light headwind made the rotorcraft descend (dotted trajectory). A strong headwind forced the MH to land (continuous curve) at negligible vertical and forward speeds (Ruffier and Franceschini, © 2004 IEEE)

The OF regulator concept was found to account for a series of puzzling, seemingly unconnected flying abilities observed in various insect species, as summarized below: (details in Franceschini et al., 2007):

- automatic terrain following. A gradual increase in relief constitutes a "disturbance" that impinges on the system at a particular point (see Fig.7a). The closed feedback loop overcomes this disturbance by increasing the flight altitude, resulting in a constant groundheight over the rising terrain (Fig.9b). This may account for the well-documented terrain and canopy following abilities of migrating insects (e.g., Srygley and Oliveira, 2001).
- suitable reactions to headwind. Windspeed is a disturbance that impinges on the system at a different point (see Fig.6a) and reduces the groundspeed. The feedback loop overcomes this disturbance by forcing the robot to descend (and even to land smoothly by strong wind) (Fig.9d). A similar reaction was observed in locusts, honeybees and dung beetles.
- flying over a no-contrast zone. Here the OF sensor fails to respond, which irremediably causes the robot to crash, just as honeybees crash into mirror-smooth water (Heran and Lindauer, 1963).
- landing on a flat surface. During the final approach, which starts when the MH has regained its completely upright position (arrowhead 4 in Fig.8a and vertical line in Fig.9c), the $O F$ regulator forces the MH to land smoothly at a constant descent angle, $\alpha$, which can be calculated as follows:

$$
\begin{equation*}
\alpha=-\arctan \left(\frac{1}{\omega_{\text {set }} \tau}\right) \tag{Eq.3}
\end{equation*}
$$

where $\omega_{\text {set }}$ [rad.s $\left.{ }^{-1}\right]^{\text {set }}$ is the OF set-point, and $\boldsymbol{\tau}[\mathrm{s}]$ is the MH's surge time constant $\left(\tau_{M H}=\right.$ 2.15 s ).

Interestingly, honeybees were also observed to land with a constant slope on flat surfaces, but the way they may achieve this feat has been explained quite differently. According to Srinivasan et al. (2000), landing bees would follow two rules: "(a) adjusting the speed of forward flight to hold constant the angular velocity of the image of the surface as seen by the eye, and (b) making the speed of descent proportional to the forward speed". By contrast, the OF regulator automatically genrates smooth landing with a constant slope while adjusting neither the forward speed nor the speed of descent.
The OF set point $\omega_{\text {set }}$ is the reference signal that the feedback loop must maintain constant under all circumstances. $\omega_{\text {set }}$ would thus correspond to Kennedy's early ideas about a "preferred angular velocity of image movement" (Kennedy, 1939, 1951). By increasing its $\omega_{\text {set }}$ (see Fig.7A), the flier will follow the terrain at a lower height, as typically observed in the case of the MH (see Ruffier and Franceschini, 2003, Fig.9a). Conversely, by setting $\omega_{\text {set }}$ near zero, the animal will rise farther from the ground, as also typically observed on the MH . This OF set point $\omega_{\text {set }}$ may well be under the control of other (e.g., visual or olfactory) sensors, but it may also depend on other external and/or internal factors such a 'drive for migration' (in the case of locusts: Preiss, 1992)
Taken together, these data show that an aerial vehicle equipped with an $O F$ regulator will be able to take off, navigate over flat or rising terrain, react sensibly to headwind and land without ever measuring and holding any groundheights, groundspeeds or descent speeds. A similar principle was recently applied to a 0.4 kg flying wing, which by flying at a constant cruise speed (imposed by an extra airspeed regulator) was able to maintain its altitude from its ventral OF measurement (Beyeler et al., 2009).

## Micro-hovercraft's versus honeybees' behavioural patterns

Behavioral experiments on several insect species have long shown that motion perceived by the lateral part of their compound eyes affects the forward thrust, and hence the forward speed (rev.: Franceschini et al., 2007). Firstly, when flying through a tapered corridor, honeybees slowed down as they approached the narrowest section and speeded up when the corridor widened beyond this point (Srinivasan et al.,1996). The authors concluded that bees tended to adjust their speed proportionally to the local corridor width by regulating the image velocity. Secondly, when flying through a straight corridor, honeybees tended to fly along the midline (Srinivasan et al.,1991). To explain this "centering behavior", the authors hypothesized that bees were balancing the speeds of the retinal images (i.e., the lateral OFs) of the two walls, an hypothesis that subsequently gave rise to many wheeled and aerial robots capable of centering in a corridor (e.g., Coombs and Roberts 1993; Duchon and Warren, 1995; Santos-Victor et al., 1995).
We recently found, however, that honeybees trained to fly along a larger corridor do not systematically center on the corridor midline (Fig.10b,c). They keep remarkably close to one wall, even when part of the opposite wall is missing (Fig.10d). Distance from that wall ( $\boldsymbol{D}_{\boldsymbol{R}}$ or $\boldsymbol{D}_{\boldsymbol{L}}$ ) and forward speed $\boldsymbol{V}_{\boldsymbol{x}}$ were on average such that the speed-to-distance ratio (i.e., the lateral OF) was maintained practically constant, at about $230^{\circ} / \mathrm{s}$ in our $95-\mathrm{cm}$ wide corridor (Serres et al., 2008a).


Figure 10: Honeybees' centering and wall-following behaviors. Bees were trained to enter a wide (width 0.95 m ) 3 -meter long corridor, formed by two $0.25-\mathrm{m}$ high walls lined with vertical white-and-grey stripes (period 0.1 m ; contrast $\mathrm{m}=0.41$ ). The bee's entrance $\left(\mathrm{E}_{\mathrm{C}}\right)$ and the feeder $\left(\mathrm{F}_{\mathrm{C}}\right)$ were placed either on the corridor midline (a) or on one side ( $\mathrm{b}, \mathrm{c}, \mathrm{d}$ ). In (d), part of the left wall was removed during the trials. Mean distances distribution as shown on top (Serres et al., 2008a).

With a view to explaining the various honeybees' behaviors observed in the various corridors, we came up with the design of the LORA III autopilot (LORA III stands for Lateral Optic flow Regulator Autopilot, mark III), which is able to control both the forward speed $\boldsymbol{V}_{\boldsymbol{x}}$ of an aerial vehicle and its lateral distances $\boldsymbol{D}_{\boldsymbol{R}}$ and $\boldsymbol{D}_{\boldsymbol{L}}$ from the two corridor walls jointly, without ever measuring speed and distances (Fig.11A) (Serres et al., 2008b). A micro-hovercraft (HO) was used, which can produce insect-like forward and sideward slips independently, because the two added lateral thrusters $L T 1$ and $L T 2$ (Fig.11B,C) make it fully actuated. It travels at a constant altitude ( $\sim 2 \mathrm{~mm}$ ) and senses the environment with two laterally oriented eyes measuring the right and left OFs. The HO's heading is maintained along the X -axis of the corridor (Fig.11C) by a heading lock system which compensates for any yaw disturbances by controlling the two rear thrusters differentially. This system mimics the honeybee's heading lock system, which is based on a polarized light compass (Rossel and Wehner, 1972) and gives the insect an impressively straight course even in the presence of wind (Riley and Osborne, 2001) .


Figure 11: (A) LORA III autopilot enabling a hovercraft to navigate in a corridor by controlling its forward speed and its distance to the walls jointly, without measuring any speeds or distances. ( $\mathrm{B}, \mathrm{C}$ ) fully actuated hovercraft (HO) equipped with two OF sensors looking sidewards at an angle of $+90 /-90^{\circ}$. The corridor walls are randomly textured (Serres et al., 2008b).

LORA III autopilot is based on only two OF sensors (one looking to the right, one to the left). The forward speed $\boldsymbol{V}_{\boldsymbol{x}}$ is controlled (via a proportional-integral controller) by the error signal $\boldsymbol{\varepsilon}_{\text {Fwd }}$ between the sum of the two OFs (right and left) and the forward OF set- point $\boldsymbol{\omega}_{\text {setFwd }}$.

The side slip speed $\boldsymbol{V}_{\boldsymbol{y}}$, and thus the lateral distances $\boldsymbol{D}_{\boldsymbol{L}}$ and $\boldsymbol{D}_{\boldsymbol{R}}$ to the walls, is controlled (via a proportional derivative controller) by the error signal $\boldsymbol{\varepsilon}_{\text {side }}$ between the larger of the two OFs and the sideways OF set-point $\omega_{\text {setSide }}$. The HO's behavior is entirely determined by these two OF set points: $\omega_{\text {setFwd }}=300^{\circ} / \mathrm{s}$ and $\omega_{\text {setSide }}=230^{\circ} / \mathrm{s}$.
Simulation experiments where the HO navigated in a straight or tapered corridor accounted for all the honeybees' behaviors reported above (Serres et al., 2008b). Fig. 12 illustrates, for example, the HO's behavior in a tapered corridor. Whatever the position of its initial ordinate $y_{0}$, the HO automatically decelerated on approaching the narrowest section of the corridor and accelerated when the corridor widened. It can be seen that the forward control system succeeded in keeping the sum of the two lateral OFs measured nearly constant and equal to the forward OF set-point $\omega_{\text {setFwd }}=300^{\circ} /$ s (Fig.12c). Likewise, the side control system succeeded in keeping the larger of the two lateral OFs measured practically constant and equal to the sideways OF set-point $\omega_{\text {setSide }}=230^{\circ} / \mathrm{s}$ (Fig.12e). The result is that the HO automatically tuned both its groundspeed an its distance to the walls jointly, without any knowledge about the current corridor width, the groundspeed and the clearance from the walls.


Figure 12: Simulated navigation of the hovercraft (HO) along a tapered corridor, requiring no data on the corridor width, tapering angle $\boldsymbol{\alpha}$, nor any measurements of groundspeed and distance to the walls. (a) Simulated trajectories of the HO moving to the right along the corridor (tapering angle $\alpha=7^{\circ}$ ) with three initial ordinates $y_{0}$ (open dots: $y_{0}=0.90 \mathrm{~m}$, crosses: $y_{0}=0.60 \mathrm{~m}$, full dots: $y_{0}=0.30 \mathrm{~m}$ ). (b) Forward speed profile. (c,d) sum and maximum of the two lateral OFs measured, respectively. (e,f) sum and maximum of the two actual OFs, respectively (Serres et al. 2008b).

The field of view (FOV) of the eyes and the provocatively small numbers of pixels (four) and EMDs (two) will obviously need to be increased for dealing with navigation in more sparsely textured environments. It will also be necessary to control the heading direction (e.g., Zufferey, 2008) to enable the HO to successfully negotiate more challenging corridors including L-junctions and T-junctions (cf Humbert and Hyslop, 2010)

## Conclusion

In studying the types of operations that insects may perform to guide their flight on the basis of optic flow (OF) cues, we came up with several bio-inspired autopilot principles that harness the power of the translatory $O F$ parsimoniously and therefore offer interesting prospects for MAV autonomous guidance. The micro-helicopter's outstanding visuo-motor performance (Fig.7,8) suggests how insects and MAVs may take off, follow terrain and land if they are equipped with OF sensors facing the ground and an OF regulator that servoes the measured OF to a given set point (Fig.6). The great advantage of this autopilot is that it requires neither measuring nor computing nor regulating (i.e., holding constant) any groundspeeds or groundheights. The only variable it needs to measure and regulate is the OF - a variable that can be accessed straight forward by dedicated sensors called OF sensors (Fig.3). The recent finding that bees gradually descend when they fly in a corridor the floor of which is moved in the same direction as their flight, is fully consistent with the OCTAVE autopilot model (Portelli et al., 2010a). The OCTAVE principle differs markedly from another OF-based navigation strategy which requires measuring not only the ventral OF but also the groundspeed (e.g., from GPS), with an aim to estimate the groundheight (see equation (2)) (Barber et al, 2005; Srinivasan et al., 2006, Garratt and Chahl, 2008).

OCTAVE and LORA III autopilots consist of interdependent OF regulators, which control the lift, lateral thrust, and forward thrust, on which the groundheight, lateral position and groundspeed, respectively, depend. The block diagrams (Fig. 6 and Fig.10) show which variables need to be measured, which ones are controlled and which ones are regulated, as well as the point of application of the various disturbances.
In contrast with the control schemes presented by Conroy et al. (2009) for a quadrotor navigating a straight corridor, OCTAVE's task is not to hold a "desired height" and LORA III's task is not to hold a "desired forward speed" and a "desired lateral position" in the corridor. Before entering the corridor, our hovercraft does not know how fast it will eventually fly and whether or not it will center or follow one wall: it is the environment itself that constrains both its speed and its distance to the walls, depending on the OF set points (Fig.12). These explicit control schemes account for a series of flying abilities observed in numerous insect species, including honeybees' habit of landing at a constant slope and their flight pattern along a straight or tapered corridor. Our recent finding that bees do not center systematically in a corridor but may follow a wall unilaterally (Fig.9d) cannot be accounted for by the "optic flow balance hypothesis" (Srinivasan et al., 1991) but is convincingly accounted for by the LORA III model, where "centering behavior" arises as a particular case of "wall-following behavior" (Serres et al., 2008b). OCTAVE and LORA III interdependent OF regulators were recently combined in a comprehensive model, called ALIS (AutopiLot using an Insect-based vision System), which allows a simulated bee to travel safely along (horizontally or vertically) tapered tunnels, by automatically controlling both its speed and its clearance from the right wall, left wall, ground and roof, without ever estimating any groundspeeds or distances (Portelli et al, 2010). The simulated bee navigates on the basis of two parameters alone: the forward OF set-point and the positioning OF set-point. While it is
conceivable that on board insects the OF set points may depend on either innate, internal or external factors, MAVs could receive their OF set-points from the control station via a radiolink.
Once engineered further, the OF-feedback control systems we have described here could serve to improve navigation aids and automatic maneuvers. When measured on a commercial aircraft, a ventral OF greater than the set point would mean that the current altitude is "too low for the current groundspeed" (Franceschini et al., 2003). Installed on board a MAV, the OCTAVE autopilot would enable it to automatically take off, fly level at a groundheight proportional to the groundspeed, follow shallow terrains, make it react automatically to unpredictable headwind or tailwind disturbances (by descending or climbing, respectively), and land safely (Franceschini et al., 2003, Ruffier and Franceschini, 2004, 2005b). Both OCTAVE and LORA III could potentially guide MAVs indoors or through complex terrains such as mountain or urban canyons, without using any computationally intensive visuomotor algorithms. Since these autopilots do not rely on GPS and ILS, and do not require any bulky (and power-hungry) emissive sensors such as RADARs, SONARs, FLIRs, or laser rangefinders, they can be of very small size, lightweight and power-lean, and therefore meet the challenge of future insect-scale MAVs. For the same reasons, these simple autopilots could potentially be adapted to micro- or nano-space vehicles (MSVs) landing on command on other celestial bodies or performing rendezvous and docking missions in space. A recent paper presented the first simulation experiment conducted in our laboratory, showing an OCTAVE-based descent to the Moon (Valette et al., 2010). Over the last 2.6 km , the lander actuated its thrusters as a function of its pitch, so as to brake from $1800 \mathrm{~km} / \mathrm{h}$ down to only $15 \mathrm{~km} / \mathrm{h}$. This descent (from 500 m down to 10 m above the Moon surface) occurred "under visual control", thanks to the ventral OF sensor and the OF regulator, without using any altimeters or speedometers. Throughout descent, the lunar lander maintained an approximately constant OF of about 0.3 rad.s ${ }^{-1}$ (i.e., $17.2^{\circ} \mathrm{s}^{-1}$ ).
An aerial Martian rover equipped with more elaborate OCTAVE and LORA III autopilots could take off autonomously and explore an area, skimming the ground and hugging the walls of a canyon, and adapting its groundspeed and clearance from the walls automatically to the width of the canyon. With ground and obstacle avoidance at a premium, the rover could perform its mission successfully in uncharted environments, despite being unaware of its own groundspeed and altitude at all times. The orbiter (or the Earth-based control station) would simply be required to send the rover a set of low bandwidth signals: the values of the OF set points (Franceschini, 2009).

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