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# Modelling honeybee visual guidance in a 3-D environment

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# Abstract

In view of the behavioral findings published on bees during the last two decades, it was proposed to decipher the principles underlying bees' autopilot system, focusing in particular on these insects' use of the optic flow (OF). Based on computer-simulated experiments, we developed a vision-based autopilot that enables a "simulated bee" to travel along a tunnel, controlling both its speed and its clearance from the right wall, left wall, ground, and roof. The flying agent thus equipped enjoys three translational degrees of freedom on the surge (x), sway (y), and heave (z) axes, which are uncoupled. This visuo-motor control system, which is called ALIS (AutopiLot using an Insect based vision System), is a *dual OF regulator* consisting of two interdependent feedback loops, each of which has its own OF set-point. The experiments presented here showed that the simulated bee was able to navigate safely along a straight or tapered tunnel and to react appropriately to any untoward OF perturbations, such as those resulting from the occasional lack of texture on one wall or the tapering of the tunnel. The minimalistic visual system used here (involving only eight pixels) suffices to jointly control both the clearance from the four walls and the forward speed without

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having to measure any speeds or distances. The OF sensors and the simple visuo-motor control system we have developed account well for the results of ethological studies performed on honeybees flying freely along straight and tapered corridors.

*Key words:* Optic Flow (OF), computational neurosciences, honeybee, speed control, biomimetics, obstacle avoidance.

#### 1 1. INTRODUCTION

Winged insects are able to navigate in unfamiliar environments, using the 2 optic flow (OF) (Gibson, 1950) generated by their own motion (Horridge, 3 1987). Insects make use of the OF to avoid lateral obstacles (Srinivasan et 4 al., 1991; Serres et al., 2008b), control their speed (Preiss, 1987; Baird et al., 5 2005, 2006) and height (Baird et al., 2006; Franceschini et al., 2007), cruise 6 and land (Srinivasan et al., 1996, 2000; Franceschini et al., 2007). Behavioral 7 studies on flying insects have inspired several researchers to develop visually 8 guided mobile robots (Pichon et al., 1989; Franceschini et al., 1992; Coombs 9 and Roberts, 1992; Duchon and Warren, 1994; Santos-Victor et al., 1995; 10 Weber et al., 1997; Lewis, 1997; Netter and Franceschini, 2002; Ruffier and 11 Franceschini, 2003; Humbert et al., 2007; Beyeler et al., 2007). 12

The LORA III autopilot we previously developed was based on a pair of 13 lateral OF regulators steering a *fully actuated* hovercraft, in which the surge 14 and sway dynamics were uncoupled (Serres et al., 2008a). The LORA III 15 autopilot was found to account for the behaviors such as *centering* and *speed* 16 control observed in bees flying along stationary and nonstationary corridors 17 (Srinivasan et al., 1991) as well as tapered corridors (Srinivasan et al., 1996). 18 LORA III also accounted for the novel findings on *wall-following* (Serres et 19 al., 2008b), which the previous hypothesis ("optic flow balance" hypothesis) 20 could not explain. 21

In the ALIS autopilot described here, the LORA III autopilot principle is extended to include the vertical plane. The problem consisted here of developing a functional scheme for a joint speed control and obstacle avoidance system that would take not only *lateral* obstacles but also *ventral* obstacles (Baird et al., 2006; Franceschini et al., 2007), and *dorsal* obstacles (Vickers and Baker, 1994) into account. The ALIS autopilot we designed was used to test a simulated honeybee, in which all the translational degrees of freedom (DOF) (surge, sway, and heave) were uncoupled (Ellington, 1984). In our simulations, the flying agent was endowed with the following novel flight features:

- use of 2-D model for photoreceptor sensitivity,
- use of the walls, ground, and roof, which were all textured with *natural*scenes,

• use of a new linearized model for flying bees' locomotion.

use of an optic flow regulator based on both the *lateral* and the *vertical* OFs.

The ALIS autopilot regulates the OF thanks to the positioning and forward control systems with which it is equipped, according to the following principles:

(i) the first OF regulator adjusts the bee's forward speed so as to keep whichever sum of the two opposite OFs (i.e., left/right or ventral/dorsal) is maximum equal to a *forward OF set-point*. The outcome is that the bee's forward speed becomes proportional to the smallest dimension (either the width or the height) of the flight tunnel. The forward speed attained will be such that the OF generated equals the value of the *forward OF set-point*.

(ii) the second OF regulator adjusts the bee's lateral or vertical position
so as to keep whichever OF is maximum (among the four OFs : left, right,

ventral, and dorsal) equal to the *positioning OF set-point*. The outcome is
that the clearance from the nearest tunnel surface (the walls, ground, or roof)
becomes proportional to the bee's current forward speed, as defined in (i).
The clearance from the nearest tunnel will be such that the OF generated
equals to the *positioning OF set-point*.

The ALIS autopilot enables the agent to perform obstacle avoidance by 54 performing maneuvers involving only translational DOFs, unlike the obsta-55 cle avoidance schemes based on body saccades that involve rotational DOFs 56 (Lewis, 1997; Schilstra and van Hateren, 1999; Tammero and Dickinson, 2002; 57 Beyeler et al., 2007). The ALIS autopilot operates without relying on any 58 speed or distance measurements. It also differs fundamentally from previ-59 ous "insect-like" navigation systems based on speed or distance regulation 60 (Dickson et al., 2006). 61

In section 2, the dynamical model for the simulated bee is described in 62 terms of its three translational DOFs. In section 3, the simulation set-up 63 used to test the ALIS autopilot on board the simulated bee is described. 64 Section 4 describes the ALIS autopilot in detail. Section 5 gives the results 65 of computer-simulated experiments carried out on the simulated bee, which 66 is able to perform various tasks such as takeoff, straight and tapered tunnel-67 following, and to react appropriately to any local lack of lateral or dorsal 68 OF. 69

#### 70 2. DYNAMICAL MODEL FOR BEES' FLIGHT

<sup>71</sup> Here we focus on the visuomotor feedback loops that may explain how <sup>72</sup> a flying insect controls its speed and avoids obstacles. A linearized model

for the bee's dynamics is proposed in terms of the three *translational* DOFs 73 (surge, sway, and heave dynamics). Linearization was justified here by the 74 limited range of speeds (0-2 m/sec) possible. The value of the three rota-75 tional DOFs was kept at zero because bees are known to fly straight to their 76 nectar source (von Frisch, 1948; Riley et al., 2003). In our experiments, the 77 simulated insect was not subjected to any wind disturbances: the ground-78 speed was therefore taken to be equal to the airspeed. The bee's dynamic 79 performances in the three translational DOFs will be described in detail be-80 low. 81

82

# (FIGURE 1 about here)

#### 83 2.1. Bees' Surge dynamics

Experiments on fruitflies (David, 1978) and honeybees (Nachtigall et al., 84 1971; Esch et al., 1975) have shown that flying insects gain forward speed 85 by pitching their mean flight-force vector  $\vec{F}$  forward at a small angle  $\theta_{pitch}$ 86  $(\leq 20 \text{ deg})$  with respect to the vertical (Fig. 1A, B). By slightly changing the 87 wing stroke plane pitch angle  $\theta_{pitch}$ , the insect generates a forward Thrust T, 88 which hardly affects the vertical Lift L (Ellington, 1984). In bees, the mean 89 flight-force vector orientation differs from the body orientation, forming a 90 fixed angle (Nachtigall et al., 1971; Ellington, 1984). 91

#### 92 2.2. Bees' Sway dynamics

In flying hymenopterans, sideslip motion results from roll changes (Ellington, 1984; Zeil et al., 2008). The wing stroke plane roll angle  $\theta_{roll}$  therefore drives the Sideways thrust S (Fig. 1A, C).

#### 96 2.3. Bees' Heave dynamics

The mean flight-force vector  $\vec{F}$  (Eq. 1)resulting from the wing stroke amplitude  $\Phi$  (Dillon and Dudley, 2004; Altshuler et al., 2005) can be expressed in terms of forward Thrust T, Side thrust S, and vertical Lift L.

$$\vec{F} = \left\{ \begin{array}{c} T\\ S\\ L \end{array} \right\} = \left\{ \begin{array}{c} F(\Phi) \cdot \sin \theta_{pitch} \cdot \cos \theta_{roll}\\ F(\Phi) \cdot \cos \theta_{pitch} \cdot \sin \theta_{roll}\\ F(\Phi) \cdot \cos \theta_{pitch} \cdot \cos \theta_{roll} \end{array} \right\}$$
(1)

where  $F(\Phi)$  is the force generated by an amplitude  $\Phi$  of the wing stroke. At small angles ( $\theta_{pitch}$  and  $\theta_{roll}$ ) angles, L is roughly equal to F. The wing stroke amplitude  $\Phi$  therefore mainly drives the vertical lift L.

#### <sup>103</sup> 2.4. Calculating the gain between the wing stroke amplitude and the lift

The lift produced by a bee depends on both the density  $\rho$  of the air and 104 the wing stroke amplitude  $\Phi$  (Dudley, 1995). In order to determine the gain 105  $K_{wing}$  between the wing stroke amplitude  $\Phi$  and the lift L, we used the results 106 of experiments on *hovering bees* that were carried out in media with different 107 densities. Hovering bees were filmed in normal air ( $\rho_{Air} = 1, 21 \text{ kg/m}^3$ ) and 108 in heliox ( $\rho_{Heliox} = 0, 41 \text{ kg/m}^3$ ) (Altshuler et al., 2005). In the low density 109 heliox, bees were found to increase their wing stroke amplitude  $\Phi$  from 90 deg 110 to 130 deg, while keeping their wingbeat frequency constant. In these two 111 hovering situations ( $\theta_{pitch} = \theta_{roll} = 0^{\circ}$ ), the lift L is equal to the weight: 112

$$L_{Heliox}(\Phi = 130 \operatorname{deg}) = L_{Air}(\Phi = 90 \operatorname{deg}) = m \cdot g \cong 1 \operatorname{mN}$$

In a steady state analysis, the lift is proportional to the density at a given stroke amplitude  $\Phi = 130 \deg$  (Ellington, 1984; Sane and Dickinson, 2002):

$$L_{Air}(\Phi = 130 \text{ deg})/\rho_{Air} = L_{Heliox}(\Phi = 130 \text{ deg})/\rho_{Heliox}$$

We therefore calculated  $L_{Air}(\Phi = 130 \text{ deg}) \cong 3 \text{ mN}$ , and obtained the mean sensitivity of the lift production to the wing stroke amplitude,  $K_{wing} = \frac{\partial L_{Air}}{\partial \Phi} = 50 \,\mu\text{N/deg}$  in hovering bees ( $\Phi_{Hover} = 90 \text{ deg}$ ).

#### <sup>118</sup> 2.5. The Linearized Flying Bee model

At small pitch levels  $|\theta_{pitch}| \leq 20 \text{ deg and roll } |\theta_{roll}| \leq 20 \text{ deg angles, each}$ component of the mean flight-force vector  $\vec{F}$  can be linearized on the surge, sway, and heave axes (Eq. 2) as a function of the pitch angle  $\theta_{pitch}$ , the roll angle  $\theta_{roll}$ , and the wing stroke amplitude  $\Phi = \Phi_{Hover} + \Delta \Phi$ , respectively:

$$\vec{F} = \begin{cases} T \\ S \\ L \end{cases} = \begin{cases} m \cdot g \cdot \theta_{pitch} \\ m \cdot g \cdot \theta_{roll} & \text{with } K_{wing} \cdot \Phi_{Hover} = m \cdot g \\ K_{wing} \cdot (\Phi_{Hover} + \Delta \Phi) \end{cases}$$
(2)

The following linearized system of equations was referred to the bee's center of gravity as follows:

$$m \cdot d\vec{V}/dt + Z \cdot \vec{V} = \vec{F} + m \cdot \vec{g} \tag{3}$$

where  $\vec{V}$  is the mean speed vector,  $\vec{F}$  is the mean flight force vector,  $\vec{g}$  is the gravity constant, m = 100 mg (the bee's mass), and Z is the translational viscous friction matrix  $Z = \begin{bmatrix} \zeta & 0 & 0 \\ 0 & \zeta & 0 \\ 0 & 0 & \zeta \end{bmatrix}$ .

The time constant along a translational DOF can be defined by the ratio 128 between the mass and the translational viscous friction coefficient. To the 129 best of our knowledge, no data are available so far on the sway and heave time 130 *constants* in the case of freely flying honeybees but these values are likely to 131 be of the same order as the surge time constant. The bee's surge time constant 132  $\tau\,=\,m/\zeta\,=\,0.22\,{\rm sec}$  can be estimated from bees' landing data (Srinivasan 133 et al., 2000) and from bees OF based autopilot system (Franceschini et al., 134 2007). In what follows, bee sway and bee heave time constants are assumed 135 to be equal to the *bee surge time constant*. 136

Equation 3 can be written as follows:

$$\begin{cases} \tau \cdot dV_x/dt + V_x = (m \cdot g)/\zeta \cdot \theta_{pitch} \\ \tau \cdot dV_y/dt + V_y = (m \cdot g)/\zeta \cdot \theta_{roll} \\ \tau \cdot dV_z/dt + V_z = (K_{wing}/\zeta) \cdot \Delta\Phi \end{cases}$$
(4)

The sensitivity  $K_{surge}$  of the forward speed  $V_x$  to the pitch angle  $\theta_{pitch}$ can be determined from figure 2b in Esch et al. (1975) and estimated as follows:

$$K_{surge} = |\partial V_x / \partial \theta_{pitch}| = 0.10 \text{ m.sec}^{-1}.\text{deg}^{-1}$$

 $K_{sway}$  is assumed to have a similar value:  $K_{sway} = K_{surge}$ 

The Laplace transfer functions giving the bee's surge dynamics  $G_{V_x}(s)$ , sway dynamics  $G_{V_y}(s)$ , and heave dynamics  $G_{V_z}(s)$  can therefore be written as follows:

$$\int G_{V_x}(s) = \frac{V_x(s)}{\theta_{pitch}(s)} = \frac{K_{surge}}{1 + \tau_{surge} \cdot s} = \frac{0.10}{1 + 0.22 \cdot s}$$
(5a)

$$G_{V_y}(s) = \frac{V_y(s)}{\theta_{roll}(s)} = \frac{K_{sway}}{1 + \tau_{sway} \cdot s} = \frac{0.10}{1 + 0.22 \cdot s}$$
(5b)

$$\begin{pmatrix}
G_{V_z}(s) = \frac{V_z(s)}{\Delta \Phi(s)} = \frac{K_{wing}/\zeta_z}{1 + \tau_{heave} \cdot s} = \frac{0.11}{1 + 0.22 \cdot s}$$
(5c)

The pitch angle was limited here to  $\mid \theta_{pitch} \mid \leq 20 \deg$  so as to keep the 145 maximum forward speed range to  $V_{x Max} = 2 \text{ m/sec}$ , and the roll angle was 146 limited to  $|\theta_{roll}| \leq 5 \deg$  so as to keep the maximum lateral speed range 147 to  $V_{yMax} = 0.5 \,\mathrm{m/sec.}$  Bees are thought to reach the maximum stroke 148 amplitude  $\Phi_{max} = 140 \deg$  and the minimum stroke amplitude  $\Phi_{min} =$ 149 70 deg (Dudley, 2000; Dillon and Dudley, 2004). The maximum ascent speed 150  $V_{zUpMax}$  and the maximum descent speed  $V_{zDownMax}$  on the heave-axis are 151 therefore: 152

$$\begin{cases}
V_{zUpMax} = (6a) \\
(K_{wing}/\zeta_z) \cdot (\Phi_{max} - \Phi_{Hover}) = 5.5 \,\mathrm{m/sec} \\
V_{zDownMax} = (6b) \\
(K_{wing}/\zeta_z) \cdot (\Phi_{Hover} - \Phi_{min}) = -2.2 \,\mathrm{m/sec}
\end{cases}$$

The bees' ascent speed, was calculated from figure 7b in Srinivasan et al. (2000) and found to be equal to  $\approx 2 \text{ m/sec}$ . The bees' descent speed measured during landing manoeuvers reaches a value of 2 m/sec (figure 6d in Srinivasan et al. (2000)): this value is quite similar to our own predictions (Eq. 6). In order to limit the vertical speed ( $|V_z| = 2 \text{ m/sec}$ ), we set the maximum stroke amplitude at  $|\Delta \Phi| \leq 18 \text{ deg}$ .

#### 159 3. SIMULATION SET-UP

# 160 3.1. Simulated 3-D environment

169

The simulated 3-D visual environment consisted of a straight or tapered 161 flight tunnel (6 meters long, 1 meter wide, and 1 meter high), the four walls 162 of which were lined with high resolution photographs of natural panoramic 163 scenes (Brinkworth and O'Carroll, 2007). These images were converted into 164 256 gravscale levels and resized keeping the original size ratios. One image 165 pixel corresponded to one millimeter of the simulated environment (Fig. 2). 166 The four natural grayscale images are shown in Fig. 2: right wall (Fig. 2A), 167 left wall (Fig. 2B), roof (Fig. 2C), and ground (Fig. 2D). 168

# (FIGURE 2 about here)

#### <sup>170</sup> 3.2. Optic flow generated by the bee's own motion

The simulated bee was assumed to be flying at a speed vector  $\vec{V}$  along the 171 flight tunnel covered with natural-scene textures (Fig. 2). It has been shown 172 that hymenopterans stabilize their gaze by compensating for any body rota-173 tions (Zeil et al., 2008), in much the same way as the blowfly does (Schilstra 174 and van Hateren, 1999). The bee's head orientation was therefore assumed to 175 be locked to the X-axis of the tunnel. Since any rotation is compensated for, 176 each OF sensor will receive a purely translational OF, which is the angular 177 velocity of the environmental features detected by the lateral (diametrically 178 opposed) and vertical (also diametrically opposed) OF sensors (Fig. 3). 179

The translational OF can be defined simply as the forward speed-todistance ratio (expressed in rad/sec) in line with (7).

$$\omega_i = V_x/D_i, \quad \text{with} \quad i \in \left\{ Rght, Left, Vtrl, Drsl \right\}$$
(7)

where  $V_x$  is the bee's forward speed,  $D_{Rght}$ ,  $D_{Left}$  are the distances to the side (right and left) walls, and  $D_{Vtrl}$ ,  $D_{Drsl}$  are the distances to the ground (ventral eye) and to the roof (dorsal eye) (Fig. 3). Each OF sensor receives its own OF, which can be a right OF ( $\omega_{Rght}$ ), a left OF ( $\omega_{Left}$ ), a ventral OF ( $\omega_{Vtrl}$ ), or a dorsal OF ( $\omega_{Drsl}$ ).

#### (FIGURE 3 about here)

#### 188 3.3. OF sensors on board the simulated bee

187

Bees are endowed with two compound eves, each of which is composed of 189 4500 ommatidia. The visual axes of two adjacent ommatidia are separated 190 by an interommatidial angle  $\Delta \varphi$ , which varies from one region of the eye to 191 another (Seidl and Kaiser, 1981). Each ommatidium is composed of a lens 192 and nine photoreceptor cells with identical receptive fields. Six of these cells 193 have a green spectral sensitivity (Wakakuwa et al., 2005) and are involved 194 in motion vision. These photoreceptor cells are connected to three succes-195 sive visual optic lobes: the lamina, the medulla, and the lobula. Further 196 down the visual processing chain, descending neurons have been found to re-197 spond to object velocity (Velocity-Tuned motion-sensitive neurons VT cells 198 in Ibbotson (2001)). VT neurons respond monotonically to front-to-back 199 translational movements, and therefore act like real OF sensors. Our sim-200 ulated bee is equipped with only four OF sensors (two lateral, one ventral, 201 and one dorsal sensor, Fig. 3A). Each of these sensors consists of only two 202 photoreceptors (two pixels) driving an Elementary Motion Detector (EMD). 203

The visual axes of the two photoreceptors are assumed to be separated by an angle  $\Delta \varphi = 4 \text{ deg}$ . Each photoreceptor's angular sensitivity is assumed to be a Gaussoid function with an acceptance angle (angular width at half height)  $\Delta \rho = 4 \text{ deg}$ , and a total field of view of 10.4 deg × 10.4 deg. The photoreceptors' output was computed at each time step (0.5 msec) by multiplying two matrixes:

• a matrix representing the visible local natural scene (Fig. 2),

• a matrix representing the insect-like photoreceptor Gaussoid sensitivity.

The "time-of-travel" scheme of the bio-inspired EMD developed by Franceschini's research group has been previously described in detail (Blanes, 1986; Pudas et al., 2007; Aubépart and Franceschini, 2007; Franceschini et al., 2009). The response of this OF sensor is a monotonic function of the angular velocity within a 10-fold range (from 40 deg/sec to 400 deg/sec) (Ruffier and Franceschini, 2005), resembling that of the Velocity-Tuned motion-sensitive descending neurons found to exist in honeybees(VT neurons: Ibbotson, 2001).

# 219 4. THE ALIS AUTOPILOT

The simulated bee is controlled by an autopilot called ALIS (which stands for AutopiLot using an Insect-based vision System), which is reminiscent of both the OCTAVE autopilot for ground avoidance (Ruffier and Franceschini, 2005) and the LORA III autopilot for speed control and lateral obstacle avoidance (Serres et al., 2008a) previously developed at our laboratory. The ALIS autopilot relies, however, on four OF measurements: right, left, ventral, and dorsal. We designed the ALIS autopilot assuming that speed control

and obstacle avoidance problems could be solved in a similar way in both the 227 horizontal and vertical planes. The ALIS autopilot consists of two visuomotor 228 feedback loops: the speed control loop (on the surge axis) and the positioning 229 *control* loop (on the sway and heave axes). These two loops work in parallel 230 and are *interdependent*. Each of them involves multiple processing stages 231 (Fig. 4), and each has its own OF set-point: the forward OF set-point and 232 the positioning OF set-point, respectively. In this dual control system, neither 233 the speed nor the distance from the tunnel surfaces (walls, ground, or roof) 234 need to be *measured*. The simulated bee will react to any changes in the OFs 235 by selectively adjusting the three orthogonal components  $V_x$ ,  $V_y$ , and  $V_z$  of 236 its speed vector  $\vec{V}$ . 237

238

# (FIGURE 4about here)

# 239 4.1. Forward speed control and forward speed criterion

The speed control loop was designed to hold the maximum sum of the two 240 diametrically opposed OFs (measured in the horizontal and vertical planes) 241 constant and equal to a forward OF set-point  $\omega_{setFwd}$ . The ALIS autopilot 242 does so by adjusting the forward thrust T (that will determine the forward 243 speed  $V_x$ ). In other words, this regulation process consists in first determining 244 whether the sum of the OFs measured in the horizontal plane  $(\omega_{Rght}^m + \omega_{Left}^m)$ 245 or the sum of those measured in the vertical plane  $(\omega_{Vtrl}^m + \omega_{Drsl}^m)$ , is the 246 larger of the two. The larger of the two sums is then compared with the 247 forward OF set-point  $\omega_{setFwd}$  (blue loop, Fig. 4). The forward OF set-point 248 was set at:  $\omega_{setFwd} = 4.57 \text{ V}$  (i.e., 540 deg/sec). This value was based on that 249 recorded in freely flying bees (Baird et al., 2005). The error signal  $\varepsilon_{Fwd}$  (the 250 input to the surge controller) is calculated as follows: 251

$$\varepsilon_{Fwd} = \omega_{setFwd} - max[(\omega_{Rght}^m + \omega_{Left}^m), (\omega_{Vtrl}^m + \omega_{Drsl}^m)]$$
(8)

The surge controller was tuned using the same procedures as those previously described in the case of the LORA III autopilot (Serres et al., 2008a).

#### 254 4.2. Positioning control and positioning criterion

The *positioning control* loop is in charge of positioning the bee with 255 respect to either the side walls or the ground or the roof of the tunnel. 256 Whether this positioning involves motion on the sway or the heave axis 257 depends on whether the maximum OF measured is in the horizontal or 258 vertical plane. The regulation process adopted here is based on the max-259 imum value of the four OFs measured  $(max(\omega_{Rght}^{m}, \omega_{Left}^{m}, \omega_{Vtrl}^{m}, \omega_{Drsl}^{m}))$ , the 260 red loop in Fig. 4), i.e., the value given by the nearest tunnel surface (walls, 261 ground, or roof). This OF regulator is designed to maintain whichever of 262 the four OFs measured is the larger equal to the positioning OF set-point 263  $\omega_{setPos}$ . The larger OF measured is compared with  $\omega_{setPos}$ , which was set 264 at:  $\omega_{setPos} = 2.4 \text{ V}$  (i.e., 315 deg/sec). This value was again based on that 265 recorded in freely flying bees (Baird et al., 2005). The error signal  $\varepsilon_{Pos}$  (the 266 input to the positioning controller) is calculated as follows: 267

$$\varepsilon_{Pos} = \omega_{setPos} - max(\omega_{Rqht}^{m}, \omega_{Left}^{m}, \omega_{Vtrl}^{m}, \omega_{Drsl}^{m}) \tag{9}$$

The positioning controller was tuned using the same procedures as those previously described in the case of the LORA III autopilot (Serres et al., 2008a).

(FIGURE 5about here)

271

The surface that will be followed (walls, ground or roof) is specified by 272 a Control direction Selector (Fig. 4, 5). The positioning control signal 273 is multiplied by a *direction factor* that corresponds to the *direction of the* 274 maximum OF signal. Note that the sway and heave dynamics can be driven 275 alternately, depending on whichever (lateral or vertical) OF is maximum at 276 any given time. The input to the type of dynamics is *not* commanded is then 277 set at zero (Fig. 5) (Side thrust = 0 or Vertical lift = 0). The simulated 278 bee will react to any unexpected changes in the OFs measured by adjusting 279 either its lateral speed  $V_y$  (and hence its lateral position) or its vertical speed 280  $V_z$  (and hence its vertical position). The OF regulator will always react to 281 the nearest of the four tunnel surfaces. 282

#### 283 5. SIMULATION RESULTS

#### 284 5.1. Automatic tunnel-following

In Fig. 6, the simulated environment is a straight tunnel 6 meters long, 285 1 meter wide, and 1 meter high. Fig. 6A shows a perspective view. Walls, 286 ground, and roof were lined with natural grayscale images (Fig. 2). The 287 simulated bee enters the tunnel at the speed  $V_{x0} = 0.2 \,\mathrm{m/sec}$  and with the 288 initial coordinates  $x_0 = 0.1 \,\mathrm{m}$ , and various couples of  $y_0$  and  $z_0$  (Fig. 6B). 289 Fig. 6C shows the five trajectories in the vertical plane (x, z) and Fig. 6D 290 in the horizontal plane (x, y), plotted every 500 msec. Each bar indicates 291 the honeybee's body orientation, which is known to form a fixed angle with 292 the orientation of the mean flight-force vector (Nachtigall et al., 1971; David, 293 1978). 294

<sup>295</sup> The simulated bee can be seen to have gradually increased both its height

<sup>296</sup> of flight (Fig. 6C) and its right clearance (Fig. 6D) to 0.33 m, while the for-<sup>297</sup> ward speed (Fig. 6E) increased automatically up to 2 m/sec (i.e., the maxi-<sup>298</sup> mum speed allowed) whichever is the initial positions.

These results show that the ALIS autopilot caused the simulated bee to travel safely along the tunnel, while reaching a given forward speed and a given clearance from the walls.

# (FIGURE 6 and FIGURE 7 about here)

# 5.2. Effect of the local absence of contrast on one of the internal faces of the tunnel

Fig. 7 shows successful tests on the behavior of the simulated bee in the presence of "no contrast" zones on the left wall or the roof of the tunnel. These "no contrast" zones could be either a real aperture or a lack of texture (Fig. 7A). The simulated bee was made to enter the tunnel at speed  $V_{x0} =$ 0.2 m/sec with the initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.85 \text{ m}$ (Fig. 7B). Fig. 7C shows the trajectory in the vertical plane (x, z) and Fig. 7D in the horizontal plane (x, y), plotted every 500 msec.

As can be seen from Fig. 7, the simulated bee was not greatly disturbed by either the 2-meter long aperture encountered on its left-hand side (at the beginning of the tunnel) or a similar aperture entering its dorsal field of view (at the end of the tunnel).

The positioning criterion (Fig. 7F) could select either the left or dorsal EMD output ( $\omega_{Left}^m$  or  $\omega_{Drsl}^m$ ) when there were no lateral or vertical OF outputs because of the presence of "no contrast" zones (from X= 0.5 m to X= 2.5 m and from X= 3.5 m to X= 5.5 m). The positioning criterion caused the simulated bee to keep a dorsal clearance  $D_{Drsl} = 0.35 \,\mathrm{m}$  (Fig. 7C) and a left clearance  $D_{Left} = 0.39 \,\mathrm{m}$  (Fig. 7D) throughout its journey.

The forward criterion (Fig. 7G) could select either the vertical or horizontal EMD output when there were no lateral or vertical OF outputs because of the "no contrast" zones encountered (from X= 0.5 m to X= 2.5 m and from X= 3.5 m to X= 5.5 m). This criterion caused the simulated bee to maintain a relatively constant speed  $V_x = 1.85$  m/sec throughout its journey (Fig. 7E).

These results show that the ALIS autopilot enabled the simulated bee to travel safely along the tunnel without being greatly disturbed by the presence of a lateral or dorsal "no contrast" zone.

# 331 5.3. Automatic terrain-following

339

Fig. 8 shows successful tests on the behaviour of the simulated bee on a sloping terrain (slope angle 7,deg). As this sloping zone gradually affected the relative distance from the bee to the ground  $D_{Vtrl}$ , it acted like an OF perturbation (Fig. 8A). The simulated bee was made to enter the tunnel at the speed  $V_{x0} = 0.2$  m/sec with the initial coordinates  $x_0 = 0.1$  m,  $y_0 =$ 0.85 m,  $z_0 = 0.15$  m (Fig. 8B). Fig. 8C shows the trajectory in the vertical plane (x, z) and Fig. 8D in the horizontal plane (x, y), plotted every 500 msec.

(FIGURE 8 about here)

As can be seen from Fig. 8, the simulated bee was not greatly disturbed by the ramp-like slope occurring below its flight path.

The positioning criterion (Fig. 8F) could select either the ventral or left 343 EMD output ( $\omega_{Vtlr}^m$  and  $\omega_{Left}^m$ ). This automatic choice caused the simulated bee to maintain both a ventral clearance and a left clearance (Fig. 8D)
throughout its journey.

The forward criterion can be seen to have mostly opted for vertical EMD outputs ( $\omega_{Vtlr}^m + \omega_{Drsl}^m$ , Fig. 8G) because the ventral slope made the vertical section of the tunnel smaller than its horizontal section. This criterion caused the simulated bee to maintain a relatively constant speed  $V_x = 1.45$  m/sec throughout its journey (Fig. 8E).

These results show that the ALIS autopilot made the simulated bee travel along the tunnel without being greatly disturbed by the sloping ground encountered.

#### <sup>354</sup> 5.4. Automatic speed control in horizontally and/or vertically tapered tunnels

The simulated tunnels used here were 6-meter long, 1-meter high tapered tunnels with a 1-meter wide entrance and a 0.25-meter constriction halfway along the tunnel. This constriction could occur in either the horizontal plane (Fig. 9A) the vertical plane (Fig. 10A), or both planes together (Fig. 11A). These tunnels were designed to test the ability of the ALIS autopilot to overcome several strong OF disturbances at the same time.

(FIGURE 9 and FIGURE 10 about here)

As shown in Fig. 9, the simulated bee was made to enter a tunnel with a midway constriction in the *horizontal* plane, at the speed  $V_{x0} = 0.2 \text{ m/sec}$  and with the initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.15 \text{ m}$  (Fig. 9B). Fig. 9C shows the trajectory in the vertical plane (x, z) and Fig. 9D in the horizontal plane (x, y), plotted every 500 msec.

The simulated bee followed the left wall of the tapered tunnel, simply 367 because its starting point was close to that wall. The positioning criterion 368 (Fig. 9F) selected the left EMD output  $(\omega_{left}^m)$ , which remained approximately 369 equal to the *positioning OF set-point* throughout the journey (Fig. 9F). The 370 simulated bee kept a safe left clearance throughout its journey. The simulated 371 bee automatically slowed down as it approached the narrowest section of the 372 tapered tunnel, and accelerated again when the tunnel widened out beyond 373 that point (Fig. 9E). Since the tunnel narrowed only in the horizontal plane, 374 the OF in the vertical plane was of little relevance to the speed control part 375 of the ALIS autopilot. The forward speed depended mostly on the OF in 376 the horizontal plane  $(\omega_{Left}^m + \omega_{Rght}^m, \text{Fig. 9G})$  because the horizontal section 377 of the tunnel was smaller than its vertical section. 378

The ALIS autopilot made the simulated bee travel safely along the "horizontal" tapered tunnel (tapering angle 7 deg) without being greatly perturbed by the major OF disturbance concomitantly detected by both its left and right OF sensors.

As shown in Fig. 10, the simulated bee was then made to enter a tun-383 nel with a midway constriction in the vertical plane, at the speed  $V_{x0}$  = 384 0.2 m/sec, with the initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.15 \text{ m}$ 385 (Fig. 10B). Fig. 10C shows the trajectory in the vertical plane (x, z) and 386 Fig. 10D in the horizontal plane (x, y), plotted every 500 msec. In this case, 387 the simulated bee followed both the ground and the left wall of the tapered 388 tunnel, simply because its starting point was near to the ground and the 389 left wall. The positioning criterion could select either the ventral or left OF 390 measured ( $\omega_{Vtlr}^m$  and  $\omega_{Left}^m$ ), which remained approximately equal to the *po*-391

sitioning OF set-point throughout the journey (Fig. 10F). The simulated bee
kept a safe ventral and left clearance throughout its journey.

The simulated bee automatically slowed down as it approached the narrowest section of the tapered tunnel, and accelerated again when the tunnel widened out beyond that point (Fig. 10E). As the tunnel narrowed only in the vertical plane, the OF in the horizontal plane was of little relevance to the speed control part of the ALIS autopilot. The forward speed depended mostly on the OF in the vertical plane ( $\omega_{vtrl}^m + \omega_{Drsl}^m$ , Fig. 10G) because the vertical section of the tunnel was smaller than its horizontal section.

The ALIS autopilot made the simulated bee travel along the vertically tapered tunnel (tapering angle 7 deg) without being greatly perturbed by the major OF disturbance concomitantly detected by both its ventral and dorsal OF sensors.

405

#### (FIGURE 11 about here)

As shown in Fig. 11, the simulated bee was then made to enter the tunnel 406 with midway constrictions in both the horizontal and vertical planes. The bee 407 entered at the speed  $V_{x0} = 0.2 \text{ m/sec}$  with the initial coordinates  $x_0 = 0.1 \text{ m}$ , 408  $y_0 = 0.85 \,\mathrm{m}, z_0 = 0.15 \,\mathrm{m}$  (Fig. 11B). Fig. 11C shows the trajectory in the 409 vertical plane (x, z) and Fig. 11D in the horizontal plane (x, y), plotted every 410 500 msec. The simulated bee followed both the ground and the left wall of 411 the tapered tunnel, simply because its starting point was near the ground 412 and the left wall. The positioning criterion could select either the ventral or 413 the left OF measured ( $\omega_{Vtrl}^{m}$  and  $\omega_{Left}^{m}$ ), which remained approximately equal 414 to the positioning OF set-point throughout the trajectory (Fig. 11F). The 415 simulated bee kept a safe ventral and left clearance throughout its journey. 416

The simulated bee automatically slowed down as it approached the nar-417 rowest section of the tapered tunnel and accelerated again when the tunnel 418 widened out beyond this point (Fig. 11E). As the tunnel narrowed in both the 419 horizontal and vertical planes, the OFs in the horizontal and vertical planes 420 were both equally relevant to the speed control part of the ALIS autopilot. 421 The forward speed depended on the OFs in both the horizontal and vertical 422 planes  $(\omega_{Rqht}^m + \omega_{Left}^m \text{ and } \omega_{Vtlr}^m + \omega_{Drsl}^m, \text{ Fig. 11G})$  because the horizontal and 423 the vertical sections of the tunnel both varied to an equal extent. 424

The ALIS autopilot made the simulated bee cross the "horizontal and vertical" tapered tunnel (tapering angle 7 deg in both planes) without being greatly perturbed by a major overall OF disturbance concomitantly affecting its lateral, ventral, and dorsal OF sensors.

All in all, these results show that the ALIS autopilot made the simulated bee:

adopt a cruise speed that will automatically adjust to whichever section
(horizontal or vertical) produces the largest optic flow, and

adopt a clearance from one of the tunnel surfaces (the ground or the roof or one wall) that will be proportional to the animal's ground speed, thus automatically generating both *terrain-following* and *wall-following* behavior.

#### 437 6. CONCLUSIONS

Here we have presented an OF-based 3D autopilot called ALIS. The results of the computer simulations described above show that a simulated bee

equipped with the ALIS autopilot can navigate safely under purely visual 440 control along a straight tunnel (Fig. 6), occurs even when part of the wall or 441 the roof is devoid of texture (Fig. 7) and when the tunnel narrows or expands, 442 in either the horizontal or vertical plane (Fig. 8A, 9A, 10A), or in both planes 443 (Fig. 11A). Here we have not investigated dynamical disturbances such as 444 wind perturbations but tested ALIS's robustness to strong OF perturbations. 445 Absence of contrast on one side (as Fig. 7) and tapered tunnels (Fig. 9-11) 44F are considered by the ALIS control system (Fig. 4) as strong perturbations. 447 The autopilot manages to cope with these major perturbations, allowing the 448 simulated bee to fly safely in these tunnels. 449

These feats can all be achieved with a really minimalistic visual system 450 consisting of only eight pixels forming four EMDs (two EMDs in the hor-451 izontal plane and two in the vertical plane). The ALIS autopilot enables 452 the agent to avoid obstacles by performing maneuvers involving only trans-453 lational DOFs (along x, y, z). The key to the performances of the ALIS 454 autopilot is a pair of OF regulators designed to hold the perceived OF con-455 stant by adjusting the forward, side, and vertical thrusts. More specifically, 456 these two *OF regulators* operate as follows: 457

(i) The first *OF regulator* adjusts the bee's forward speed so as to keep *whichever sum* of the two opposite OFs (i.e., left+right or ventral+dorsal) is maximum equal to a *forward OF set-point*. The outcome is that the bee's forward speed becomes proportional to the smallest dimension (width or height, or both) of the corridor (Fig. 9E, 10E, 11E). Further simulations showed (data not shown) that this occurs regardless of the position of the bee's starting point at the tunnel entrance. The forward speed attained by the simulated bee depends also on the forward OF set-point  $\omega_{setFwd}$ .

(ii) The second *OF regulator* adjusts the bee's lateral and vertical position so as to keep the *largest OF value* (from any of the four tunnel surfaces: walls, ground, or roof) equal to the *positioning OF set-point*. The outcome is that the clearance from the nearest wall (or ground or roof) becomes proportional to the bee's forward speed as defined in (i). The clearance from the nearest tunnel surface depends on the positioning OF set-point  $\omega_{setPos}$ .

The main advantage of this visuomotor control system is that it operates 472 efficiently without any needs for explicit speed or distance information, and 473 hence without any needs for speed or range sensors. The emphasis here 474 is on behavior rather than metrics: the simulated bee behaves appropriately 475 although it is completely "unaware" of its ground speed and its distance from 476 the walls, ground, and roof. The simulated bee navigates on the basis of two 477 parameters alone: the forward OF set-point  $\omega_{setFwd}$  and the positioning OF 478 set-point  $\omega_{setPos}$  (Fig. 4). The *explicit* ALIS control scheme presented here 479 (Fig. 4) can be viewed as a working hypothesis and is very much in line with 480 the ecological approach (Gibson, 1950), according to which an animal's visual 481 system is thought to drive the locomotor system directly, without requiring 482 any "representation" of the environment (Franceschini et al., 1992; Duchon 483 and Warren, 1994). The ALIS control scheme (Fig. 4) readily accounts for the 484 behavior observed on real bees flying along a stationary corridor (Srinivasan 485 et al., 1991; Serres et al., 2008b; Baird et al., 2006) or a tapered corridor 486 (Srinivasan et al., 1996). It also accounts for the *wall-following* behavior 487 observed in straight or tapered corridors (Serres et al., 2008b). 488

489

Real bees have 4500 ommatidia, per eye and obviously more than four

OF sensors. These large number of OF sensors therefore enable them to 490 measure the OF in many directions and an elaborated autopilot could make 491 them to avoid obstacles occurring in many directions. An OF regulator is 492 little demanding in terms of its neural (or electronic) implementation since 493 it requires only a few *linear* operations (such as adding, subtracting, and 494 applying various filters) and *nonlinear* operations (such as minimum and 495 maximum detection). The minimalist control scheme described in this paper 496 could be implemented in a micro-controller running at 1kHz. In this way, 497 the "computation time" could be up to 1 msec. 498

In terms of the potential applications of these findings, biomimetic solutions of the kind described here may pave the way for the design of computationlean, lightweight visual guidance systems for autonomous aerial, underwater, and space vehicles.

503

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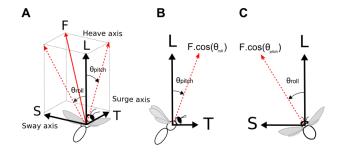


Figure 1: (A) Resolution of the mean flight-force vector  $\vec{F}$  along the surge X-axis giving the forward thrust T, along the sway Y-axis giving the side thrust S, and along the heave Z-axis giving the vertical lift L. (B) Pitching the mean flight-force vector  $\vec{F}$  by an angle  $\theta_{pitch}$  generates a forward thrust T. (C) Rolling the mean flight-force vector  $\vec{F}$  by an angle  $\theta_{roll}$  generates a side thrust S.

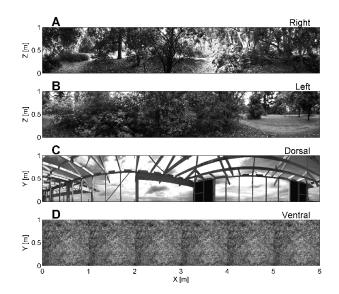


Figure 2: The grayscale natural scenes used to line the 4 internal faces of the simulated tunnel. Resolution of the images was  $1000 \times 6000$  pixels (1 pixel = 1 mm<sup>2</sup>). Images are therefore 1×6-meter in size. All four faces of the tunnel were lined with different images: right wall (A), left wall (B), roof (C), and ground (D).

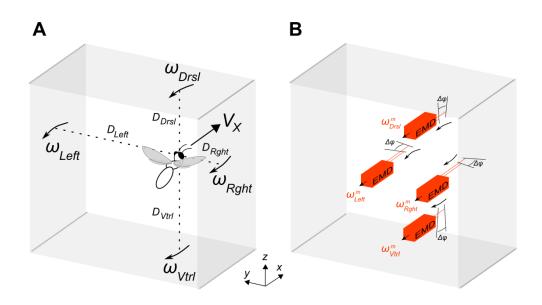


Figure 3: (A) A simulated bee flying at forward speed  $V_x$  along a tunnel generates an OF (Eq. 8) that depends on the perpendicular distance (right  $D_{Rght}$ , left  $D_{Left}$ , ventral  $D_{Vtrl}$ , dorsal  $D_{Drsl}$ ) from the tunnel surfaces. The simulated bee is equipped with four OF sensors. The sensors'axes are always oriented at fixed roll and pitch orientations, perpendicular to the walls, ground and roof, respectively, and the OF is generated laterally ( $\omega_{Left}$  and  $\omega_{Rght}$ ), ventrally ( $\omega_{Vtrl}$ ) and dorsally ( $\omega_{Drsl}$ ). (B) Each OF sensor consists of only two photoreceptors (two pixels) driving an Elementary Motion Detector (EMD). The visual axes of the two photoreceptors are separated by an interreceptor angle  $\Delta \varphi = 4 \deg$ .

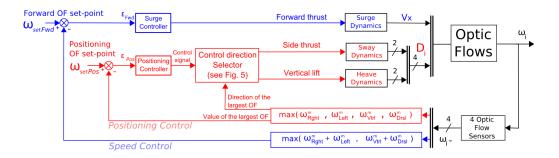


Figure 4: The ALIS autopilot is based on two interdependent visual feedback loops, each with its own OF set-point: a speed control loop (in blue) and a positioning control loop (in red). The surge controller adjusts the pitch angle  $\theta_{pitch}$  (that determines  $V_x$  via the bees' surge dynamics) on the basis of whichever sum of the two coplanar (horizontal or vertical) OFs measured is the largest. This value is compared with the forward OF set-point  $\omega_{setFwd}$ . The surge controller commands the forward speed so as to minimize the error  $\varepsilon_{Fwd}$ . The positioning controller controls the roll angle  $\theta_{roll}$  (or the stroke amplitude  $\Delta \Phi$ ), which determines the distances to the walls (or the distances to the ground and to the roof), depending on the sway (or heave) dynamics on the basis of whichever of the four measured OFs is the largest. The latter value is compared with the positioning OF set-point  $\omega_{setPos}$ . At any time, the direction of avoidance is given by a *Control direction Selector* that multiplies the control signal by a *direction factor* depending on the *direction of the maximum OF* signal (see Fig. 5). The positioning controller (Proportional-Derivative, PD) commands the sway (or heave) dynamics so as to minimize the error  $\varepsilon_{Pos}$ . The dash accross the connection lines indicates the number of variables involved.  $D_i$  is the distance to the surface involved (see Eq. 7).

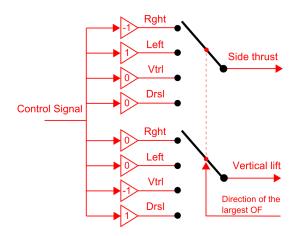


Figure 5: The Control direction Selector automatically selects the tunnel surface to be followed (wall, ground or roof) by multiplying the control signal (the output from the Positioning controller) by a direction factor that depends on the direction of the largest OF signal. Note that the sway and heave dynamics can be driven alternately, depending on which OF (side or vertical) is the largest at any given time. The input to the sway or heave dynamics that is not relevant is set to zero. In the example shown here, the direction of the maximum OF is "right". Consequently, the output for the Side thrust is the control signal multiplied by -1 and the output for the Vertical thrust is the control signal multiplied by 0.

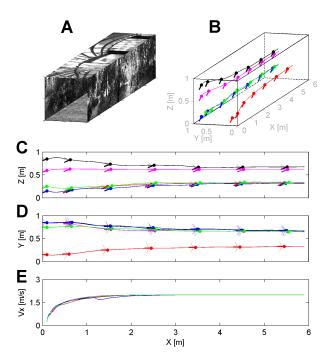


Figure 6: (A) Perspective view of the straight flight tunnel. (B) Simulated bee's 3-D trajectory starting at  $x_0 = 0.1$  m, with initial speed  $V_{xo} = 0.2$  m/sec, and various  $y_0$  and  $z_0$ , plotted every 500 msec. (C) Trajectory in the vertical plane (x, z), every 500 msec. (D) Flight track in the horizontal plane (x, y), plotted every 500 msec. (E) Forward speed  $V_x$  profile.

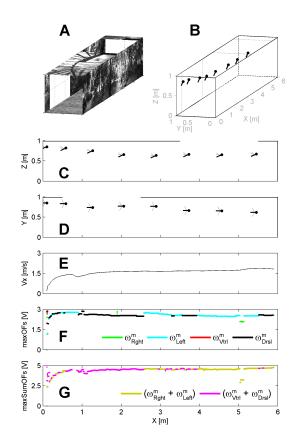


Figure 7: (A) Perspective view of the straight flight tunnel including two "no contrast" zones. (B)Simulated bee's 3-D trajectory starting at  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.85 \text{ m}$ , at the forward speed  $V_{xo} = 0.2 \text{ m/sec}$ , plotted every 500 msec. (C) Trajectory in the vertical plane (x, z), every 500 msec. (D) Trajectory in the horizontal plane (x, y), plotted every 500 msec. (E) Forward speed  $V_x$  profile. (F) Positioning feedback signal determined by the largest output from the four OF sensors (right OF sensor = green; left OF sensor = cyan; ventral OF sensor = red; dorsal OF sensor = black). (G) Forward feedback signal determined by the largest sum of the two diametrically opposed OF sensors (horizontal OF sensors = yellow; vertical OF sensors = magenta).

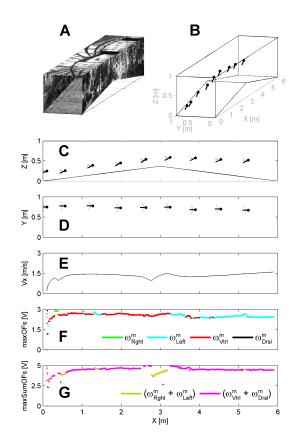


Figure 8: (A) Perspective view of the tapered tunnel. (B) Simulated bee's 3-D trajectory starting at the initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.75 \text{ m}$ ,  $z_0 = 0.25 \text{ m}$ , and at the speed  $V_{xo} = 0.2 \text{ m/sec}$ , plotted every 500 msec. (C) Trajectory in the vertical plane (x, z), every 500 msec. (D) Trajectory in the horizontal plane (x, y), plotted every 500 msec. (E) Forward speed  $V_x$  profile. (F) Positioning feedback signal determined by the largest output from the four OF sensors (right OF sensor = green; left OF sensor = cyan; ventral OF sensor = red; dorsal OF sensor = black). (G) Forward feedback signal determined by the largest sum of the two diametrically opposed OF sensors (horizontal OF sensors = yellow; vertical OF sensors = magenta).

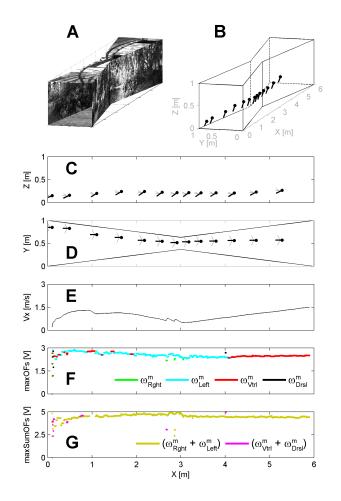


Figure 9: (A) Perspective view of the tapered tunnel. (B) Simulated bee's 3-D trajectory starting at the initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.15 \text{ m}$ , and at the speed  $V_{xo} = 0.2 \text{ m/sec}$ , plotted every 500 msec. (C) Trajectory in the vertical plane (x, z), every 500 msec. (D) Trajectory in the horizontal plane (x, y), plotted every 500 msec. (E) Forward speed  $V_x$  profile. (F) Positioning feedback signal determined by the largest output from the four OF sensors (right OF sensor = green; left OF sensor = cyan; ventral OF sensor = red; dorsal OF sensor = black). (G) Forward feedback signal determined by the largest sum of the two diametrically opposed OF sensors (horizontal OF sensors = yellow; vertical OF sensors = magenta).

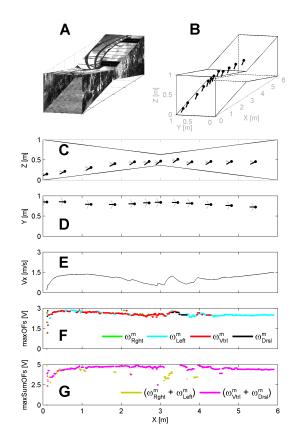


Figure 10: (A) Perspective view of the tapered tunnel. (B) Simulated bee's 3-D trajectory starting at the initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.15 \text{ m}$ , and at the speed  $V_{xo} = 0.2 \text{ m/sec}$ , plotted every 500 msec. (C) Trajectory in the vertical plane (x, z), every 500 msec. (D) Trajectory in the horizontal plane (x, y), plotted every 500 msec. (E) Forward speed  $V_x$  profile. (F) Positioning feedback signal determined by the largest output from the four OF sensors (right OF sensor = green; left OF sensor = cyan; ventral OF sensor = red; dorsal OF sensor = black). (G) Forward feedback signal determined by the largest sum of the two diametrically opposed OF sensors (horizontal OF sensors = yellow; vertical OF sensors = magenta).

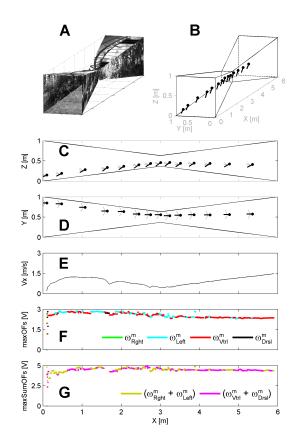


Figure 11: (A) Perspective view of the tapered tunnel. (B) Simulated bee's 3-D trajectory starting at initial coordinates  $x_0 = 0.1 \text{ m}$ ,  $y_0 = 0.85 \text{ m}$ ,  $z_0 = 0.15 \text{ m}$ , and at the speed  $V_{xo} = 0.2 \text{ m/sec}$ , plotted every 500 msec. (C) Trajectory in the vertical plane (x, z), every 500 msec. (D) Trajectory in the horizontal plane (x, y), plotted every 500 msec. (E) Forward speed  $V_x$  profile. (F) Positioning feedback signal determined by the largest output from the four OF sensors (right OF sensor = green; left OF sensor = cyan; ventral OF sensor = red; dorsal OF sensor = black). (G) Forward feedback signal determined by the largest sum of the two diametrically opposed OF sensors (horizontal OF sensors = yellow; vertical OF sensors = magenta).