Hydration and Ionic Conductivity of Model Cation and Anion-Conducting Ionomers in Buffer Solutions (Phosphate, Acetate, Citrate)

L. Pasquini\textsuperscript{1,2}, O. Wacrenier\textsuperscript{1}, M. L. Di Vona\textsuperscript{2,3}, P. Knauth\textsuperscript{1,2}\
\textsuperscript{1} Aix Marseille Univ, CNRS, MADIREL (UMR 7246), Campus Etoile-St Jérôme, 13013 Marseille, France
\textsuperscript{2} International Associated Laboratory (L.I.A.) “Ionomer Materials for Energy”, Aix Marseille Univ, CNRS, Univ. Rome Tor Vergata
\textsuperscript{3} Univ. Rome Tor Vergata, Dip. Ing. Industriale, Via del Politecnico, 00133 Roma, Italy

Abstract

We studied the gravimetric and volumetric water uptake and ionic conductivity of two model ionomers, cation-conducting sulfonated poly(ether ether ketone) (SPEEK) and anion-conducting polysulfone-trimethylammonium chloride (PSU-TMA), after immersion in phosphate, acetate and citrate buffer solutions. The equilibrium swelling of SPEEK and PSU-TMA ionomer networks was determined as a function of pH and buffer composition. The hydration data can be interpreted using the osmotic swelling pressure dependence on the ion exchange capacity of the ionomers and the concentration of the electrolyte solutions. In the case of SPEEK, anisotropic swelling is observed in diluted buffer solutions, where the swelling pressure is higher. A large water uptake is observed for citrate ions, due to the large hydration of this bulky anion. The ionic conductivity is related to the conducting ions and, in the case of SPEEK, to sorbed excess electrolyte. The highest ionic conductivity is observed after immersion in phosphate buffers. Ionic cross-linking is for the first time observed in the case of an anion-conducting ionomer in presence of divalent citrate ions, which limits the volumetric swelling and decreases the ionic conductivity of PSU-TMA.

* Corresponding author: Philippe.Knauth@univ-amu.fr
Introduction

Polyelectrolytes are macromolecules with ionic groups grafted on the main or side chains\(^1,2\). They are called ionomers, when a nanophase separation between hydrophobic and hydrophilic domains is observed with the formation of nanosized ion conduction channels inside the solid polymer matrix\(^3\). A well-defined nanophase separation promotes better-connected and less tortuous ion conduction channels and enhances the ionic conductivity\(^4,5\), but also the ionic permeability\(^6-8\). The selectivity of the ion transport process can therefore be improved by a careful balance between hydrophilic and hydrophobic domains.

Ionomers are often used in membrane form for applications, typically prepared by casting from an appropriate solvent\(^9,10\). The hydrolytic stability\(^11,12\) is related to the amount of ion exchange groups (a high ion exchange capacity increases the hydrophilicity and generally the swelling and solubility in polar and protic solvents with high dielectric constant) and to the hydrophobicity of the ionomer backbone (which might increase the solubility in non-polar solvents).

One can prepare cation-conducting ionomers (including proton exchange membranes) by grafting various cation exchange groups, in the majority of cases sulfonic acid\(^13-16\), and anion-conducting ionomers (including hydroxide exchange membranes) by anchoring typically quaternary ammonium groups\(^17-20\). The ionic conductivity is related to the ion exchange capacity of the polymers, but also to the solvation of the conducting ions and other factors such as the connectivity and tortuosity of the ion conduction channels in the ionomer\(^21\).

Ion exchange polymers have many important applications, including separation membranes for electrochemical energy technologies\(^22,23\), such as polymer electrolyte membrane fuel cells\(^14,19,24\) and redox flow batteries\(^25,26\), and other environmental technologies, such as water purification (by ultrafiltration\(^27\) or electrodialysis\(^20,28\)). They have also important applications in the biological field, where ionomers can be practical models for protein membranes or other biochemical systems, in which ion transport plays a role.

In particular, biofuel cells\(^29\) and enzymatic fuel cells\(^30\) have recently been much improved and really promising performance jumps have been reported\(^31\). Biofuel cells work still mostly with liquid electrolytes, but a miniaturisation using ion exchange membrane separators is worthwhile to open the field of power supplies for miniaturized sensors and actuators and medical systems.

The used separator membranes should be biocompatible and should not alter the enzymatic activity. Nafion-type membranes are potentially harmful to the enzymatic activity due to the presence of fluorinated degradation species\(^32\). Membranes obtained with functionalized non-fluorinated organic polymers are a good alternative, thanks to their ion selectivity, high ionic
conductivity, good stability, long life and low production cost, while keeping a low overall size to tend towards the miniaturization of the device.

Enzymatic fuel cells\textsuperscript{30} work typically in pH-buffered media in order to keep a good enzymatic activity without enzyme denaturation; phosphate, citrate and acetate buffers are the most commonly applied. However, the hydration stability and conductivity of ion exchange membranes in these solutions has never been studied. The hydration behaviour of ion exchange membranes is governed by the interplay between the osmotic pressure of inner and outer electrolyte solutions and the mechanical properties of the membrane, which are interdependent\textsuperscript{11,33-36}. We have previously reported a simple phenomenological model, relating the hydration and the mechanical properties of ionomers\textsuperscript{35}. The ionic conductivity is also very sensitive to the hydration, because the ion mobility is a function of the amount of water\textsuperscript{21,37}. The effects of pH and ionic strength on the swelling of polyelectrolyte\textsuperscript{38,39} and copolymer gels\textsuperscript{33} were studied before.

In the following, we report for the first time the hydration and ionic conductivity after immersion in phosphate, citrate and acetate buffers of two model ionomers: cation-conducting sulfonated poly(ether ether ketone) (SPEEK)\textsuperscript{40-43} and anion-conducting PSU-trimethylammonium chloride (PSU-TMA)\textsuperscript{44-48} (Figure 1). These ionomers are among the most investigated and can be applied in enzymatic and biofuel cells. Sufficient literature exists for both ionomers\textsuperscript{20,24,43}, reporting many relevant properties and data facilitating the discussion of the measured properties.

We studied 0.05 M and 0.1 M solutions of phosphate, citrate and acetate buffers, which are the most employed in enzymatic fuel cells. The hydration and ionic conductivity of SPEEK and PSU-TMA ionomer networks were determined as a function of pH and buffer composition.
Figure 1. Repeat units of SPEEK and PSU-TMA.

Experimental

SPEEK was prepared by reaction of poly(ether ether ketone) (PEEK, Victrex) with concentrated sulphuric acid. The degree of sulfonation of SPEEK, determined by NMR spectroscopy and acid-base titration, was DS = 0.96, corresponding to an ion exchange capacity IEC = 2.62 meq g⁻¹. The membranes were cast from DMSO solutions using a doctor-blade equipment. 1 g SPEEK was dissolved in 30 mL DMSO. After evaporation to around one third of the original volume, the solution was spread on a glass plate using a doctor-blade type equipment and then put in the oven at 120 °C for 24 h. The dry density of the ionomer in acid form is 1.3 g cm⁻³.

PSU-TMA was prepared by chloromethylation of PSU using the procedure reported in reference. The chloromethylated product was then aminated by reaction with trimethylamine. The degree of amination determined by NMR spectroscopy and acid-base titration was DAM = 0.66, corresponding to an ion exchange capacity IEC = 1.34 meq g⁻¹. The membranes were cast from DMSO solutions; typically, 10 mL of a 0.05 M solution of PSU-TMA was evaporated to 5 mL, cast on a Petri dish then heated to dryness at 100 °C for 24 h.

The dry density of the ionomer in Cl form was measured after drying the membranes over P₂O₅ for 24 h. The membranes were rapidly weighed in a closed vessel and the geometrical dimensions determined. The average value of 9 measurements was (1.15 ± 0.05) g cm⁻³.

The hydration and ion conductivity was investigated in 3 different buffers: phosphate (H₂PO₄⁻ /HPO₄²⁻), citrate (monocitrate/dicitrate) and acetate (CH₃CO₂H / CH₃CO₂⁻). The concentration of the buffer solutions was 0.1 or 0.05 M. The desired pH values were obtained by mixing the buffer components and the pH was determined with a calibrated pH meter (Mettler Toledo).

The membranes were immersed in 100 mL buffer solution for 24 h at room temperature, washed rapidly in pure water to remove any excess of buffer solutions and wiped carefully with absorbing paper before the measurements.

The gravimetric water uptake $WU$ was measured in duplicate at 25 °C and calculated according to the equation:

$$WU = 100 \cdot \frac{(m_{\text{wet}} - m_{\text{dry}})}{m_{\text{dry}}}$$  \hspace{1cm} (1)

The mass of wet samples ($m_{\text{wet}}$) was determined after 24 h immersion in buffer solutions. The mass of dry samples ($m_{\text{dry}}$) was measured in a closed vessel after drying over P₂O₅ for 24 h.
Furthermore, the variations of sample area and thickness were determined after immersion in buffers by measuring the sample dimensions with a micrometer (Mitutoyo 293-230). The dry samples had an area of around 4 cm$^2$ and a thickness between 20 and 40 µm. The percentage variations of area ($\Delta A$) and thickness ($\Delta d$) were calculated from the relations:

$$\Delta A = 100 \cdot \frac{A_{\text{wet}} - A_{\text{dry}}}{A_{\text{dry}}} \quad \Delta d = 100 \cdot \frac{d_{\text{wet}} - d_{\text{dry}}}{d_{\text{dry}}}$$

(2)

The density $D$ of the ionomer after swelling can be obtained from the following equation:

$$D = \frac{m_{\text{wet}}}{A_{\text{wet}} \cdot d_{\text{wet}}}$$

(3)

The through-plane ionic conductivity was measured by impedance spectrometry between 1 Hz and 6 MHz using an impedance spectrometer Biologic VSP300. The amplitude of the oscillating voltage was 20 mV. The samples were studied at 25 °C in fully humidified conditions inside a Swagelok cell with two stainless steel electrodes. The sample resistance $R_s$ was obtained from typical impedance spectra (Figure 2) using the intercept with the real axis. The ionic conductivity $\sigma$ was calculated using the equation:

$$\sigma = \frac{d_{\text{wet}}}{R_s \cdot A_{\text{wet}}}$$

(4)

**Results**

The gravimetric and volumetric water uptake, the change of membrane dimensions (area and thickness), the density and the ionic conductivity of SPEEK and PSU-TMA membranes after immersion in phosphate, citrate or acetate buffers at various pH values at 25 °C are reported in Tables 1 and 2, respectively. Typical impedance spectra for SPEEK and PSU-TMA membranes are shown in Figure 2. The ionic conductivities $\sigma$, calculated according to equation 4, are reported in Tables 1 and 2.
Figure 2. Typical impedance spectra observed for SPEEK (open dots, $R_s = 1.6 \, \Omega$, thickness $d = 25 \, \mu m$) and PSU-TMA (black dots, $R_s = 24.8 \, \Omega$, $d = 40 \, \mu m$) membranes at $25 \, ^\circ C$ after immersion in phosphate buffer at $pH = 5.8$. The lines represent non-linear least-square plots using an equivalent circuit consisting of a series arrangement of $R_s$ and a parallel circuit resistance/constant phase element.$^{32,33}$
Table 1. Gravimetric (WU) and volumetric (ΔV) water uptake, change of membrane area ΔA and thickness Δd, density D and ionic conductivity σ of SPEEK in various buffers and pH at 25 °C. The molar counter-ion concentration c'(Na⁺) in each buffer solution was calculated from the acid and base concentrations determined using equation (8). Sample dissolution is indicated by “/”.

<table>
<thead>
<tr>
<th></th>
<th>Phosphate</th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>5.8</td>
<td>7</td>
<td>8</td>
<td>4</td>
<td>5</td>
<td>5.9</td>
<td>3.6</td>
<td>4.4</td>
<td>5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>WU / %</td>
<td>26.7</td>
<td>32.3</td>
<td>27.2</td>
<td>76.0</td>
<td>65.7</td>
<td>63.3</td>
<td>/</td>
<td>203.0</td>
<td>66.7</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ΔV / %</td>
<td>33.3</td>
<td>41.8</td>
<td>37.8</td>
<td>139.6</td>
<td>105.0</td>
<td>105.9</td>
<td>/</td>
<td>293.6</td>
<td>77.8</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ΔA / %</td>
<td>15.0</td>
<td>21.3</td>
<td>27.0</td>
<td>80.1</td>
<td>60.3</td>
<td>62.5</td>
<td>/</td>
<td>136.4</td>
<td>51.2</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Δd / %</td>
<td>15.3</td>
<td>16.9</td>
<td>11.9</td>
<td>34.4</td>
<td>26.7</td>
<td>27.9</td>
<td>/</td>
<td>66.5</td>
<td>17.9</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>D / g cm⁻³</td>
<td>1.09</td>
<td>1.22</td>
<td>1.22</td>
<td>0.92</td>
<td>0.90</td>
<td>0.92</td>
<td>/</td>
<td>1.05</td>
<td>1.06</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>σ / mS cm⁻¹</td>
<td>5.6</td>
<td>6.5</td>
<td>8.4</td>
<td>1.6</td>
<td>4.1</td>
<td>3.8</td>
<td>/</td>
<td>/</td>
<td>4.5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>c'(Na⁺)/molL⁻¹</td>
<td>0.104</td>
<td>0.139</td>
<td>0.186</td>
<td>0.115</td>
<td>0.163</td>
<td>0.193</td>
<td>0.006</td>
<td>0.029</td>
<td>0.063</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>0.05 M</th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>5.8</td>
<td>7</td>
<td>8</td>
<td>4</td>
<td>5</td>
<td>5.9</td>
<td>3.6</td>
<td>4.4</td>
<td>5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>WU / %</td>
<td>66.0</td>
<td>63.0</td>
<td>65.3</td>
<td>77.7</td>
<td>72.4</td>
<td>66.3</td>
<td>/</td>
<td>/</td>
<td>/</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ΔV / %</td>
<td>76.0</td>
<td>70.7</td>
<td>93.0</td>
<td>90.0</td>
<td>68.7</td>
<td>66.1</td>
<td>/</td>
<td>/</td>
<td>/</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ΔA / %</td>
<td>56.1</td>
<td>51.8</td>
<td>65.3</td>
<td>62.9</td>
<td>53.8</td>
<td>51.5</td>
<td>/</td>
<td>/</td>
<td>/</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Δd / %</td>
<td>12.6</td>
<td>12.4</td>
<td>16.8</td>
<td>16.7</td>
<td>10.5</td>
<td>9.6</td>
<td>/</td>
<td>/</td>
<td>/</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>D / g cm⁻³</td>
<td>1.26</td>
<td>1.16</td>
<td>1.09</td>
<td>1.18</td>
<td>1.12</td>
<td>1.18</td>
<td>/</td>
<td>/</td>
<td>/</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>σ / mS cm⁻¹</td>
<td>6.6</td>
<td>6.6</td>
<td>8.3</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>/</td>
<td>/</td>
<td>/</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>c'(Na⁺)/molL⁻¹</td>
<td>0.052</td>
<td>0.069</td>
<td>0.093</td>
<td>0.057</td>
<td>0.082</td>
<td>0.096</td>
<td>0.003</td>
<td>0.014</td>
<td>0.031</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 2. Gravimetric (WU) and volumetric (ΔV) water uptake, change of membrane area ΔA and thickness Δd, density D and ionic conductivity σ of PSU-TMA in various buffers and pH at 25 °C. The molar concentrations of the monovalent c'(A⁻) and divalent c'(A²⁻) counter-anions in each buffer solution are calculated using equation (8).

<table>
<thead>
<tr>
<th>pH</th>
<th>0.1 M</th>
<th>Phosphate</th>
<th>Citrate</th>
<th>Acetate</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>WU / %</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.8</td>
<td>11.5</td>
<td>14.0</td>
<td>17.0</td>
<td>24.1</td>
</tr>
<tr>
<td>7</td>
<td>22.7</td>
<td>10.0</td>
<td>19.8</td>
<td>10.4</td>
</tr>
<tr>
<td>8</td>
<td>10.7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>28.1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>22.1</td>
<td>8.8</td>
<td>24.8</td>
<td>31.9</td>
</tr>
<tr>
<td>5.9</td>
<td>22.5</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3.6</td>
<td>17.0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4.4</td>
<td>10.0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>10.7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ΔV / %</td>
<td>17.1</td>
<td>25.1</td>
<td>28.1</td>
<td>16.5</td>
</tr>
<tr>
<td>ΔA / %</td>
<td>11.6</td>
<td>11.5</td>
<td>12.7</td>
<td>6.5</td>
</tr>
<tr>
<td>Δd / %</td>
<td>4.9</td>
<td>12.1</td>
<td>13.6</td>
<td>9.4</td>
</tr>
<tr>
<td>D / g cm⁻³</td>
<td>0.97</td>
<td>1.02</td>
<td>1.03</td>
<td>1.14</td>
</tr>
<tr>
<td>σ / mS cm⁻¹</td>
<td>0.6</td>
<td>1.0</td>
<td>1.3</td>
<td>&lt;0.01</td>
</tr>
<tr>
<td>c'(A⁻)/ mol L⁻¹</td>
<td>0.096</td>
<td>0.061</td>
<td>0.014</td>
<td>0.085</td>
</tr>
<tr>
<td>c'(A²⁻)/ mol L⁻¹</td>
<td>0.004</td>
<td>0.039</td>
<td>0.086</td>
<td>0.015</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>0.05 M</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>WU / %</td>
<td>6.1</td>
<td>9.1</td>
<td>23.3</td>
</tr>
<tr>
<td>ΔV / %</td>
<td>30.9</td>
<td>19.3</td>
<td>23.2</td>
</tr>
<tr>
<td>ΔA / %</td>
<td>24.4</td>
<td>13.8</td>
<td>13.8</td>
</tr>
<tr>
<td>Δd / %</td>
<td>5.3</td>
<td>4.8</td>
<td>8.2</td>
</tr>
<tr>
<td>D / g cm⁻³</td>
<td>0.93</td>
<td>1.08</td>
<td>1.13</td>
</tr>
<tr>
<td>σ / mS cm⁻¹</td>
<td>0.20</td>
<td>0.29</td>
<td>0.32</td>
</tr>
<tr>
<td>c'(A⁻)/ mol L⁻¹</td>
<td>0.048</td>
<td>0.031</td>
<td>0.007</td>
</tr>
<tr>
<td>c'(A²⁻)/ mol L⁻¹</td>
<td>0.002</td>
<td>0.019</td>
<td>0.043</td>
</tr>
</tbody>
</table>

Table 2. Gravimetric (WU) and volumetric (ΔV) water uptake, change of membrane area ΔA and thickness Δd, density D and ionic conductivity σ of PSU-TMA in various buffers and pH at 25 °C. The molar concentrations of the monovalent c'(A⁻) and divalent c'(A²⁻) counter-anions in each buffer solution are calculated using equation (8).
Discussion

Theory: buffer equilibria, counter-ion concentration and osmotic pressure

For the $\text{H}_2\text{PO}_4^-/\text{HPO}_4^{2-}$ buffer, $\text{pK}_a = 7.20$ at $25 \, ^\circ\text{C}$, the equilibrium can be written:

$$\text{H}_2\text{PO}_4^- + \text{H}_2\text{O} \rightleftharpoons \text{HPO}_4^{2-} + \text{H}_3\text{O}^+ \tag{5}$$

Acetic acid is a weak acid with a $\text{pK}_a = 4.76$ at $25 \, ^\circ\text{C}$; the acid dissociation is small and the concentration of hydronium ions can be neglected for the calculation of the osmotic pressure.

$$\text{CH}_3\text{CO}_2\text{H} + \text{H}_2\text{O} \rightleftharpoons \text{CH}_3\text{CO}_2^- + \text{H}_3\text{O}^+ \tag{6}$$

Citric acid is a tribasic acid; the buffer prepared corresponds to the second dissociation step, coincidently also with $\text{pK}_a = 4.76$ at $25^\circ\text{C}$.

$$\text{O}_2\text{C(HO)}\text{C(CH}_2\text{CO}_2\text{H})_2 + \text{H}_2\text{O} \rightleftharpoons \text{O}_2\text{C(HO)}\text{C(CH}_2\text{CO}_2\text{H})\text{CH}_2\text{CO}_2^- + \text{H}_3\text{O}^+ \tag{7}$$

The concentrations of the acidic form $c(\text{HA})$ and of the basic form $c(\text{A})$ in the buffer can be calculated at each pH according to the well-known Henderson-Hasselbalch equation $^{51}$:

$$\text{pH} = \text{pK}_a + \log \frac{c(\text{A})}{c(\text{HA})} \tag{8}$$

In this equation, $\text{pK}_a$ is the negative decadic logarithm of the acid constant. The Na$^+$ ion concentrations in Table 1 are obtained by a straightforward calculation.

The osmotic pressure of electrolytic solutions is proportional to the solute activities (or solute concentrations for ideal solutions). The swelling of polyelectrolytes is proportional to the osmotic pressure difference; the relation between the osmotic swelling pressure $\pi$ and the counter ion concentrations inside the ionomer $c(i)$ and in the buffer solution $c'(i)$ is given by the following equation $^{33}$:

$$\pi = RT \sum_i c(i) - c'(i) \tag{9}$$

R is the ideal gas constant and $T$ the absolute temperature. The counter-ions are Na$^+$ ions for cation-conducting SPEEK and for anion-conducting PSU-TMA: $\text{H}_2\text{PO}_4^-/\text{HPO}_4^{2-}, \text{CH}_3\text{CO}_2^-$ or $\text{O}_2\text{C(HO)}\text{C(CH}_2\text{CO}_2\text{H})_2/\text{O}_2\text{C(HO)}\text{C(CH}_2\text{CO}_2\text{H})\text{CH}_2\text{CO}_2^-$ in phosphate, acetate and citrate buffers respectively.

The counter-ion concentration inside the ionomer can be calculated from the ion exchange capacity and the dry density of the ionomers. For SPEEK, the dry density was determined before ($1.3 \, \text{g cm}^{-3}$ $^{35,51}$) and for PSU-TMA, the average value from 9 measurements was ($1.15 \pm 0.05$) g cm$^{-3}$. This gives molar counter-ion concentrations of 3.41 mol L$^{-1}$ and 1.47 mol L$^{-1}$ for SPEEK and PSU-TMA, respectively.
Gravimetric (WU) and volumetric (ΔV) water uptake of SPEEK and PSU-TMA

Given the molar counter-ion concentrations inside SPEEK and PSU-TMA, the osmotic swelling pressure is more than double for SPEEK than for PSU-TMA according to equation (9). Consequently, the WU and ΔV values for similar buffer concentrations are much larger for SPEEK than for PSU-TMA. Whereas in 0.1 M solutions, WU is about double for SPEEK in comparison with PSU-TMA in phosphate buffer, it is about triple for citrate and an even larger difference is observed for acetate. In all cases, except PSU-TMA in citrate buffers (see below), the volumetric swelling ΔV is larger than the gravimetric WU, showing that the membrane loses stiffness, due to the presence of the plastifying solvent.

Within a type of buffer, WU and ΔV can be correlated with the osmotic swelling pressure at a certain pH. For SPEEK in acetate buffers, the membrane dissolves totally at the most acidic pH where the counter-ion concentration is particularly low (acetic acid presents a low dissociation). In phosphate buffers, the WU is lower, due to the larger counter-ion concentrations in the outer solution, which contains a mixture of hydrogen- and dihydrogen-phosphate. According to the expectation, the WU is approximately double in 0.05 M phosphate buffer, due to the lower outer solution concentration leading to a larger osmotic swelling pressure. Intermediate data are observed in citrate buffer; evidently, some citrate co-ions are adsorbed by the ionomer and the large, strongly hydrated citrate ions drag supplementary water molecules. WU decreases with increasing counter-ion concentration in the citrate buffer solution. The increase of WU is lower than expected in the 0.05 M citrate buffer, because there is less driving force for co-ion adsorption from the more diluted solution.

For PSU-TMA, WU is generally much lower due to the lower IEC, which decreases the osmotic swelling pressure of PSU-TMA, especially in the acetate buffer. Furthermore, the difference between 0.1 and 0.05 M solutions is much lower than in the case of SPEEK, because the swelling pressure is much lower. One must also take into account the fact that divalent anions, present in phosphate and citrate buffers, are highly hydrated, due to the larger charge and increase WU.

For acetate buffers, one can clearly observe that an increase of the counter-ion concentration leads to a decrease of WU. The trend is opposite for phosphate buffers, due to an increasing concentration of divalent hydrogen phosphate ions with increase of pH. The case of citrate buffers is particular: it is the only buffer, where ΔV is consistently lower than WU. WU decreases with increasing counter-ion concentrations in the outer solution, because the amount of divalent ions increases. Furthermore, WU is nearly similar, or even decreases, in the 0.05 M buffer. These
surprising facts can be related to an ionic cross-linking mechanism by divalent citrate ions that is discussed below.

Variations of membrane area ($\Delta A$), thickness ($\Delta d$) and density ($D$)

Tables 1 and 2 show the area and thickness variations for SPEEK and PSU-TMA, respectively. One notices globally much larger variations for SPEEK than for PSU-TMA, in agreement with the larger gravimetric water uptake, particularly in the case of the citrate buffer, as discussed below in more detail.

Considering SPEEK, it is remarkable that while the area and thickness variations are consistent in the 0.1 M buffer solutions, the thickness variation is much smaller than the area variation in the 0.05 M buffers (Table 1). The hydration is anisotropic in these cases, probably due to the larger swelling pressure in the diluted solution.

An anisotropic swelling behaviour of proton-conducting membranes has been demonstrated before. Alberti and coworkers reported the formation of oriented chain arrangements in constrained Nafion, leading to a strongly anisotropic swelling and proton conductivity, but these layered phases were formed under uniaxial pressure and with pure water. Here, the swelling occurs without constraints, but it is clearly anisotropic in diluted buffers (0.05 M), which can be attributed to an initial orientation of uncross-linked SPEEK chains. This observation is of interest for the optimization of swelling and conductivity in SPEEK.

The density of wet SPEEK has an average value of $(1.15\pm0.05) \text{ g cm}^{-3}$ (Table 1) with the noticeable exception of samples immersed in 0.1 M citrate buffer, where the density is much lower. The most plausible explanation is that some adsorbed bulky citrate ions can enter the channels and expand their size, leading to a larger volume change. In the more diluted 0.05 M solution, this effect is not observed, because the adsorption of excess electrolyte decreases with decreasing concentration of the external solution, in agreement with the previous discussion.

In PSU-TMA, the WU and the change of membrane dimensions (area and thickness) are quite similar within the experimental uncertainty in phosphate and acetate buffers. One can conclude that there is no anisotropic swelling and that preferred chain orientations do not exist in PSU-TMA, but the volumetric swelling is always higher than the gravimetric water uptake, with the remarkable exception of citrate buffers. Here, $\Delta V$ is actually lower than $WU$. The average density is also higher than for the other samples. This singularity can be attributed to the presence of bulky doubly charged citrate counter-anions that permit an ionic cross-linking of macromolecular chains as shown schematically in Figure 3. This mechanism limits the volumetric swelling of the
ionomer, because the chains are held together by electrostatic forces. This hypothesis is corroborated by the extremely low ionic conductivity of PSU-TMA in citrate solutions (Table 2), because the citrate ions are trapped inside the ionomer by this mechanism (see below). Ionic cross-linking has previously been reported for cationic-conducting ionomers. To our knowledge, this is the first time that ionic cross-linking by anions is reported. One might ask why ionic cross-linking is not observed in the case of HPO$_4^{2-}$ anions; however, the anion size is also important, because the ion-ion interactions decrease strongly with the distance and the citrate ion is much bulkier than hydrogen-phosphate, which does not allow a sufficient proximity with the ionomer chains.

![Figure 3. Schematic anionic crosslinking of PSU-TMA by dicitrate ions.](image)

**Ionic conductivity of SPEEK and PSU-TMA as function of hydration and conducting ions**

In an ionomer, the ionic conductivity is due to the mobile counter-ions; the grafted ionic groups do not contribute. However, a contribution by excess ions adsorbed from the outer solution can play a role especially when the outer electrolyte solution is concentrated. The ionic conductivity is proportional to the concentration, mobility $u(i)$ and charge $q(i)$ of the mobile ions according to the well-known equation:

$$\sigma = \sum_i q(i) \cdot u(i) \cdot c(i)$$

(10)
A comparison of the ionic conductivity data reported in Tables 1 and 2 shows a much higher ionic conductivity of SPEEK vs PSU-TMA, which is evidently related to the more than double IEC of SPEEK, giving a more than twice higher mobile counter-ion concentration. Furthermore, the mobility of Na\textsuperscript{+} ions, which exchange the protons initially present in SPEEK, is higher than that of the mobile anions in PSU-TMA, but it is much lower than that of very mobile protons that can move by structural diffusion (Grotthuss mechanism). In accordance with this fact, the ionic conductivity is between 2 and 8 mS/cm, lower than for proton-conducting SPEEK\textsuperscript{37, 49}, due to the lower mobility of sodium ions in comparison with protons. The anion conductivity of PSU-TMA is between 0.2 and 1.3 mS/cm, except for citrate buffers, where the doubly charged citrate anion can form ionic cross-links and have a very low mobility.

Other subtle variations can also be observed. For example, there is a good correlation between the ionic conductivity of SPEEK and the concentration of the buffer. This correlation indicates a contribution of excess sorbed ions to the total ionic conductivity. In SPEEK with a high IEC, adsorbed ions cannot be removed by washing, because the membranes dissolve in pure water. Furthermore, there is an influence of the ion charge, because the amount of doubly charged HPO\textsubscript{4}\textsuperscript{2}\textsuperscript{-} ions increases with increasing pH, which gives a larger conductivity contribution due to larger adsorption. A similar observation can be made for the citrate buffer, where the concentration of doubly charged citrate ions increases with the pH. In acetate buffers at lower pH, where the concentration of Na\textsuperscript{+} ions is very low, the SPEEK membrane swells very strongly and even dissolves, so that the conductivity measurement is impossible.

Other factors, such as a different level of hydration, play also a role. We have previously shown for SPEEK the possibility to increase the ion conductivity by increasing the hydration level, due to the mobility increase at high dilution\textsuperscript{49}. In proton-conducting ionomers, this mobility change with hydration is well-known and attributed to the change of conduction mechanism with a higher contribution of structural diffusion vs vehicular diffusion\textsuperscript{59, 60}. Other factors such as a better connectivity of the ion-conduction channels and a better dissociation of ion pairs can also be operational. In fact, the conductivity of SPEEK in 0.05 M phosphate buffer is identical or even higher than in 0.1 M solutions, evidently due to a higher WU. In this case, the pH dependence is also lower, probably due to a lower sorption of ions from the more diluted buffer solution.

The consistently lower ionic conductivity of PSU-TMA membranes is related to the lower IEC and the lower anion mobility. Furthermore, the membranes were washed in water before the measurements, because they do not swell excessively, so that an important influence of excess ions sorbed from the buffer solution can be excluded here. The relatively high conductivity of
acetate anions in PSU-TMA is in good agreement with the previously reported value\footnote{61}. Given the generally low values of $W/U$, the improvement of ionic conductivity in 0.05 M solution observed for SPEEK, is not detected in PSU-TMA.

The extremely low ionic conductivity determined for PSU-TMA in citrate buffer is consistent with an ionic crosslinking by the divalent citrate ions, which are therefore trapped inside the ionomer and have an extremely low mobility (Figure 3).

Conclusions

This work shows the importance of ion concentrations for the hydration and conductivity behaviour of ionomer membranes. An increasing concentration of ions in buffer solutions reduces the gravimetric water uptake. A simple interpretation of the hydration data can be based on the osmotic pressure dependence. The area and thickness variations show that for SPEEK in diluted buffer solutions, where the swelling pressure is higher, the variation of dimensions is larger in the plane than in the transverse direction. This anisotropy might be related to a pre-orientation of the chains. In PSU-TMA, the volumetric water uptake is larger than the gravimetric one, except in citrate buffer; this result is attributed to an ionic cross-linking by the bulky citrate di-anion, which reduces the volumetric swelling. The ionic conductivity confirms this ion-specific effect, because the ionic conductivity of the anion-conducting membrane is very low in citrate buffer.

A good compromise between low swelling and relatively high ionic conductivity is found in phosphate buffers, which seem most appropriate for use in enzymatic fuel systems.

Acknowledgments

The financial support of CNRS in the frame of the exploratory project “IMPEC” is gratefully acknowledged.

References

Hydration and Ionic Conductivity of Model Cation and Anion-Conducting Ionomers in Buffer Solutions (Phosphate, Acetate, Citrate)

L. Pasquini, O. Wacrenier, M. L. Di Vona, P. Knauth