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# **Extending the Balbi fire spread Model for field scale conditions:**

# the case of shrubland fires

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Abstract: The 'Balbi model' is a simplified rate of fire spread model aimed at providing fast and accurate simulations for fire spread that can be used by fire managers under operational conditions. This model describes the steady-state spread rate of surface fires by accounting for both radiation and convection heat transfer processes. In the present work the original Balbi model developed for laboratory conditions is improved with changes that address specificities of outdoor fires, such as fuel complexes with a mix of live and dead materials, a larger scale and an open environment. The model is calibrated against a small training dataset (n=25) of shrubland fires conducted in Turkey. A sensitivity analysis of model output is presented and its predictive capacity against a larger independent dataset of experimental fires in shrubland fuels

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from different regions of the world (Europe, Australia, New-Zealand and South Africa) is tested. A comparison with older versions of the model and a generic-empirical model is also conducted to investigate contrasts with other models and quantify improvements in the predictive capacity of the model. The improved model remains physics-based, faster than real time and fully predictive. Keywords: Fire spread, shrubs, live fuel, radiation, convection, fire dynamics, model performance, physical model, steady-state model 

#### Introduction

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Many regions of the world are severely hit by severe wildfires. As the result of interactions between climate, fuels, topography and people, wildfires can have negative socioeconomic and ecological consequences (Finlay et al. 2012; Meyer et al. 2013; Youssouf et al. 2014; Castro Rego et al. 2018; Dupuy et al. 2020; European Science & Technology Advisory Group 2020). They represent a significant factor changing ecosystem function and resilience (Wotton et al. 2003; Running 2006; Sağlam et al. 2008; Fernandes 2013; San-Miguel-Ayanz et al. 2013; Tang et al. 2015) and they pose a threat to human life, infrastructure and activities, particularly when fires spread into the Wildland-Urban Interface (Radeloff et al. 2005; Hammer et al. 2007; Keane et al. 2010). These negative impacts of wildfires have been exacerbated as a result of climate change (European Science & Technology Advisory Group 2020). The need for fire spread simulation tools (e.g. Finney (1998); Filippi et al. (2011); Mandel et al. (2011)) that aid emergency response, firefighting and fire management decision making has become more and more crucial. Development of new fire spread models that overcome previous ones constrains and limitations is one the the main aims of fire behaviour scientists around the globe. Over the last three decades, significant advances made on physical and chemical modelling of wildland fire processes has contributed to the development of a significant number of models describing wildfire propagation. This model evolution reviewed by several authors (Weber 1991; Perry 1998; Pastor et al. 2003; Sullivan 2009a; b; c) is basically categorized in three main approaches: (1) mathematical or empirical models, (2) semi-empirical models and (3) physical models. Statistical or empirical models (McArthur 1966; Noble et al. 1980; Cheney et al. 1998; Anderson et al. 2015; Rossa and Fernandes 2018) are generally built over a large set of observational data and they do not describe any physical mechanisms for heat transfer. The fire rate of spread is usually defined as a function of several independent variables such as wind

velocity, terrain slope angle, fuel moisture content and fuel structure variables (Cheney et al. 1998; Fernandes 2001; Keane 2019a). Semi-empirical models, such as the well-known Rothermel model (Rothermel 1972), are able to simplify the physical description of the fire spread processes while incorporating some key principles. Both the empirical and semiempirical approach produced models that are applicable to operational conditions. For example, the Rothermel (1972) is at the core of fire behaviour prediction systems like BEHAVE (Andrews 1986) and FARSITE (Finney 1998). It is also incorporated in more comprehensive fire - weather prediction systems like WRF-SFIRE (Mandel et al. 2011; Kochanski et al. 2013). In contrast, physical models are based on the understanding of physical and chemical processes determining wildland fire behaviour. These models describe how the heat, mass and momentum fluxes are transferred from the fuel burning zone or from the flame body to the unburnt fuel (Lattimer 2019). Detailed physical models based on multiphase modelling (Grishin 1997; Morvan et al. 2000) solve a system of partial differential equations strongly coupled obtained from the gaseous phase and the different solid phases and represent the physical basis of computational fluid dynamics (CFD) simulators such as FireStar2D (Morvan et al. 2009), FireStar3D (Frangieh et al. 2018; Morvan et al. 2018), FIRETEC (Linn and Cunningham 2005) or Wildland Urban Interface Fire Dynamics Simulator, WFDS (Mell et al. 2007). These CFDmodels are of great interest to extend our understanding of the physics of the fire dynamics but they are not suitable for simulating fire spread at large scales and under time contraints because of the high computational requirements. Simplified physical models (Pagni and Peterson 1973; Albini 1985, 1986; Koo et al. 2005; Balbi et al. 2007) are a family of models that can bridge the gap between the simple empirical models and complex physical models. They incorporate the most important physical processes without having the computational needs of a full physical model, allowing for their use in operational settings. These models require parameterization of certain intermediate processes.

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but this parameterization can be done with only a few fires in contrast with the data needs for the development of empirical models. This is significant due to the costs and inherent limitations of conducting large scale, high intensity experimental fire programs.

The 'Balbi model' (Balbi *et al.* 2020) follows this concept. The model is a fully predictive simplified physical model for surface fire spread which takes into account meteorological (wind velocity), topographical (terrain slope angle) and fuel (fuel moisture and fuel bed structure) conditions. The model has been developed and parameterized to describe fire propagation in free spreading fires at a laboratory scale (e.g. Nelson Jr. and Adkins (1986); Catchpole *et al.* (1998)).

The main goal of this paper is to extend the previous work by introducing changes that allow its use in outdoor fires, where scale and fuel characteristics depart from the original model fitting. The parameterization is applied to shrubland fuel types, an interesting challenge for the proposed model due to the stratified fuel complex arrangement composed of vertically separated fuel layers (Cruz *et al.* 2013). The new formulation is evaluated through the analysis of the effect of environmental variables in the model ouput and against a large set of outdoor shrubland fires given in (Anderson *et al.* 2015). A comparison between the obtained model fit statistics with results from other models is also made.

# Methods

#### Model idealization

The Balbi et al. (2020) model

The global structure of the model proposed by Balbi *et al.* (2020) is kept, with changes introduced that aim at simulate relevant processes occurring in shrubland fires. Following Chatelon *et al.* (2017) and Balbi *et al.* (2020), it is still assumed that the fresh airstream which

enters the flame base (the pyrolysis area) is divided in two layers (Fig. 1): the hot gases from the upper layer are driven to the top of the flame base, due to buoyancy and create the free flame structure above the vegetal stratum. The mixed air-pyrolysis gases from the lower layer go out through the front panel of the fuel burning particles area and create an internal, or combustion zone, flame which directly contacts the unburnt fuel.

The four energy contributions suggested by Balbi *et al.* (2020) are considered: (1) flame base radiation (the fuel burning particles radiate towards the unburnt fuel); (2) flame radiation (the flame body acts as a grey radiant panel); (3) convective cooling (the flame body creates a indraught of fresh air coming from the unburnt zone which offsets the flame radiation and the periodic free flame contact with unburnt fuels because of turbulent effects); and (4) convective heating (hot gases flow from the combustion zone and impinge the unburnt fuel particles by direct contact). Note that the convective cooling effect did not explicitly appear in the equation of the model but is incorporated in the flame radiation modelling (Balbi *et al.* 2010).

The rate of spread was obtained using a simplified preheating balance and based on the fuel load  $\sigma$  and fuel moisture content m of the dead fuel. The main equation of the model, in a condensed form, is the following:

121 
$$R = R_b + R_c + R_r$$
 (1)

122 With

$$123 R_b = a_b \frac{\phi_b}{\sigma q} (2)$$

$$124 R_c = a_c \frac{\phi_c}{\sigma q} (3)$$

$$125 R_r = a_r \frac{\phi_r}{\sigma q} (4)$$

where  $R_{\bullet}$ ,  $\phi_{\bullet}$ ,  $a_{\bullet}$ , are the contributions of heat transfer mechanisms to the ROS, heat fluxes and scaling factors, respectively. The term q represents the energy required for ignition:

128 
$$q = C_p(T_i - T_a) + m(\Delta h + C_{pw}(T_{vap} - T_a))$$
 (5)

- where  $C_p$ ,  $C_{pw}$ ,  $T_i$ ,  $T_a$ ,  $T_{vap}$ ,  $\Delta h$ , m are specific heat of fuel and water, ignition, ambient and
- vaporization temperature, heat of latent evaporation and fuel moisture content respectively (see
- 131 Table 1).
- 132 Changes in the scaling factors
- The scaling factors in Eqns 2-4 are modified in order to take into account the live fuel. As the
- flame base scaling factor  $a_b$  increases with the fuel height and decreases with the extinction
- depth  $\delta$ , it was defined in (Balbi *et al.* 2020) by the following relationship:

$$136 a_b = \min\left(2\frac{h}{\delta},1\right) (6)$$

137 Two slight changes are made on Eqn 6. First, the factor 2 in Eqn 6 is removed because it is 138 assumed that at field scale the soil absorbs a part of the flame base radiative flux unlike the 139 laboratory experiments in which the ground reflects the flame base radiation. Second, following 140 the work of De Mestre et al. (1989) about optical depth, Balbi et al. (2020) have defined the 141 extinction depth as inversely proportional to the fuel porosity ( $\delta = 2\pi/(s \beta_t)$ ), where s is the 142 surface area to volume ratio and  $\beta_t$  is the total packing ratio (dead and live fuel load). So, 143 considering the total leaf area  $S_t$  (equal to the double of total LAI (Keane 2019b)), the scaling 144 factor  $a_b$  is changed in:

$$145 a_b = \min\left(\frac{S_t}{2\pi}, 1\right) (7)$$

Moreover, as one part of the heat release affects the live fuel and assuming that the spread of the ignition interface mainly depends on the catalytic effect of dead fuel, the leaf areas ratio (dead and total) is added to the scaling factor  $a_b$ :

$$149 a_b = \min\left(\frac{S_t}{2\pi}, 1\right) \left(\frac{S}{S_t}\right)^2 (8)$$

- 150 The square on the ratio  $S/S_t$  expresses the action of this 'energy sink' effect on both emitted and 151 absorbed flame base radiation, where S is the leaf area  $(2 \times LAI)$ . As noticed by Chandler et al. 152 (1983), it seems that live fuel properties have a role on fire behaviour but this role is not clear (Pimont et al. 2019) and still discussed in the literature. Inhere, it is assumed that the live fuel 153 154 is not directly involved in movement of the ignition interface, but as it contributes a proportion 155 of the heat released, the part of the heat which does not imping the dead fuel material is added 156 in the improved model as the ratio between dead leaf area and total leaf area (which is related 157 to a ratio between dead and total packing ratio).
- The scaling factor  $a_r$  related to the flame radiation heat flux is similarly modified but only the absorption of this heat flux by the unburnt fuel is concerned:

$$160 a_r = \min\left(\frac{h}{\delta}, 1\right) \frac{S}{S_t} = \min\left(\frac{S_t}{2\pi}, 1\right) \frac{S}{S_t} = \min\left(\frac{S}{2\pi}, \frac{S}{S_t}\right)$$
 (9)

The scaling factor  $a_c$  related to the convective heat flux is significantly changed. It is now split up in three contributions which corresponds to energy losses:

$$163 a_c = a_{up} a_{lat} a_{liv} (10)$$

The factor  $a_{liv}$  represents the heat provided to the unburnt live fuel and the same modelling as in the scaling factors  $a_b$  and  $a_r$  is chosen:

$$166 a_{liv} = \frac{s}{s} (11)$$

The factor  $a_{lat}$  describes the heat loss on the lateral edges of the fire front. Balbi  $et\ al.$  (2020) assumed this factor was equal to 1 for a laboratory set up where lateral walls constrained lateral heat losses at the combustion zone level (Catchpole  $et\ al.$  1998). In our present formulation it is assumed that this factor explicitly depends on the effective fireline width  $W_0$  (Cheney and Gould 1995) but remains equal to 1 when  $W_0$  is greater than 50 m. For the current analysis  $W_0$  is represented by the ignition line length in (Anderson  $et\ al.$  2015).  $W_0$  in the dataset change with experimental source/fuel type. See appendix B for further discussion):

$$174 a_{lat} = \min\left(\frac{W_0}{50}, 1\right) (12)$$

Finally the factor  $a_{up}$  expresses two combined effects. The first one corrects the amount of pyrolysis gases produced by the airstream below the streamline which enters the flame base at point E (see Fig. 1). Indeed, this zone delimited by points  $BB_0A_0E$  was approximated by the surface of the triangle  $BB_0F$ . The second effect corresponds to the heat remaining in the fuel burning particles area when the heat released to the upper part of the fuel is removed. This effect is assumed to be proportional to the total leaf area  $S_t$  ( $S_t = s h \beta_t$ , where h is the fuel bed depth and  $\beta_t$  the total packing ratio) and inversely proportional to the flux of gases moving upward i.e the upward gas velocity in the preheating zone which is proportional to the root square of the fuel bed depth (due to buoyancy forces). The parameter  $a_{up}$  is modelled according to the following empirical relationship:

$$185 a_{up} = a_M s \, \beta_t \sqrt{h} (13)$$

With  $a_M$  being an empirically parameter fitted to a training dataset through a calibration protocol. After this fitting,  $a_M$  is considered a constant for the application of the model to simulating fire spread in shrubland fuel complexes.

Finally, combining Eqns 11-13, Eqn 10 yields:

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$$a_c = a_M s \,\beta_t \sqrt{h} \min\left(\frac{W_0}{50}, 1\right) \frac{S}{S_t}$$
 (14)

- 191 Changes in the convective heat contribution
- According to (Balbi *et al.* 2020) the convective heat flux is modelled as:

193 
$$\phi_c = \frac{\Delta H}{2\tau_0} \sigma s \min(h, \delta) \tan \gamma_c$$
 (15)

- Where  $\Delta H$  and  $\tau_0$  are the heat of combustion of pyrolysis gases and the flame residence time
- parameter, respectively. The angle  $\gamma_c$  is defined as in Fig. 1 by:

$$196 \quad \tan \gamma_c = \tan \alpha + \frac{U(L)}{u_c} \tag{16}$$

- where U(L),  $u_c$  and  $\alpha$  are horizontal wind speed at point B, upward gas velocity at the top of
- the flame base and terrain slope angle, respectively.
- Due to the vertical dimension of the fuel bed, namely due to the existence of live fuels on its
- 200 top, the definition of U(L) is slightly changed. It is expressed as a function of wind velocity U
- at flame mid-height and drag forces:

202 
$$U(L) = U \frac{h}{h + \frac{H}{2}} exp(-K^*L)$$
 (17)

- where H, L and  $K^*$  are the flame height, flame depth and a drag coefficient, respectively. This
- decrease in wind velocity along the flame base has been reported by Anderson *et al.* (2010).
- Flame depth L is equal to the product of the R and flame residence time  $\tau$  (L = R  $\tau$ ). In the
- 206 current formulation flame residence time is estimated from surface area-to-volume ratio ( $\tau =$
- $\tau_0/s$ ) as parameterised by Anderson (1969). The modelling of drag forces is slightly modified
- in order to take into account the whole fuel (live and dead fuel) and the drag coefficient  $K^*$  is

- assumed to linearly depend on fuel porosity ( $K^* = K_1 s \beta_t$ ) with  $K_1$  is a drag coefficient. So Eqn
- 210 17 yields

211 
$$U(L) = U \frac{h}{h + \frac{H}{2}} Exp(-KR)$$
 (18)

where the drag forces law K is defined as follows:

213 
$$K = \frac{\beta_t}{\min(\frac{W_0}{50}, 1)}$$
 (19)

- Note that, contrary to (Balbi et al. 2020), the model coefficient  $K_1$  depends on  $W_0$  and thus it is
- removed from Eqn 19 and is not a model parameter anymore.
- Finally, after some simplifications (see Appendix C for further calculus), combining Eqns 4,
- 217 15-16 and 18-19 yields

$$218 R_c = a_M \min\left(\frac{W_0}{50}, 1\right) \frac{\Delta H \rho_a T_a s \sqrt{h}}{2q(s_t + 1)\rho_v T} \left(\frac{(s_t + 1)}{\tau_0} \frac{\rho_v}{\rho_a} \frac{T}{T_a} \min\left(S, \frac{2\pi S}{S_t}\right) \tan \alpha + U Exp\left(-\frac{\beta_t}{\min\left(\frac{W_0}{50}, 1\right)} R\right)\right) (20)$$

- 219 Main equations of the improved model
- Combining Eqns 2-4, 8, 9, 15 and 20, the equation (1) of the ROS is written in its detailed
- 221 expression:

222 
$$R = \min\left(\frac{S_t}{\pi}, 1\right) \left(\frac{S}{S_t}\right)^2 \frac{BT^4}{\beta \rho_v q} + AR \frac{(1 + \sin \gamma - \cos \gamma)}{1 + \frac{R\cos \gamma}{ST_{ss}}} +$$

$$+ a_{M} \min\left(\frac{W_{0}}{50}, 1\right) \frac{\Delta H \rho_{a} T_{a} s \sqrt{h}}{2q(s_{t}+1)\rho_{v} T} \left(\frac{(s_{t}+1)}{\tau_{0}} \frac{\rho_{v}}{\rho_{a}} \frac{T}{T_{a}} \min\left(S, \frac{2\pi S}{S_{t}}\right) \tan \alpha + U Exp\left(-\frac{\beta_{t}}{\min\left(\frac{W_{0}}{50}, 1\right)} R\right)\right)$$
(21)

where the radiative factor *A* is defined as following:

$$225 A = \min\left(\frac{S}{2\pi'S_t}\right)^{\chi_0\Delta H}_{4q} (22)$$

Equations for the flame tilt angle γ, flame height *H* and flame temperature *T* are not changed
since (Balbi *et al.* 2020):

$$228 \quad \tan \gamma = \tan \alpha + \frac{U}{u_0} \tag{23}$$

229 
$$T = T_a + \frac{\Delta H (1 - \chi)}{(s_t + 1)C_{pa}}$$
 (24)

230 
$$H = \frac{u_0^2}{g(\frac{T}{T_a} - 1)}$$
 (25)

231 Egns 21-25 can be summed up in one non linear algebraic equation (Egn 21). As the ROS given 232 in eqn 21 depends on environmental parameters (wind velocity, terrain slope angle, ignition 233 line length, ambient temperature), fuel characteristics (dead FMC, total leaf area, packing ratio, 234 fuel density, surface area-to-volume ratio, heat of combustion of pyrolysis gases, specific heat 235 of fuel) and on the ROS itself, an iterative method is necessary to numerically solve this 236 equation. A convergent series is built in which its first term is the solution of the radiative model 237 defined by Eqn A2 (solution of second order polynomial). Then a loop is performed up to 238 convergence.

Note that Eqn 21 depends on four model parameters: the air-pyrolysis gases mass ratio in the flame body  $(s_t)$ , a model coefficient  $(r_{00})$ , a radiant factor  $(\chi_0)$  and a fitted model parameter  $(a_M)$ . Of these all but  $a_M$  have been determined by Balbi et al. (2020) and are not expected to vary for the current model parameterization. Parameter  $a_M$  needs to be determined for field scale fires. As the various parameter values are assumed to not vary with fuel characteristics in free-spreading shrubland fires, the proposed model is fully predictive.

## Data

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Two distinct field scale, experimental fire datasets were used in the present analysis. One for model calibration and the other for model evaluation against independent data.

#### Model calibration

Model calibration for its application to field scale shrubland fires required the estimation of the  $a_M$  parameter. This model calibration used the experimental dataset published by Bilgili and Saglam (2003). This series was carried out in a shrubland fuel type (maquis) in Turkey. These authors reported on a study where 25 experimental shrubland fires were conducted on flat ground under a range of weather and fuel conditions. Plot size was 20 x 30 m, for a 20 m ignition line and 30 m run. Wind speed (measured at 1.8 m height) varied between 0.27 m s<sup>-1</sup> and 4.11 m s<sup>-1</sup>. Fuel height ranged between 0.35 m and 1.15 m. Fine fuel load for the dead and live components ranged between 0.46 and 0.82 kg m<sup>-2</sup>, and 0.95 and 1.49 kg m<sup>-2</sup>, respectively. Rate of fire spread varied between 0.013 and 0.11 m s<sup>-1</sup>. Further details on environmental conditions are given in the original publication. The estimation of the  $a_M$  parameter was based on the parameter that would minimize error and bias.

#### Sensitivity analysis

<u>A</u> univariate sensitivity (Millington et al. 2009) analysis was conducted to quantify the effect of different fuel parameters on the modelled *R*. This analysis allows to identify the most influential variables in the R ouput. This analysis considers a benchmark simulation on flat ground under a 2 m s<sup>-1</sup> fuel level wind velocity, 10% dead fuel moisture content and a total fine fuel loading of 0.5 kg m<sup>-2</sup>. The full list of variables tested in the analysis and their default values is given in Table 2). The sensitivity analysis consists in calculating the percent change in ROS between the benchmark environment and the simulation with the fuel parameter perturbed by plus or minus 10%. This analysis considers the effects of the variable perturbation separately

applied to each fuel characteristic. Note that the perturbation of total fine fuel loading only affects the fine live fuel load because the dead fuel loading of 0.3 kg m<sup>-2</sup> does not vary.

#### Model evaluation

The proposed model predictive capacity was evaluated through its application to the data given in (Anderson *et al.* 2015) and (van Wilgen *et al.* 1985). Anderson *et al.* (2015) gathered a large set of experimental field fires from several regions of the world, namely from (New Zealand, Spain, Portugal, Australia and South Africa. The dataset in Anderson *et al.* (2015) provides the necessary detail relative to fire environment and fuel variables that allow the evalution of Eqn (21). Of the 135 fires reported in the Anderson's database (Table A1 in (Anderson *et al.* 2015)), only fires where live fuel data, quantity and moisture content were given (n = 109) were used. This dataset was complemented with the data from 14 experimental fires conducted on fynbos vegetation by van Wilgen *et al.* (1985) in South Africa. This data was used by Anderson *et al.* (2015) but the data not given in their table A1. A usual power law wind profile (Peterson and Hennessey Jr 1978) is used to calculate the wind speed at fuel height necessary to run the proposed model.

#### Benchmark models used for model fit comparison purposes

To better understand the relevance of the obtained model fit statistics, the evaluation statistics obtained with Eqn 21 are compared to the results obtained using other existent models against the same datasets. The following models were run against the (Anderson *et al.* 2015) dataset (equations of each model are provided in appendix A): (1) a predictive version of the radiative only model presented by Balbi *et al.* (2010) (Eqn A1), (2) the generic shrubland fire spread model provided by Anderson *et al.* (2015) (Eqn A4) and (3) the simplified physical model given by Balbi *et al.* (2020) (Eqn A5). We note that the evaluation data being use here was part of the dataset used to develop the Anderson *et al.* (2015) model.

#### 293 Statistics used

The error between predicted and measured values is quantified through a number of metrics. To estimate the overall deviations we used the normalized mean square error (NMSE) introduced by Poli and Cirillo (1993). The fractional bias (FB, see (Warner *et al.* 2004)) was used to understand the model's under-predictions or over-predictions trends. This normalized tool makes the bias non-dimensionless. It varies from -2 to +2 and a positive value indicates an overestimated measured value. An ideal model is obtained for an ideal value of zero for NMSE and FB. Residuals (res = predicted R – observed R) and relative error (res/observed R) are also used in the analysis.

# **Numerical Results**

#### Model calibration

The proposed model (Eqn 21) exhibits four model parameters. The values of three of these parameters ( $s_t = 16$ ,  $r_{00} = 2.5 \times 10^{-5}$ ,  $\chi_0 = 0.3$ ) are set in (Balbi *et al.* 2020) and do not change in the proposed model. Indeed these three parameters are related to flame radiation whose modelling did not evolved. The  $a_M$  parameter was found to be most suitable parameter to parametrize the model for its application against outdoor fires. A value of 0.025 for the  $a_M$  parameter leads to the best agreement between the predicted and the observed ROS in (Bilgili and Saglam 2003) dataset (see Fig. 2). This value and the ensuing fit produce a small deviation (NMSE=0.038) without bias (FB=0.00). This parameter is assumed to be a universal coefficient, with its value not changing when applying the model to other field fires, i.e. it is independent of environmental, topographical and fuel conditions.

#### Model behaviour

315 Fig. 3 illustrates the predicted R with changes in some of the most influential environmental 316 variables in shrubland fires, namely wind speed, fuel moisture and fuel height (e.g. (Fernandes 317 et al. 2000; Anderson et al. 2015)). Benchmark values are given in Table 2. 318 Modelled ROS against wind velocity for 5 different values of the dead fuel load (0.1, 0.15, 0.2, 319 0.25 and 0.3 kg m<sup>2</sup>) shows R increasing linearly with wind speed (Fig 3a) for the lower fuel 320 loads (0.1 and 0.15 kg m<sup>2</sup>). For the higher fuel loads simulated (0.2, 0.25 and 0.3 kg m<sup>2</sup>) the 321 model suggests a slow increase of the ROS for low wind speeds and then a faster increase for 322 wind speeds greater than 2.5 m s<sup>-1</sup>. Fig. 3a also shows that for each value of wind speed, the 323 ROS increases with the dead fuel load but the difference between ROS calculated for two 324 consecutive dead fuel loads tends to decrease with increasing fuel load. This suggests that the 325 model identify the relative influence of fuel load on the ROS to gradually decline with 326 increasing fuel loads. For example, for a 10 m s<sup>-1</sup> wind speed, the variation of the ROS 327 calculated from consecutive dead fuel loads are 0.12, 0.10, 0.07 and 0.05 m s<sup>-1</sup>. These 328 simulations assume a constant fuel bed height, with changes in fuel load affecting the fuel layer 329 bulk density, a fuel bed parameter influencing a number of fluid flow and heat transfer 330 efficiencies (Rothermel 1972; Anderson et al. 2015). The effect of fuel load, fuel height and 331 bulk density on fire propagation in shrubland vegetation are intimately connected, and it is often 332 difficult, if not impossible, to extract the effect of one variable independently from the effect of 333 the other two in natural fuel beds. We did not explicitly investigate the effect of fuel bulk density 334 on model behaviour in this analysis due to space constraints. 335 The effect of FMC on ROS is presented in Fig. 3b, using the ratio the predicted ROS and an 336 hypothetical ROS for zero FMC (R/ROS(m=0)), as per (Morvan 2013). The observed decay in 337 ROS/ROS(m=0) expressing the relative influence of FMC on ROS follows the trends obtained 338 by Balbi et al. (2020), by simulations carried out with FireStar2D (Morvan 2013) and the 339 exponential decay in ROS as a function of FMC modelled by Anderson et al. (2015), Fernandes

et al. (2009) or Rossa et al. (2016). As found by Anderson et al. (2015), the effect is not pronounced.

The influence of fuel bed height on ROS is illustrated in Fig. 3c for four different wind velocities (2.5, 5, 7.5 and 10 m s<sup>-1</sup>). The ROS is found to increase with fuel height independently of wind speed. A doubling in fuel height from 1 to 2 meters results in a 31% increase on average in *R* but it is noticeable that this increase in the *R* output is more pronounced for low wind speeds (42.8%, 31.4%, 27.3%, 25.2%, for wind speeds of 2.5, 5, 7.5 and 10 m s<sup>-1</sup> respectively). Results also indicate that the higher the fuel bed height the lower the effect of height increases (whatever the wind speed).

#### Sensitivity analysis

The univariate sensitivity analysis shows that the fuel characteristics leading to the most important variation in ROS are surface area-to-volume ratio, fuel density, heat of combustion of pyrolysis gases and specific heat (see Table 2). All these variables showed an effect approximately proportional to the 10% perturbation. It is important to notice that these variables, with the exception of surface area-to-volume ratio, tend to be considered constant in fire behaviour modelling. The  $\pm 10\%$  change in fuel height and dead fuel moisture content result in an approximate 5% change in the R output. Fuel load parameters, dead and total, were the fuel variables showing the least impact on the change in R, with the perturbation leading to an absolute percent change varying between 0.8 and 3.5%. These results are restricted to the range of the defaut values used in the sensitivity analysis. A more comprehensive sensitivity analysis over the natural range of the fuel variables tested would likely show areas where the model will be more sensitive to changes in environment conditions.

## Model evaluation and comparison

The scatter diagram plotted in Fig. 4a compares predicted and observed ROS for fires conducted in New Zealand (NZ), Australia (WC and SA), Portugal (PT), Spain (SP) and South Africa (SoA). The solid line and dashed lines represent the line of perfect agreement and  $\pm 35\%$  error levels, respectively. A good overall agreement is found with an average NMSE of 0.132 and a slight under-estimation of the predicted ROS (FB=-0.03). Larger relative errors presented in Fig. 4c seem to concentrate in the lower rates of fire spread. Table 3 displays the full model performance results for each experimental series. It is noticeable that deviation results are very low (NMSE close to 0) for all the experimental fire series, with the exception of the Portugal fire dataset that yield a NMSE of 0.308. Fig. 4c illustrates behaviour with the Portugal fires subset showing the largest relative error of all data subsets. Fig. 5a and b plot residuals and relative error as a function of observed ROS in four broad classes. The residual distribution shows the model to produce unbiased results within the three lower R classes ( $R < 0.5 \text{ m s}^{-1}$ ) and a higher under-prediction for the faster spreading fires (R > 0.5 m s<sup>-1</sup>). The analysis of the percent error shows that this increase in residuals for faster fires is associated with the lowest percent errors (Fig. 5b). The model error in a relative sense decreases considerably as the observed *R* increases.

Analysis of modelled convective and radiative heat transfer

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The bubble diagram (Fig. 6) plots the convective ( $R_c$ , Eqn 3) v. radiative ( $R_b+R_r$ , Eqns 2 and 4) contributions calculated on the datasets of Anderson *et al.* (2015) and Bilgili and Saglam (2003). Wind speed is the third variable and the larger the bubble sizes, the larger the wind speed. The solid line represents the perfect equilibrium between these two contributions. Fig. 6 shows the model identifying convection as the main heat transfer mechanism for 79.7% of the fires (118 of 148). Radiation is identified as dominant in all the 10 fires of one of the Australia fire group (SA). If convection is found to drive all the South African (SoA), Turkish (TU) and Australian (WC), the convective contribution to the ROS also outweighs the radiative effects

in the major part of New Zealander (NZ), Portuguese (PT) and Spanish (SP) fires (89.2%, 79.2% and 72.73% respectively). So, overall, the model formulation identified convection as the most influential heat transfer mechanism driving fire propagation. As an exception, two Spanish fires burning under nil, or zero, wind conditions had radiative heat transfer largely dominating fire propagation.

## Comparison with other models

The comparison of model fit statistics obtained with the eqn 21 model and previous published models is presented in Table 3. The Balbi *et al.* (2010) radiative model yields the largest NMSE and a strong underestimation. The results obtained by the Anderson *et al.* (2015) empirical model (NMSE=0.180, FB=-0.05) were expected to a good approximation of the observed ROS as the data used in this evaluation was part of the data used in the development of the model (Eqn A4). The Balbi *et al.* (2020) model also produced very encouraging results, with an overall NMSE of 0.183 and a FB of -0.02. This corroborates Balbi *et al.* (2020) claims that their model could be used at field scale even if it was developed at laboratory scale. Overall, the eqn 21 model produced the best results of all the models analysed, with small overall deviations (NMSE=0.132) and a bias close to zero (FB=-0.03). Fig. 7 presents the comparison between the previous models as a scatter plot; the Balbi *et al.* (2010) radiative model was removed from this plot because of its poor agreement with observed data.

#### Discussion

- Effect of domimant environmental variables
- The proposed model produces a quasi-linear relationship between *R* and wind speed, with the increase in wind speed resulting in an increase in *R* following expectations from laboratory and field observations (Bilgili and Saglam 2003; Mendes-Lopes *et al.* 2003; Butler *et al.* 2019). The

wind speed effect depends on other fuel characteristics, due to the effect of structural fuel characteristics on heat transfer processes. As example, fuel load affects the radiative coefficient  $(0.1 \text{ and } 0.15 \text{ kg m}^{-2} \text{ lead to } A=0.27 \text{ and } A=0.41, \text{ respectively})$ , and this effect is dependent on wind speed as well. The linear (when  $A < \frac{1}{2}$ ) or quasi-linear ( $A > \frac{1}{2}$ ) ROS trend agrees with experimental results presented by Beer (1991) on match splints, Rothermel and Anderson (1966) on ponderosa pine and white pine needles fuel beds or Cheney et al. (1993) on grass fuel (where the exponent modelling the effect of wind speed on ROS,  $R \propto aU^b$  is close to 1). At zero wind speed, both the convective effects and the radiative contribution from the flame body are nil (on flat ground) or close to zero (on sloped ground) and the fire is driven by the flame base radiation  $(R_b)$ . As wind speed U increases, the convective  $(R_c)$  and radiative  $(R_r)$ contributions increase as well, directly through U in  $R_c$  (Eqn 20) and through the increasing flame tilt angle for  $R_r$  (Eqn 23). Note that if  $R_r$  is always an increasing function of the wind speed,  $R_c$  theoretically increases with wind speed up to a threshold wind speed value because of the exponential in its definition. This threshold value is difficult to assess but it is quite an extreme value of the wind speed. As example, selecting the ROS obtained in the numerical simulations for a dead fuel load of 0.2 kg m<sup>-2</sup>, R<sub>c</sub> increases from 0 to 0.65 m s<sup>-1</sup>, which means that the threshold value is not reached, even for a 25 m s<sup>-1</sup> wind speed. The model suggests an effect of fuel height on R to be dependent on other fire environmental variables. For low wind speeds a doubling in fuel height results in an approximately 50% increase in R, as found in the univariate sensitivity analysis. The same doubling in fuel height at high wind speeds can result in a 25 to 35% increase in R. The effect captured by the model is comparable to the effect captured by Anderson et al. (2015) model. Nonetheless, the physics nature of the proposed model allowed to captured a more nuanced effect as influenced by other environmental and fuel conditions. It is noticeable that the most sensitive fuel characteristics for the proposed model are intrinsic fuel properties (fuel characteristics directly related to the

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fuel species). Nonetheless, it should be noticed that these intrinsic fuel characteristics vary within a narrow range comparatively to the range in structural variables such as fuel load or fuel height. Our results also show that the sensitivity of the model to the variation in the extrinsic fuel characteristics (FMC, height and load) does not cause large errors on the ROS output. This is encouraging from the point of view that within an operational fire simulation setting, an error in these estimates leads to a controlled error on the ROS.

# Model predictive performance

The overall comparison between predicted and observed ROS on the Anderson's dataset leads to a NMSE of 0.132 with a bias close to zero (FB=-0.03). We consider this to be a very good result for the application of fire spread models at a field scale, especially when the model was applied to shrubland fires from different sources and covering a broad range of fuel structures. The results showed that the model performance was worse for the dataset of Portuguese fires, where the NMSE was more than doubled the average NMSE for all fires. This result was observed in (Anderson *et al.* 2015) analysis, with the Portugal fire subset showing a distinct dynamics than the remaining data. The source of this differences was unclear to Anderson *et al.* (2015).

Our results suggest the model relative accuracy to increase with an increase in observed rate of spread, or severity of burning conditions. For a model designed to be used operationally, errors in the slow spreading fires are somewhat inconsequential. The reduction in relative error for the fast spreading fires ensures the model can be better trusted under operational conditions where simulations for these type of fires are most needed.

Overall, the good agreement between predicted and observed ROS presented by the proposed model, with errors comparable but slightly lower than obtained with Anderson *et al.* (2015) model, suggests that it is qualified to be used to predict the propagation of shrubland fires in an

operational setting. The current formulation predicted shrubland fire spread more accurately than the radiative model derived from (Balbi *et al.* 2010) which has been implemented in the Forefire simulator (Filippi *et al.* 2011).

### Heat transfer mode

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The relative contribution of the convective and radiative heat transfer to the ROS was also analysed. The ratio of convective to radiative heat transfer for the experimental shrubland fires used in model evaluation was above 1 for 79.7% of the fires, implying convection to be the dominant heat transfer mode in these fires. These results agree with the simulations conducted by Morvan and Dupuy (2004) on mediterranean shrubs. The convection dominance is more pronounced when the model is tested against the NZ data which present the higher wind speeds and high fuel loads. The same effect is found for the South African fires which has the second higher wind speed average of the whole dataset. So convection seems to be more dominant with high wind speeds. This trend agrees with the main tendencies provided by detailed physical models such as FireStar3D (Morvan et al. 2018) in which convection increases with wind speed. It was expected because of the definition of the ROS in the model (Eqn 21) in which the convective contribution linearly depends on wind speed. But according to the ROS expression of the proposed model, an increasing ROS reduces the value of the exponential in Eqn 21 and very fast ROS will finally cause a decreasing convective contribution to the ROS. This decrease happens for extreme wind speed values (no decrease was found in the numerical simulations performed under wind speeds up to 25 m s<sup>-1</sup>). Radiation prevails in all the fires of the Australian (SA) group which are conducted in a semi-arid environment (smaller average dead and live FMC and low fuel loads). Radiation is also dominant for fires spreading under zero wind conditions because the convective contribution is zero (Eqn 21) and the ROS is mainly driven by the flame base radiation  $(R = R_b)$ .

# Conclusion

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This work deals with the adaptation of the Balbi et al. (2020) convective-radiative surface fire propagation model originally developed to describe laboratory scale fires, to fires propagating at a field scale in shrubland fuels. The improved model is a simplified physical model which takes into account convective and radiative effects as heat transfer mechanisms and is designed to allow its application under operational conditions. The main physical characteristics of the fire front are assessed through algebraic equations. The ROS is calculated using a non-linear algebraic equation solved through an iterative method. It depends on environmental (wind velocity, ambient temperature), topographical (terrain slope angle) conditions and a number of intrinsic and extrinsic fuel characteristics (e.g. FMC, thickness, packing ratio, surface area to volume ratio, dead and live fuel load). The living part of the fuel is mainly taken into account through the contribution of live fuel load. Like other simplified physical models, the improved model is not able to use a detailed description of the fuel complex when the available biomass is composed of multiple species or layers with distinct physical structures, it needs an equivalent idealized fuel description in order to be run. The level of detail in the physical conservation laws, the low computational cost (faster than real time) and the observed good agreement obtained against independent data are encouraging results obtained in the present work. With model parameterization requiring only a restricted number of experimental fires, the model framework has potential to be extended to different fuel types such as grasslands and conifer forests, by using existent datasets. The model can be implemented in fire spread simulators such as ForeFire (Filippi et al. 2011) and it is currently being tested within the couple atmosphere-fire model WRF-Sfire (Kochanski et al. 2013).

### **Conflict of Interest**

508 The authors declare they have no conflicts of interest. **Acknowledgements** 509 510 The present work was supported in part by the Corsican Region under Grant GOLIAT 2020-2023. The authors also wish to thank Dr. E. Bilgili for sharing its corrected data on his field 511 512 experiments. 513 References 514 Albini FA (1985) A Model for Fire Spread in Wildland Fuels by-Radiation. Combustion 515 Science and Technology 42, 229–258. doi:10.1080/00102208508960381. 516 Albini FA (1986) Wildland Fire Spread by Radiation - a Model Including Fuel Cooling by 517 Natural Convection. Combustion Science and Technology 45, 101–113. 518 Anderson HE (1969) Heat transfer and fire spread. (U.S. Department of Agriculture, Forest 519 Service, Research Paper INT-69) 520 Anderson WR, Catchpole EA, Butler BW (2010) Convective heat transfer in fire spread through 521 fuel International Journal Wildland fine beds. Fire **19**. 284–298. doi:10.1071/WF09021. 522 523 Anderson WR, Cruz MG, Fernandes PM, McCaw L, Vega JA, Bradstock RA, Fogarty L, Gould 524 J. McCarthy G. Marsden-Smedley JB, Matthews S, Mattingley G, Pearce HG, Van Wilgen 525 BW (2015) A generic, empirical-based model for predicting rate of fire spread in 526 shrublands. International Journal of Wildland Fire 24, 443–460. doi:10.1071/WF14130. 527 Andrews PLPP (1986) BEHAVE: Fire Behavior Prediction and Fuel Modeling System - BURN 528 Subsystem, Part 1. (Ogden, UT 84401) http://digitalcommons.usu.edu/barkbeetles/151/.

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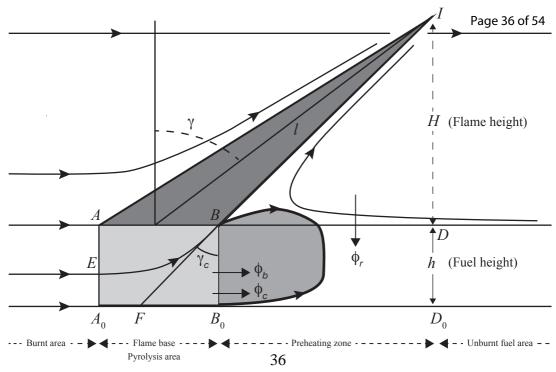
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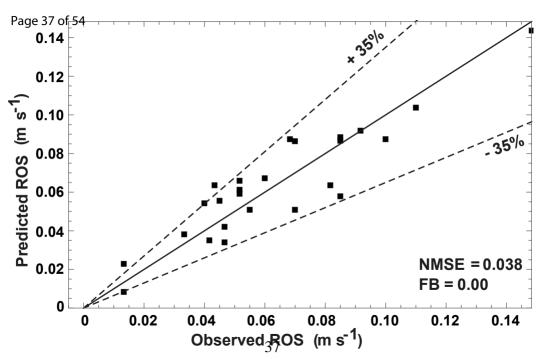
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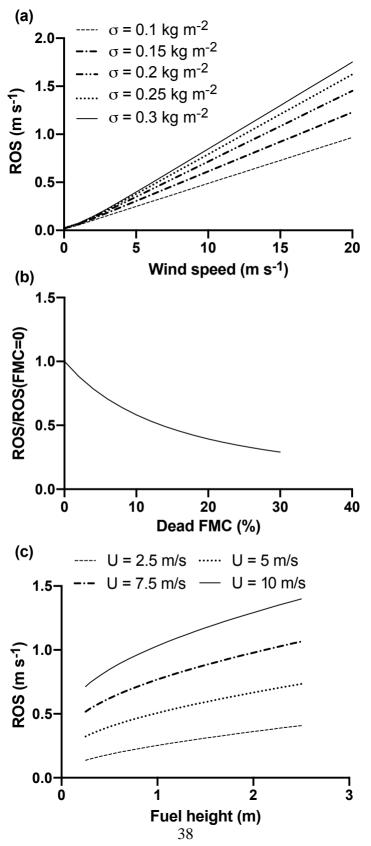
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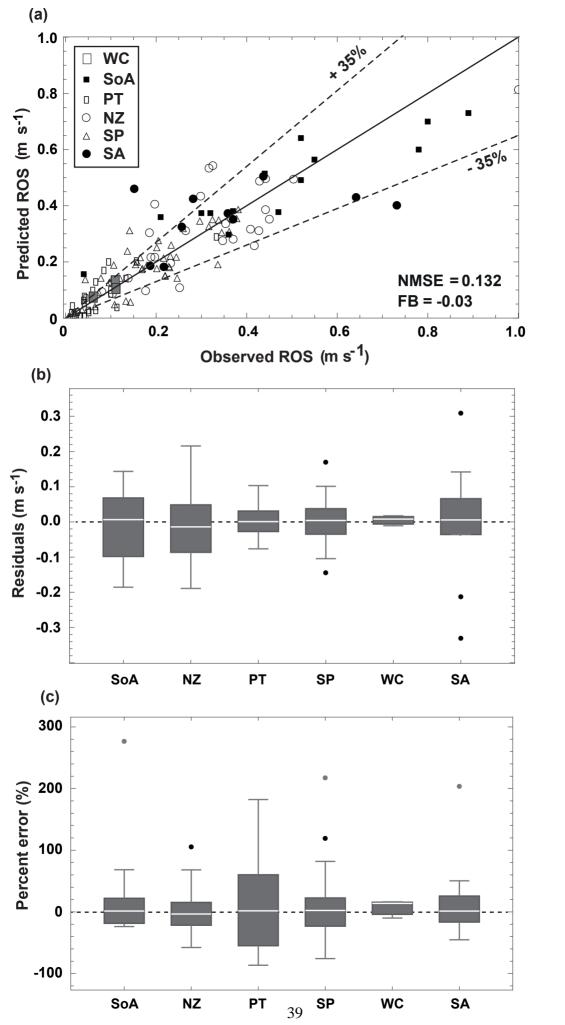
The manuscript proposes an extension of the Balbi model to the field scale. In addition to the necessary modelling section, we made a comparison between the results obtained with the proposed model and more than 100 experimental shrubland fires picked up in the literature. As the previous version of the Balbi model (developed at the laboratory scale) was published in IJWF (2020), and due to the very interesting comments from the fire community we received, we believe that the IJWF is the most appropriate outlet for the present manuscript given its broad reach to an operational and scientific readership.

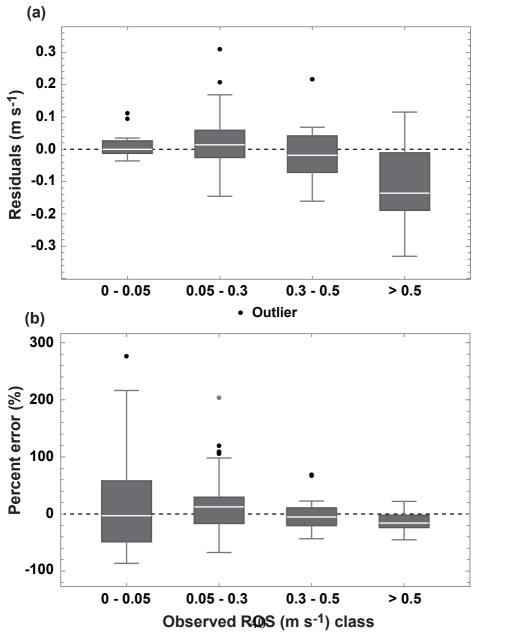
The main interest of this work is to propose a simplified physical model designed to be used under operational conditions. The model takes explicitly into account the triangle of fire (wind, slope and main fuel characteristics), is fully predictive, faster than real time and can be easily used at the field scale with a good accuracy.

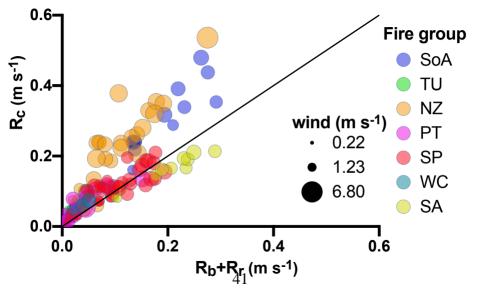


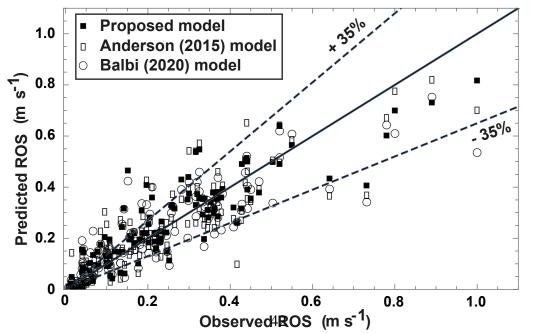


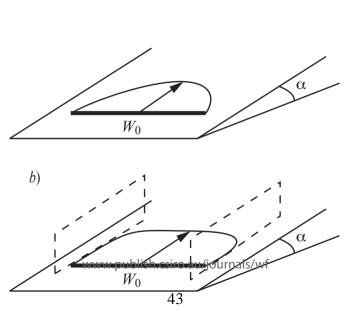


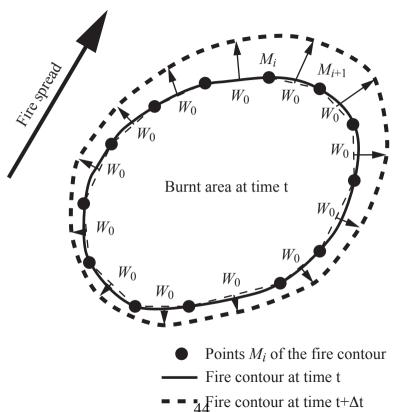












4	Radiant coefficient	
a	Scaling factor	
$a_{lat}, a_{liv}, a_{up}$	Intermediate Scaling factors	
$a_M$	Fitted model parameter	= 0.025
В	Stefan-Boltzmann constant (W m <sup>-2</sup> K <sup>-4</sup> )	$= 5.6 \times 10^{-8}$
C <sub>mw</sub>	Specific heat of water (J kg-1 K-1)	= 4180
$C_n^p$	Specific heat of fuel (J kg <sup>-1</sup> K <sup>-1</sup> )	
$C_{pw} \ C_p \ C_{pa}$	Specific heat of air (J kg <sup>-1</sup> K <sup>-1</sup> )	= 1150
2 <sup>r</sup>	Gravity acceleration (m s <sup>-2</sup> )	= 9.81
g h	Fuel bed depth (m)	
H	Flame height (m)	
K	Law for drag forces	
$K_1$	Drag coefficient (s m <sup>-1</sup> )	= 130
L	Flame depth (m)	150
1	Flame length (m)	
n	Fuel moisture content	
	Ignition energy (J kg <sup>-1</sup> )	
7	Model coefficient	$= 2.5 \cdot 10^{-5}$
700 <b>?</b>	Rate of fire spread (m s <sup>-1</sup> )	- 2.3 10
	± ', ',	DOS (m a-1)
$R_b$	Contribution of radiation of burning fuel bed to the	KOS (III S <sup>-</sup> )
$R_c$	Contribution of convection to the ROS (m s <sup>-1</sup> )	
$R_r$	Contribution of flame radiation to the ROS (m s <sup>-1</sup> )	
S	Surface area to volume ratio of fuel (m <sup>-1</sup> )	
S	Leaf area by square meter (m <sup>2</sup> m <sup>-2</sup> )	1.7
$S_t$	Air-pyrolysis gases mass ratio in the flame body	= 17
T	Mean flame temperature (K)	200
$T_a$	Ambient temperature (K)	= 300
$T_i$	Ignition temperature (K)	= 600
$T_{vap}$	Vaporization temperature (K)	= 373
U	Sum of normal component (to the fire front) of the	
	and fire generated inflow coming from the burnt ar	
U(x)	Air stream velocity within the burning fuel bed (m	
$u_c$	Upward gas velocity at the top of the flame base (n	n s <sup>-1</sup> )
$u_0$	Upward gas velocity at mid-height flame body on f	flat terrain (m s <sup>-1</sup> )
$W_0$	Ignition line width (m)	
Greek symb	ols	
	Terrain slope angle (°)	
$\alpha$	- · · · · · · · · · · · · · · · · · · ·	
	Packing ratio	
3	Packing ratio Extinction depth	
3 8	Extinction depth	
3 8 7	Extinction depth Flame tilt angle (°)	
3 5 v Vc	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°)	
3 5 7 7 6	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°) Flame emissivity	
3 5 7 7/c 5	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°) Flame emissivity Radiative fraction	
β δ γ γ <sub>c</sub> ε χ	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°) Flame emissivity Radiative fraction Radiant factor	= 0.3
β δ γ γ <sub>c</sub> ε	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°) Flame emissivity Radiative fraction	
β δ γ γ <sub>c</sub> ε χ	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°) Flame emissivity Radiative fraction Radiant factor	
β δ γ γ <sub>c</sub> ε λ λ Δ <i>H</i>	Extinction depth Flame tilt angle (°) Angle defined in fig. 1 (°) Flame emissivity Radiative fraction Radiant factor Heat of combustion of the pyrolysis gases (J kg <sup>-1</sup> )	$= 1.74 \times 10^7$

$\sigma$	Dead fine fuel load (kg m <sup>-2</sup> )
φ	Heat flux per unit length (W m <sup>-1</sup> )
$ au_0$	Flame residence time parameter (s $m^{-1}$ ) = 75591
τ	Flame residence time (s)
Subscripts	
a	Related to air
b	Related to the flame base
c	Related to the convective warming
r	Related to the flame body
t	Related to total fuel (dead and live fuel)
w	Related to the fuel water
Acronyms	
CFD	Computational fluid dynamics
FB	Fractional bias
FMC	Fuel moisture content
LAI	Leaf area index
NMSE	Normalized mean square error
ROS	Rate of spread

Parameter	Default	Effect on ROS	
	value	(+10%)	(-10%)
Surface area to volume ratio (m <sup>-1</sup> )	6000	+8.9%	-10.4%
Fuel density (kg m <sup>-3</sup> )	500	-12.2%	+13.6%
Heat of combustion of pyrolysis gases (J kg <sup>-1</sup> )	$1.74\times10^7$	10.8%	-10.2%
Fuel specific heat (J kg <sup>-1</sup> K <sup>-1</sup> )	2000	-8.4%	+9.8%
Fuel height (m)	0.5	+4.9%	-5.1%
Dead fuel moisture content	0.1	-4.4%	+4.7%
Dead fuel loading (kg m²)	0.3	+0.8%	-1.5%
Total fuel loading (kg m²)	0.5	-3.5%	+2.7%

Dataset [nb of fires]	NMSE [FB]				
	Proposed model	Anderson <i>et al</i> (2015) model	Balbi <i>et al</i> (2010) radiative model	Balbi <i>et al</i> (2020) model	
New Zealand (NZ) [28]	0.111 [-0.02]	0.190 [-0.09]	30.956 [-1.77]	0.188 [-0.15]	
Portugal (PT) [24]	0.308 [-0.14]	0.792 [0.04]	12.803 [-1.63]	0.418 [0.05]	
Spain (SP) [44]	0.095 [-0.04]	0.095 [-0.16]	9.833 [-1.54]	0.146 [-0.03]	
Australia (WC) [3]	0.018 [0.06]	0.146 [0.34]	48.232 [-1.92]	0.093 [0.00]	
Australia (SA) [10]	0.213 [0.06]	0.241 [-0.08]	1.796 [-0.88]	0.261 [-0.04]	
South Africa (SoA) [14]	0.048 [0.09]	0.056 [0.2]	9.735 [-1.53]	0.058 [0.16]	
All [123]	0.132 [-0.03]	0.180 [-0.05]	11.528 [-1.56]	0.183 [-0.02]	

## Appendix A – Models for comparison purpose

Balbi et al. (2010) model

The first version of the Balbi model was presented in 2007. This simplified semi-physical model (Balbi et al. 2007) was designed to be used in operational situations. Following Albini (1985, 1986), this model assumed that radiation was the main heat transfer mode. But several limitations appeared: (1) some physical characteristics of the fire front were defined thanks to empirical relationships (for instance, the flame height is obtained with the McCaffrey correlation (McCaffrey 1979)); (2) many model parameters varied from a fire to another which lead to a non predictive model. Balbi et al. (2009) suggested the replacement of empirical relationships by physical laws. Actually, the flame height expression was derived from the equation for the vertical momentum applied to the flame and replaced the McCaffrey correlation. Balbi et al. (2010) came up with a better modelling for the radiative fraction and introduced a fresh cooling which models the backfire better. This improved radiative model was successfully applied to a set of laboratory experiments performed by Viegas (2004), under strong wind velocities (up to 11 m s<sup>-1</sup>) with non-parallel wind and slope conditions. Moreover Weise et al. (2016) showed that the results given by this radiative model applied to laboratory experiments across litter fuel beds provided good results. But some shortcomings remained: (1) the model was still restricted to radiation heat transfer and then poorly represented a fire spread in well-ordered, vertically oriented fuel beds where convection is the dominant heat transfer mechanism (Wolff et al. 1991; Finney et al. 2013) and (2) the model still had empirical parameters and thus was not a predictive one. Later this last point was corrected and led to the radiative Balbi model defined by Eqn A1.

$$R = \min\left(\frac{S_t}{\pi}, 1\right) \left(\frac{S}{S_t}\right)^2 \frac{BT^4}{\beta \rho_v q} + AR \frac{(1 + \sin \gamma - \cos \gamma)}{1 + \frac{R\cos \gamma}{Sr_{00}}}$$
(A1)

This model is fully predictive and a good agreement is obtained when it is compared to laboratory experiments in which radiation is the heat dominant transfer mechanism. Note that Eqn A1 is a two order polynomial equation and its solution is given by:

$$R = \frac{-(r_0 - R_b \cos \gamma - r_0 A (1 + \sin \gamma - \cos \gamma)) + ((r_0 - R_b \cos \gamma - r_0 A (1 + \sin \gamma - \cos \gamma))^2 + 4r_0 R_b \cos \gamma)^{\frac{1}{2}}}{2\cos \gamma}$$
(A2)

Anderson et al. (2015) shrubland model

Anderson *et al.* (2015) developed two generic-empirical models based on an extended dataset of shrubland fires. In the comparative model analysis used here we used the fuel height model (in the present notations and units):

$$R = \frac{1}{60} 5.6715 (3.6 U)^{0.9102} h^{0.2227} exp(-7.662 m)$$
(A3)

With U being wind speed (m s<sup>-1</sup> in the equation above) measured at 10-m in the open, h being fuel height (m) and m the moisture content of dead fine fuels. A correction is done for fires spreading in zero-wind conditions in order to avoid zero-ROS. This model is designed for fires with a fireline width ( $W_0$ ) greater than 50 m. Otherwise, Anderson and her co-authors adapted Eqn A3 in order to take into account fireline width in the following way:

$$R = \left(\frac{1}{60} \, 5.6715 \, (3.6 \, U)^{0.9102} \, h^{0.2227} \, exp(-7.662 \, m)\right) \frac{1}{1 + 9 \, Exp(-0.00316 \, W_0^2)} \tag{A4}$$

Balbi et al. (2020) model

Balbi *et al.* (2020) combined the modelling approach of Chatelon *et al.* (2017) that incorporate convective heat transfer with its radiative only model (Eqn A1) (Balbi et al. 2010) in order to obtain a complete simplified physical model that explicitly take into account convective and radiative heat transfer. The main equation of the model is written as follows (see (Balbi *et al.* 2020) for details):

$$R = \min\left(\frac{S}{\pi}, 1\right) \frac{BT^4}{\beta \rho_{\nu} q} + \frac{s \Delta H}{q \tau_0} \min\left(h_{s \beta}, \frac{2\pi}{\beta}\right) \left(\frac{h}{2h + H} \tan \alpha + \frac{U Exp(-K_1 \beta^{\frac{1}{2}} R)}{u_0}\right) + AR \frac{1 + \sin \gamma - \cos \gamma}{1 + \frac{R \cos \gamma}{s r_{00}}} \quad (A5)$$

## Appendix B – Fire ignition line length

The improved model is a steady-state simplified physical model which gives the ROS for the most advanced point of the head fire front as shown in Fig. 8. The fuel bed width is usually small at laboratory scale (more or less 1 m) and the heat loss on the lateral edges of the fuel bed may be important and may play a role on the fire spread. But if the experimental apparatus is equipped with lateral walls, there is no lateral heat loss. As the (Catchpole *et al.* 1998) laboratory experiments were carried out across fuel beds lined with lateral walls, the model proposed by Balbi *et al.* (2020) does not take into account this lateral heat loss effect and the factor  $a_{lat}$  (Eqn 12) does not explicitly appear in the model because it is always equal to 1.

At field scale, except for trench fires, this effect may influence the head fire rate of spread only if the fireline width  $W_0$  is smaller than a certain value. It is assumed that this effect does not play any role on the R if  $W_0$  is greater than 50 m, which leads to the expression of the factor  $a_{lat}$  (Eqn 12).

The improved model is designed to be used under field operational conditions. For instance, if the model is inserted into a simulator, it does not need any mesh to calculate the fire contour. Each point of the fire perimeter at time  $t+\Delta t$  is obtained with the external unit normal vector to the fire front from the fire perimeter at time t. As presented in Fig. 11,  $W_0$  represents the distance between two consecutive points of the fire perimeter at time t. Indeed, as showed in Fig. 9, two points  $(M_i, M_{i+1})$  of the fire contour at time t allow the calculation of a point of the new fire contour at time  $t+\Delta t$  and t0 which is the distance between t1 and t2 and t3 are ignition line length. This is one major advantage of the model.

## 1 Appendix C – Expression of the convective heat flux

2 The convective heat flux is defined by Eqn 15. Combining Eqns 15, 16 and 18-19 yields

$$3 \qquad \phi_c = \frac{\Delta H}{2\tau_0} \sigma s \min\left(h, \delta\right) \left( \tan \alpha + U \frac{h}{h + \frac{H}{2}} \frac{Exp\left(-\frac{\beta_t}{\min\left(\frac{W_0}{50}, 1\right)}R\right)}{u_c}\right) \tag{C1}$$

- 4 The expression of upward gas velocity  $u_c$  computed at the top of the flame base does not change
- 5 from (Balbi *et al.* 2020):

6 
$$u_c = \frac{h}{h + \frac{H}{2}} \frac{u_0}{2}$$
 (C2)

7 Substituting Eqn C2 in Eqn C1, yields:

8 
$$\phi_c = \frac{\Delta H}{\tau_0 u_0} \sigma s \min \left( h, \delta \right) \left( \frac{u_0 \tan \alpha}{2} + U Exp \left( -\frac{\beta_t}{\min \left( \frac{W_0}{50}, 1 \right)} R \right) \right)$$
 (C3)

- 9 Upward gas velocity at flame mid-height  $u_0$  is also slightly changed because of the living part
- of the fuel. Indeed, following (Balbi et al. 2009), the simplified mass balance at flame mid-
- height equilibrate the rate of gas flow which enters the flame and the sum of the pyrolysis gases
- flow rate and the flow rate of the fresh air absorbed by the flame:

13 
$$\rho u_{02}^{\ L} = (s_t + 1)L\dot{\sigma}_u \frac{h_u}{h}$$
 (C4)

- where  $\rho$ ,  $s_t$ ,  $h_u$  and  $\dot{\sigma}_u$  are the gas density, a stoichiometric coefficient, the fuel bed depth under
- combustion and the derivative of the effective fuel load over time. The modelling of the ratio
- 16  $h_u/h$  is the same as in (Balbi *et al.* 2020), except for the leaf area changed in the total leaf area:

17 
$$\frac{h_u}{h} = \min\left(1, \frac{h}{\delta}\right) = \min\left(1, \frac{2\pi}{S_t}\right)$$
 (C5)

- Finally, following exactly the calculations performed in Appendix B of (Balbi et al. 2020), the
- slight variation of the upward gas velocity is obtained:

$$20 u_0 = 2 \frac{(s_t + 1)}{\tau_0} \frac{\rho_v}{\rho_a} \frac{T}{T_a} \min \left( S, \frac{2\pi S}{S_t} \right) (C6)$$

- 21 Moreover, using the definition of the leaf area  $S = s h \beta$  and extinction depth  $\delta = 2\pi/(s \beta_t)$  the
- 22 following simplification is obtained:

23 
$$\min\left(S, \frac{2\pi S}{S_t}\right) = \min\left(s \ h \ \beta, \frac{2\pi \beta}{\beta_t}\right) = s \ \beta \min\left(h, \frac{2\pi}{S}\right) = s \ \beta \min\left(h, \delta\right)$$
 (C7)

24 Substituting Eqns C6 and C7 in Eqn C3 yields:

$$\phi_c = \frac{\Delta H \rho_a T_a}{2(s_t + 1)\rho_v T \beta} \sigma \left( \frac{(s_t + 1)}{\tau_0} \frac{\rho_v}{\rho_a} \frac{T}{T_a} \min \left( S, \frac{2\pi S}{S_t} \right) \tan \alpha + U Exp \left( -\frac{\beta_t}{\min \left( \frac{W_0}{50}, 1 \right)} R \right) \right)$$
(C8)

- 26 Finally, the contribution of the convective effects to the ROS is obtained in combining Eqns 3,
- 27 14 and C8:

$$R_c = a_M \min\left(\frac{W_0}{50}, 1\right) \frac{\Delta H \rho_a T_a s \sqrt{h}}{2q(s_t + 1)\rho_v T} \left(\frac{(s_t + 1)}{\tau_0} \frac{\rho_v}{\rho_a} \frac{T}{T_a} \min\left(S, \frac{2\pi S}{S_t}\right) \tan \alpha + U Exp\left(-\frac{\beta_t}{\min\left(\frac{W_0}{50}, 1\right)}R\right)\right)$$
(C9)

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