

## Advances in the nonlinear dynamics of gaseous detonations

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# Advances in the nonlinear dynamics of gaseous detonations

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Autumn Sciences Days at University of Almeria in honor of Manuel Garcia VELARDE September 24-27 2019 Understanding complex phenomena?

Examples: combustion phenomena

Direct numerical simulations?

A physicist approach: reduce the complexity ending with simplified equations to be solved analytically and compare with experiments

Hopefully gaseous detonations are not easy to initiate

What minimum energy should be deposited by an external source to initiate a gaseous detonation in an open space?

Safety of nuclear power plant Explosions....supernovae....

### **Detonations = combustion supersonic waves**

inert shock followed by an exothermal reaction zone

in gas at ordinary conditions: 1800–3400 m/s, 15–30 bar, 2500–3700 K



Deflagration = combustion subsonic waves reaction-diffusion waves

Old scientific topic (end of 19th - extensively studied since the mid 20th)

Comprehensible explanation of the multidimensional geometry and complex dynamics of the wave fronts has been elusive. Understanding is recent (nonlinear analyses)

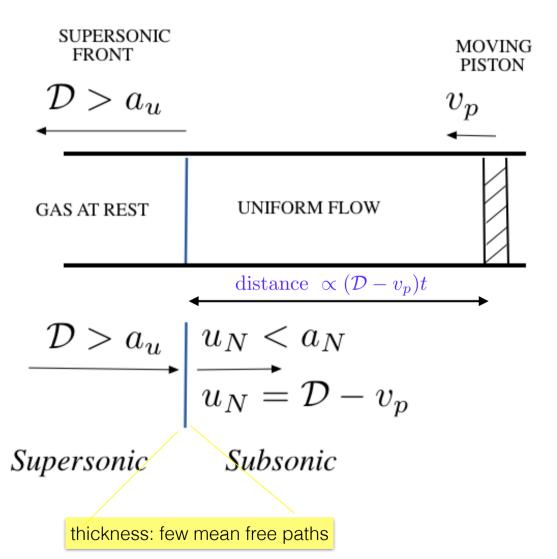
Reactive Euler equations

#### Back to school

Background in compressible fluids

Planar shock waves and detonations 1860-1940

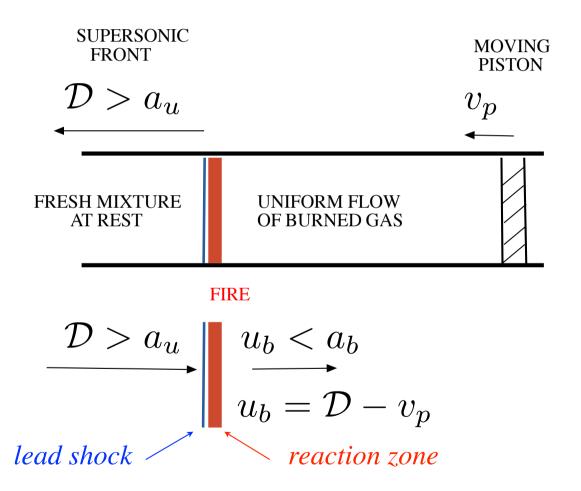
#### PLANAR SHOCK WAVE INERT GAS



Poisson 1808, Stokes 1848, Riemann 1860, Rankine 1869, Hugoniot 1889, Rayleigh 1910

### OVERDRIVEN DETONATION REACTING GAS

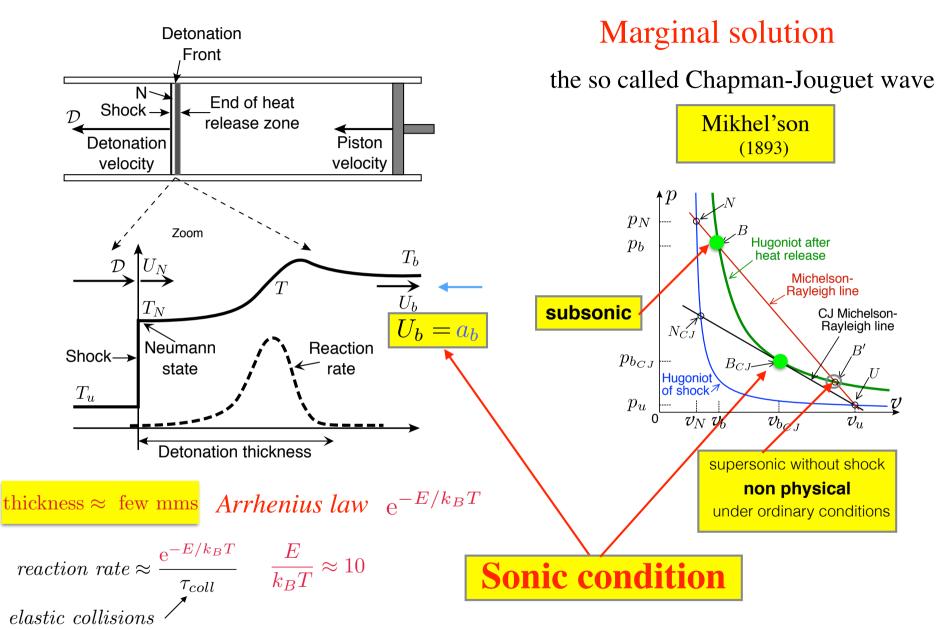
#### PISTON SUPORTED SUPERSONIC WAVE



Abel 1870, Berthelot et Vielle 1881, Mallard et Le Chatelier 1881, Mikhel'son 1893, Chapman 1899, Jouguet 1904, Vielle 1900, Zel'dovich 1940, von Neumann 1942, Döring 1943,

#### Planar detonation

#### Overdriven regime / Self sustained wave



# Planar detonation (inner structure in steady state)

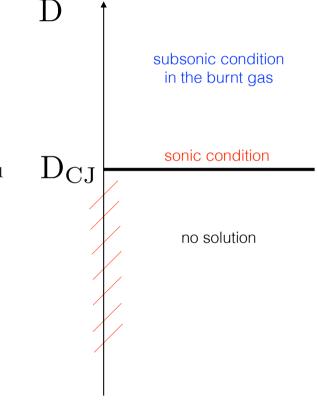
propagation velocity

supersonic overdriven wave

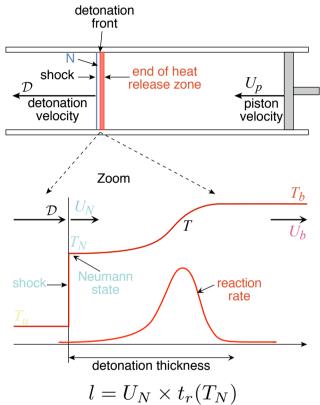
$$D > a_u$$

self sustained supersonic wave

$$\frac{q_m}{c_p T_u} \gg 1 \quad \Rightarrow \quad \frac{\mathrm{D_{CJ}}}{a_u} \approx 2\sqrt{\frac{\gamma + 1}{2} \frac{q_m}{c_p T_u}} > 1 \qquad \mathbf{D_{CJ}}$$



#### Negligible heat conduction and viscosity



 $U_N \approx a$  flow velocity/shock sound speed

reaction time 
$$t_r \approx t_{coll} \times e^{\mathcal{E}/k_b T} \gg t_{coll}$$
  $\mathcal{E}/k_b T \approx 10$ 

Reynolds nb 
$$\frac{U_N l}{\nu} \approx \frac{a^2 \times t_r}{\nu} \approx \frac{t_r}{t_{coll}} \approx e^{\mathcal{E}/k_b T} \gg 1$$

$$\nu \approx a^2 \times t_{coll}$$

#### Reactive Euler Equations

#### Back to our problem!

What minimum energy should be released by an external source to initiate a gaseous detonation in open space (3D)?

Zeldovich criterion (1956)

critical energy  $\approx \frac{\text{chemical energy}}{\text{unit volume}} \times (\text{detonation thickness})^3$ 

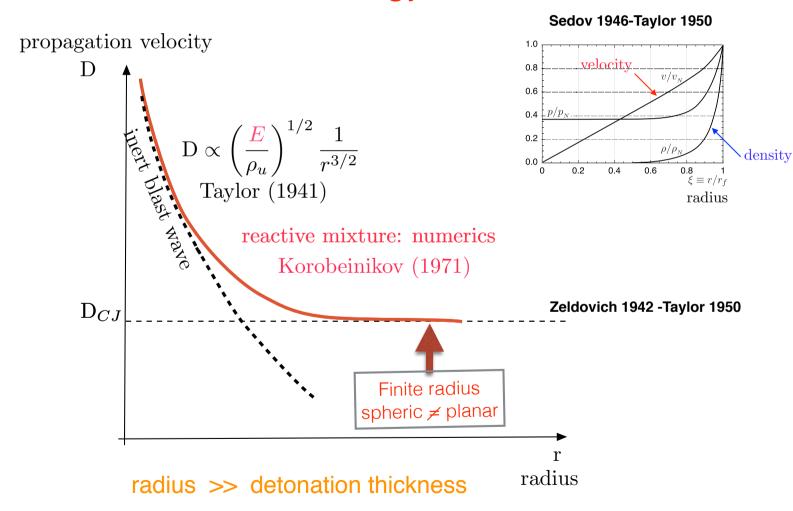
Wrong! Under estimated by a factor  $10^6-10^8$ 

Experiments (1975)-(1980)

#### Numerics in spherical geometry

Korobeinikov (1971)
Detonation = discontinuity

(zero detonation thickness)
No critical energy!



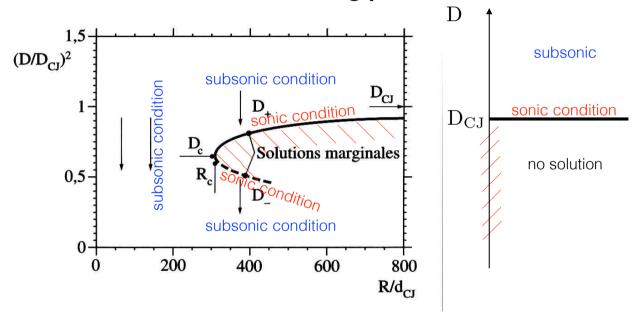
Conclusion: the critical energy is due to small modifications of the inner structure!

#### Curvature effect (steady state approximation)

L. He & P.C (1994)

#### Marginal CJ condition in the parameter space «radius-velocity »

#### **Turning point**

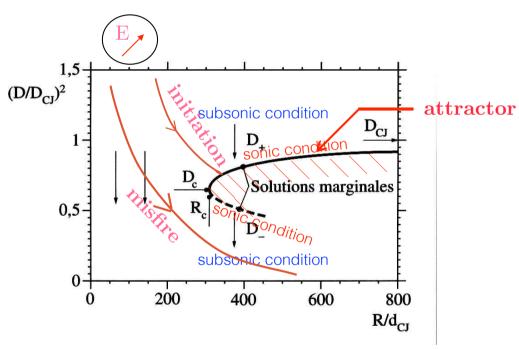


$$\frac{\text{critical radius}}{\text{detonation thickness}} \propto \frac{8}{\gamma - 1} e^{\frac{E/k_B T_N}{N}} \approx 10^2$$

Arrhenius factor

#### Curvature effect (steady state approximation)

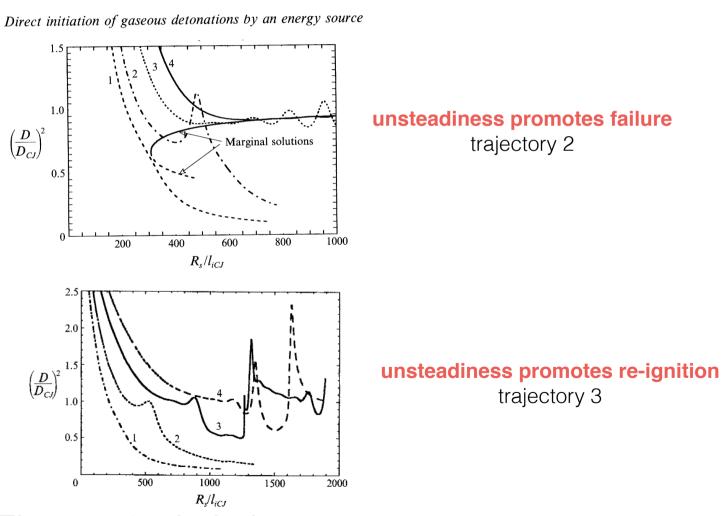




$$\frac{\text{critical radius}}{\text{detonation thickness}} \approx 10^2 \implies \frac{\text{critical energy}}{\text{Zeldovich value}} \approx 10^6$$

# Role of unsteadiness of the inner structure? Dynamics close to the critical radius?

#### Experiments and DNS show a sensitivity to details



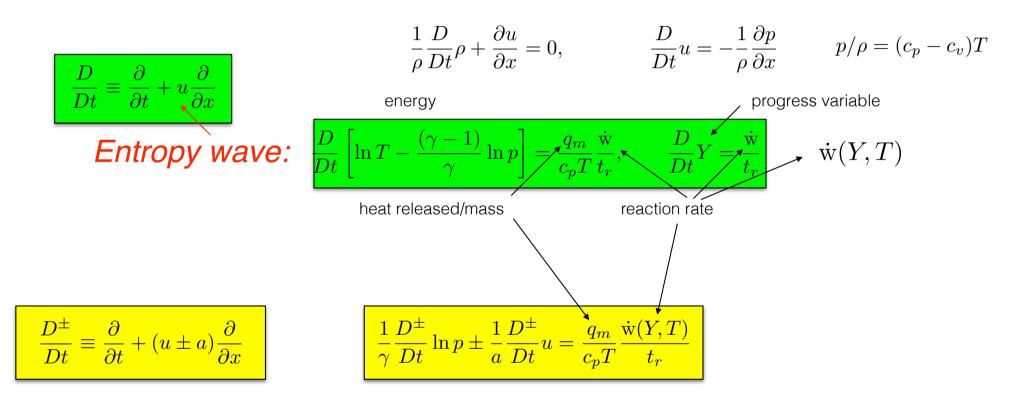
The analysis is in progress

### 1D dynamics in planar geometry

PC & F.A. Williams (2002-2009)

#### 1-D dynamics of the inner structure of planar detonations

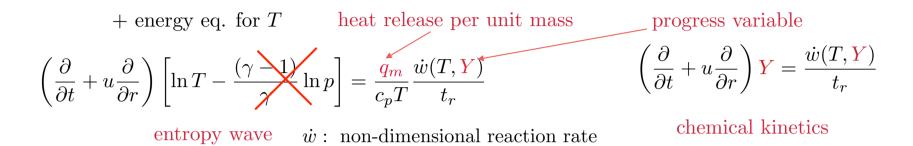
#### Constitutive equations



Hyperbolic equations: Eqs. of the characteristics

Nonlinear acoustic waves generated by an exothermal reaction

#### 1-D compressible, inviscid and reactive gas mixture



#### Newtonian approximation

acoustic waves

heat release rate

$$\frac{1}{\gamma p} \left[ \frac{\partial}{\partial t} + (u \pm a) \frac{\partial}{\partial x} \right] p \pm \frac{1}{a} \left[ \frac{\partial}{\partial t} + (u \pm a) \frac{\partial}{\partial x} \right] u = \frac{\mathbf{q}_m}{c_p T} \frac{\dot{w}}{t_r}$$
sound speed  $a \equiv \sqrt{(\gamma - 1)c_p T}$ 

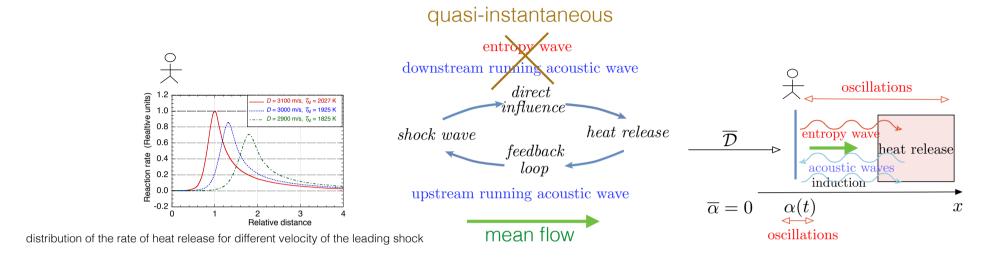
small heat release:  $a \approx \text{cst.}$ 

3 nonlinear modes: Entropy wave + 2 acoustic waves

4 nonlinear equations & 4 unknowns: p, T, u, Y

too complicated system for a general analytical solution

### 1-D dynamics of the inner structure of planar detonations Set of feedback loops



Threshold of the planar instability of the CJ regime:

Small heat release  $\Rightarrow$  Transonic flow

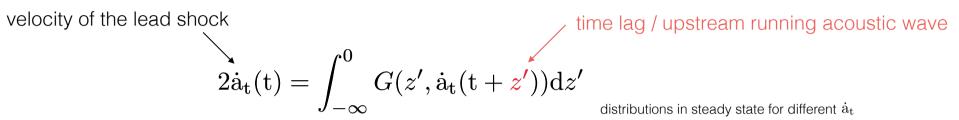
3rd simplification:

Two-time scales: The upstream running acoustic wave controls the loops

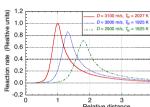
The two other modes involves much shorter time lags

#### Integral equation for the propagation velocity $\dot{a}_t(t)$

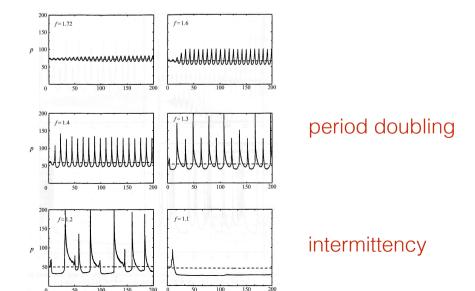
Unperturbed flow velocity of burnt gas (intrinsic dynamics):



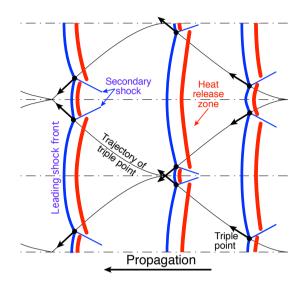
 $G(z, \dot{\mathbf{a}}_{\mathrm{t}})$ : distribution of the rate of heat release for  $\dot{\mathbf{a}}_{\mathrm{t}}$  (constant)



#### Typical solution for the dynamics when increasing the activation energy



# Theoretical analyses of cellular structures 1996-2017



1-D oscillatory instability + transverse propagation and Mach stem formation

one-dimensional instability 1996-2002

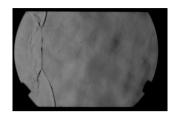


#### B.Maxwell, R.Bhattacharjee, S. Lau-Chapelaine, S.Falle, G. Sharpe and M. Radulescu

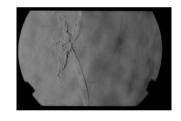
Journal of Fluid Mechanics 2017

 $CH_4 + 2O_2$   $p = 3.5kP_a$  2D geometry experiment

High activation energy: Irregular structure and transient phenomena



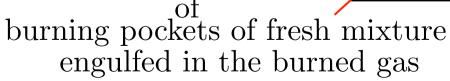


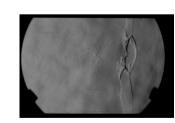


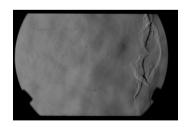


Schlieren images







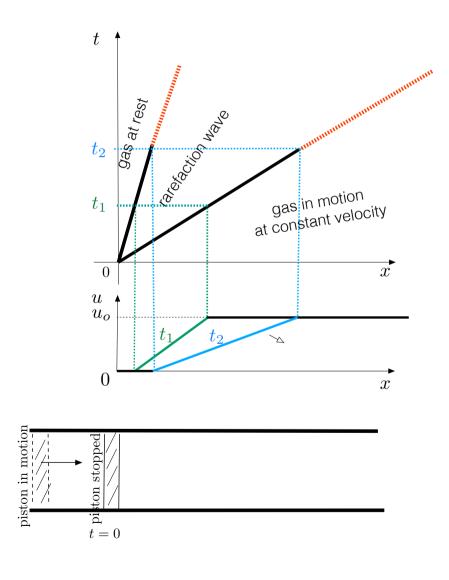


Successive frames  $11\mu s$  apart

The role of unsteadiness in the decay to the CJ regime when the piston is brought to instantaneous halt

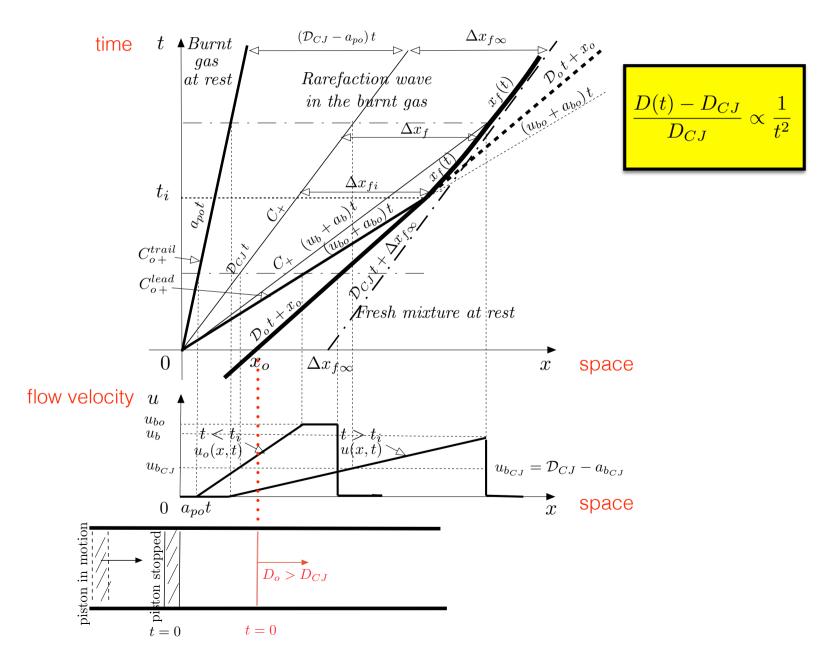
PC & B. Denet (2018)

# 1-D (planar) centered rarefaction wave when the piston is suddenly arrested



# Selection mechanism of the self sustained propagation (CJ wave) by the rarefaction wave in the burnt gas (planar geometry and inner structure of the detonation in steady state)

Levin & Chernyi (1967), P.C.& B.Denet (2017)



#### Integral equation for the propagation velocity $\dot{a}_t(t)$

Unperturbed flow velocity of burnt gas

$$2\dot{\mathbf{a}}_{\mathbf{t}}(\mathbf{t}) = \int_{-\infty}^{0} G(z', \dot{\mathbf{a}}_{\mathbf{t}}(\mathbf{t} + z')) dz'$$

#### Relaxation to the CJ regime when the piston is suddenly stopped at t=0:

PC & B. Denet *JFM* (2018)

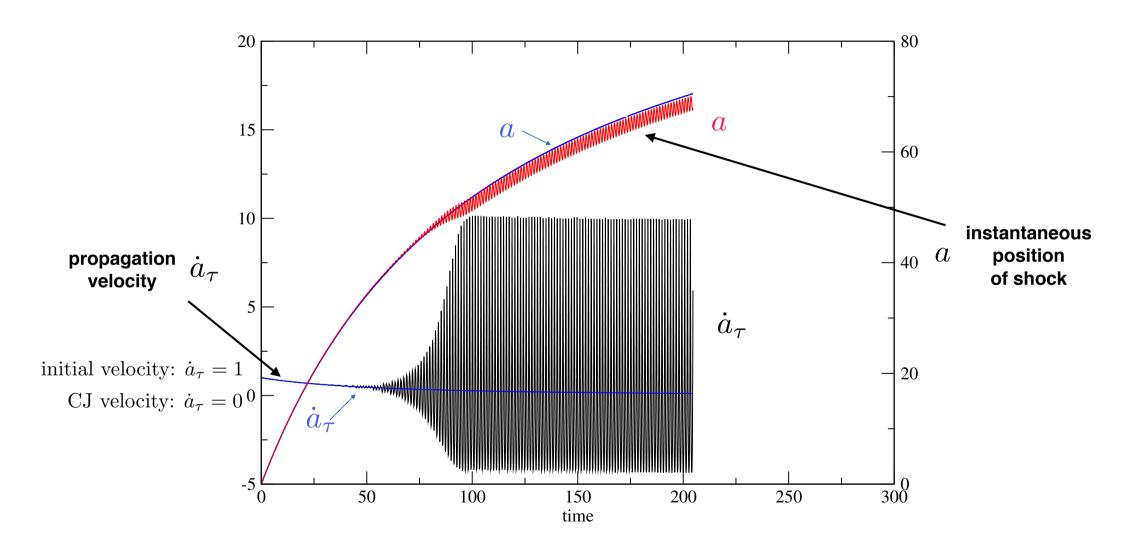
nonlinear response function: intrinsic dynamics

forcing term: rarefaction wave in the burnt gas

$$t \ge 0: \quad 2\dot{a}_{t}(t) = \int_{-\infty}^{0} G(z', \dot{a}_{t}(t+z'))dz' + (1+t/\tau_{i})^{-2}.$$

$$t \le 0: \quad \dot{a}_t(t) = 1$$
 
$$\int_{-\infty}^0 G(z', 1) dz' = 1$$

piston-supported detonation (overdriven regime)

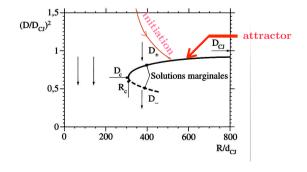


distributions in steady state for different  $\dot{a}_t$ D = 3100 m/s, T<sub>N</sub> = 2027 K .... D = 3000 m/s, T<sub>N</sub> = 1925 K ... D = 2900 m/s, T<sub>N</sub> = 1825 K 8.0 (Bealtive 용 0.4 4 o.o 2 3 Relative distance lead shock end of reaction zone directinfluencerarefaction wave driven decay heat release shockwavefeedbackloopupstream running acoustic wave mean flow

the upstream running mode controls the response

#### Transonic flow: divergence of the delay when approaching the CJ self-sustained regime

Solvability condition: selection of the family of the overdriven regimes approaching the CJ regime



This analysis presents a simple tool that can be extended for describing the chaotic dynamics around the critical radius controlling the initiation of detonations in free space.

Results are expected soon!

Thank you for your attention